

## THE MORPHODYNAMICS E-BOOK: A LABOR OF LOVE THAT NEVER QUITE GETS FINISHED

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Acknowledging the help of Enrica Viparelli Ruiyu Wang Greg Wilkerson Wes Lauer Chris Paola and many others





## GETTIN' TIME TO PUT THIS OLD HORSE OUT TO PASTURE (me not the e-book)

### 1990

The "ACRONYM" series of Pascal programs for computing bedload transport in gravel rivers. G. Parker, External Memorandum M-220, St. Anthony Falls Hydraulic Laboratory, University of Minnesota, February 1990.

## C:\WINDOWS\system32\cmd.exe - acro

Welcome to the Pascal program "acronym1"!

This program computes gravel bedload and size distribution from specified values for the bed surface size distribution, the sediment specific gravity, and the effective bed shear velocity (based on skin friction only).

The bedload transport relation is the Oak Creek surface-based relation. Grain sizes are in mm, and shear velocity is in meters / second.

The program applies only to grain sizes in excess of 2 mm. Finer sizes must be excluded from the specified surface size distribution. There must



"ACRONYM" is an acronym for whatever contorted phrase that has "ACRONYM" at its acronym, but the default intepretation is Algorithm Causing the Regurgitation Of Number Yielding Monstrosities

## 2002



MIT (Crosby Fellow, Kelin Whipple)

Hi, Nicole, There was a priest, a nun and a camel...

## TIT (summer intensive course) Syunsuke Ikeda





## An Introduction to Moving Boundary Formulation

In the context of knickpoint migration in bedrock and Migrating bedrock-alluvial transitions

The traditional formulation for bedrock incision

$$(1 - \lambda_{p}) \left( \frac{\partial \eta}{\partial t} - \upsilon_{b} \right) = -E_{p}$$
$$\upsilon_{b} = \frac{\partial \eta_{b}}{\partial t}$$
$$E_{p} = E_{p}(A, S)$$

A = drainage area upstream of a point S = bed slope at the point

e.g. 
$$E_{I} = aA^{m}S^{n}$$
  $S = -\frac{\partial \eta}{\partial x}$ 

0

CALCULATION OF 1D AGGRADATION AND DEGRADATION IN RIVERS: NORMAL FLOW AND BACKWATER FORMULATIONS 沖積河川における河床変動(上昇、低下)の1次元数値計算 等流と漸変流によるモデル化

Ok Tedi Copper Mine, Papua New Guinea パプア・ニウギニにある銅山

Aggradation in gravel-bed reaches of Ok Tedi



銅山の排砂によるれき床領域内のテディ川の河床上昇





am presently writing an e-book; ID SEDIMENT TRANSPORT MORPHODYNAMIC with applications to RIVERS AND TURBIDITY CURRENTS he main lectures are in PowerPoint. These lectures are linked to Excel files	s , most of which serve as
raphical user interfaces for code in Visual Basic for Applications. Extended /ord. Phenomena are illustrated with mpeg video clips. @ s I finish the material, I will upload it to this web site.	d explanation is given in
→ Click for downloadable PowerPoint lectures.	35 files available
→ Click for downloadable Excel files with embedded VBA code.	28 files available
- Click for downloadable Word files with extended explanation.	5 files available
→ Click for downloadable video clips in mpg format.	13 files available
What the hell??	





## The Manischewitz Wine of Programming

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Charts Plo Charts Plo Charts Plo Charts Plo Charts Plo Charts Plo Charts Plo Street Chart Street Chart S	<pre>Worksheets(*ResultsofCalc*).tells(6 + i, 4 + 6 * Mprint + 6 Next i End Sub Sub Find_Slope_and_Load() Dis i As Integer Sl(1) = (eta(1) - eta(2)) / dx Sl(M + 1) = (eta(N) - eta(N + 1)) / dx For i = 2 To N Sl(1) = (eta(1 - 1) - eta(i + 1)) / (2 * dx) Next i For i = 1 To N + 1 Ct(1) = loadcoff * (bt * Sl(1) CtTpsera(1) = cy(1) * (R + 1) * ff1 * tiseyear / 1000000# Bbf(1) = widthcoef * (bf / Sl(1) / (1g * D) ^ 0.5) / D Hbf(1) = depthcoef * (bf / gt(1) + D Tswul(1) = Hof(1) / etaddot / avulfsc / timeyear Next 1 Find Sub Sub Find New_eta() Dis i As Integer Dis etaddotdumay As Double For i = 1 To M if i = 1 Them Cttack = Qtbffeed Else Qtback = Qtbffeed Else Qtback = Qtbffeed Else Sub i find If Ctfine &lt; ct(i + 1) eta(1) + If1 * Sinu * (1 + Imsbig) * (Qtback - Qtf Next i time = time + dt eta(N + 1) = eta(N + 1) + etaddot * dt End Sub Sub More_Cutput() Dis i As Integer Norksheets(*ResultsofCalc*).Cells(5, 4 + j).Valme = CStr(Round( Worksheets(*ResultsofCalc*).Cells(5, 4 + 2 * Mprint + 2 + j).Valme For i = 1 fo(N) For Sub Sub More_Cutput() For Sub More_Cutput() For Sub More_Calc*(*).Cells(5, 4 + 2 * Mprint + 2 + j).Valme For Sub Sub More_Calc*(*ResultsofCalc*).Cells(5, 4 + 2 * Mprint + 2 + j).Valme For Sub Sub More_Calc*(*ResultsofCalc*).Cells(5, 4 + 2 * Mprint + 2 + j).Valme For Sub Sub More_Calc*(*ResultsofCalc*).Cells(5, 4 + 2 * Mprint + 2 + j).Valme For Sub Sub More_Calc*(*ResultsofCalc*).Cells(5, 4 + 2 * Mprint + 2 + j).Valme For Sub Sub More_Calc*(*ResultsofCalc*).Cells(5, 4 + 2 * Mprint + 2 + j).Valme For Sub Sub More_Calc*(*ResultsofCalc*).Cells(5, 4 + 2 * Mprint + 2 + j).Valme For For Sub Sub More_Calc*(*ResultsofCalc*).Cells(5, 4 + 2 * Mprint + 2 + j).Valme For For Sub Sub Sub For Subsets(*ResultsofCalc*).Cells(5, 4 + 2 * Mprint + 2 + j).Valme For For Subsets(*ResultsofCalc*).Cells(5, 4 + 2 * Mprint + 2 + j).Valme For For For For For For For For For For</pre>	<pre>i).value = Bflood(i)  fmt) / (2 * dxi / Bflood(i) / (1 - 1  ((time / timeyear), 3)) + " yr"  = CStr(Round((time / timeyear), 3)) lue = CStr(Round((time / timeyear), 3))</pre>	Lanp) +



## **UH, IT NEVER GOT QUITE FINISHED**

#### Part 1: 1D Sediment Transport

13 Chapters (All Loaded)

#### Part 2: Morphodynamics of Rivers

18 Chapters (All Loaded)

#### Part 3: Fluvial Fans and Fan-deltas

4 Chapters Loaded

4 Chapters Done but not Loaded

#### 6 Chapters Not Done



Part 4: Morphodynamics of Subaqueous Fans and Fandeltas Deposited by Turbidity Currents, and Co-evolving Fluvial/Turbidity Current Fan-deltas

8 Chapters, more or less Done, none Loaded

## IT'S NOT A TOY, REALLY, IT'S GOOD FOR RESEARCH AS WELL AS TEACHING...

I mean like, rilly



## AVULSION FREQUENCY OF THE MIDDLE MISSISSIPPI RIVER DURING HOLOCENE SEA LEVEL RISE, 10,000 – 4,000 BP



## CHANNEL-FORMING FLOW: SOME E-BOOK PARAMETERS

 $\begin{array}{l} Q_{bf} = \text{bankfull discharge} \\ Q_{tbf} = \text{total bed material load at bankfull discharge} \\ I_{f} = \text{flood intermittency for bankfull discharge (I_{f}Q_{tbf} = \text{mean annual bed material load)} \\ B_{bf} = \text{bankfull width} \\ H_{bf} = \text{bankfull depth} \\ U_{bf} = \text{bankfull flow velocity} \\ S = \text{bed slope} \\ D = \text{characteristic surface grain size} \end{array}$ 

v = kinematic viscosity of water

R = ( $\rho_s/\rho - 1$ ) = sediment submerged specific gravity (~ 1.65 for natural sediment)

- g = gravitational acceleration
- $\lambda_p$  = porosity of bed sediment

### **EQUATIONS AND DIMENSIONLESS PARAMETERS**

Chezy-type resistance relation:  $C_f$  and  $Cz = C_f^{-1/2}$  are resistance coefficients

$$C_f U_{bf}^2 = g H_{bf} S$$
 or  $U_{bf} = C z \sqrt{H_{bf} S}$ 

Bankfull Shields number

$$\tau_{bf}^{*} = \frac{H_{bf}S}{RD}$$

Dimensionless grain size

$$\mathsf{D}^* = \left(\frac{\sqrt{\mathsf{R}g\mathsf{D}}\,\mathsf{D}}{\mathsf{v}}\right)^{2/3} = \mathsf{R}\mathbf{e}_{\mathsf{p}}^{2/3}$$

Dimensionless bankfull discharge bankfull bed material discharge, width, depth

$$\hat{Q} = \frac{Q_{bf}}{\sqrt{gD}D^2} \quad , \quad \hat{Q}_t = \frac{Q_{tbf}}{\sqrt{gD}D^2} \quad , \quad \hat{B} = \frac{B_{bf}}{D} \quad , \quad \hat{H} = \frac{H_{bf}}{D}$$

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1D SEDIMENT TRANSPORT MORPHODYNAMICS with applications to RIVERS AND TURBIDITY CURRENTS



#### CHAPTER 3: BANKFULL CHARACTERISTICS OF RIVERS

Alluvial rivers construct their own channels and floodplains. Channels and floodplains. Channels and floodplains co-evolve over time.



Nameless Siberian stream and floodplain. Image courtesy A. Alabyan and A. Sidorchuk.



Browns Gulch, Montana

## THEN: BANKFULL SHIELDS NUMBER

#### **BANKFULL SHIELDS NUMBER VERSUS DIMENSIONLESS DISCHARGE**

"Gravel-bed streams maintain a bankfull Shields stress that is loosely about 0.05. Sand-bed streams maintain a bankfull Shields stress that is loosely about 1.9."



### **NOW: BANKFULL SHIELDS NUMBER**



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## **NOW: BANKFULL SHIELDS NUMBER**



## THEN AND NOW: CHEZY RESISTANCE COEFFICIENT



## THE PROBLEM



Questions

- 1. Why a mean avulsion period  $T_a$  of ~ 830 years, frequency  $F_a \sim 0.0012$  per year?
- 2. Do large-scale variations in floodplain width influence local avulsion frequency?

Middle Mississippi River during late Holocene sea level rise.

- 10,000 4,000 years BP
- 3.5 mm/year sea level rise
- Apparently 5 avulsions over 6000 years near Memphis, Tennessee



## SOME PARAMETERS

Parameter	Now?	Then?
Reach length L km	> 600	~ 500 km
		(transgression)
Floodplain width B <sub>f</sub> km	30 km	30 km
Q <sub>bf</sub> m <sup>3</sup> /s	30,000	40,000?
Q <sub>tbf</sub> Mt/a	30	70?
Cz	15	15?
D mm	0.25	0.25?
$\tau_{bf}^{*}$	1.9	1.9?
Sinuosity Ω	1.5 – 2.0	1.5? (quasi- braided?
Mud contained per unit sand $\Lambda$ In channel-floodplain complex	1.5	1.5?



Channel deposits within floodplain 21

# SIMPLEST FIRST-ORDER FORMULATION (Can add many other factors in a refined model)

- 1. Normal flow model (easy to add backwater)
- 2. Set base level rise rate at downstream end: throw out details of delta formation/progradation/transgression/regression for now
- 3. No tributaries
- 4. Single sand grain size (not too difficult to add multiple grain sizes
- 5. Assume that evolution is slow enough to use a *virtual channel*
- 6. Assume that channel and floodplain have time to co-evolve in long term
- 7. Base avulsion period on time for channel to aggrade to **half of bankfull depth** (Paola, Mohrig, Straub etc.)



## THE CHANNEL(s) HAS (have) SPECIFIED BANKFULL CHARACTERISTICS, BUT NOT POSITION

• The channel (or amalgamated channels) are assumed to avulse across the available space and fill it by deposition.

• The model is designed to capture the **long-term** evolution of the system, and not the details at any specific time





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#### CHAPTER 24: APPROXIMATE FORMULATION FOR SLOPE AND BANKFULL GEOMETRY OF RIVERS

$$C_{f} \frac{Q_{bf}^{2}}{B_{bf}^{2}H_{bf}^{2}} = gH_{bf}S$$

$$Q_{tbf} = B_{bf}Q_{tbf} = \frac{\alpha_{EH}}{C_{f}}B_{bf}\sqrt{RgD}D(\tau_{bf}^{*})^{5/2}$$

$$\tau_{bf}^{*} = \frac{H_{bf}S}{RD} = \text{const.} \equiv \tau_{form}^{*}$$

momentum balance

*bed material transport*: Engelund-Hansen

 $\tau_{form}^*$  = channel-formative Shields number

#### 1D SEDIMENT TRANSPORT MORPHODYNAMICS with applications to RIVERS AND TURBIDITY CURRENTS



CHAPTER 24:

## APPROXIMATE FORMULATION FOR SLOPE AND BANKFULL GEOMETRY OF RIVERS

 $\rightarrow$ 

$$C_f \frac{Q_{bf}^2}{B_{bf}^2 H_{bf}^2} = g H_{bf} S$$

$$Q_{tbf} = B_{bf} q_{tbf} = \frac{\alpha_{EH}}{C_f} B_{bf} \sqrt{RgD} D(\tau_{bf}^*)^{5/2}$$

$$\tau^*_{bf} = \frac{H_{bf}S}{RD} = const. \equiv \tau^*_{form}$$

$$\hat{\mathsf{B}} = \frac{\mathsf{C}_{\mathsf{f}}}{\alpha_{\mathsf{EH}} (\tau_{\mathsf{form}}^*)^{2.5}} \hat{\mathsf{Q}}_{\mathsf{t}}$$
$$S = \frac{\mathsf{R}^{3/2} \mathsf{C}_{\mathsf{f}}^{1/2}}{\alpha_{\mathsf{EH}} \tau_{\mathsf{form}}^*} \frac{\hat{\mathsf{Q}}_{\mathsf{t}}}{\hat{\mathsf{Q}}}$$
$$\hat{\mathsf{H}} = \frac{\alpha_{\mathsf{EH}} (\tau_{\mathsf{form}}^*)^2}{(\mathsf{R}\mathsf{C}_{\mathsf{f}})^{1/2}} \frac{\hat{\mathsf{Q}}}{\hat{\mathsf{Q}}_{\mathsf{t}}}$$

where

$$\hat{Q} = \frac{Q_{bf}}{\sqrt{gD}D^2} \quad , \quad \hat{Q}_t = \frac{Q_{tbf}}{\sqrt{gD}D^2} \quad , \quad \hat{B} = \frac{B_{bf}}{D} \quad , \quad \hat{H} = \frac{H_{bf}}{D}$$

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#### **ENGELO-HANSO-PAOLAESQUE SEDIMENT TRANSPORT RELATION**

 $P_{tbf} = \frac{\alpha_{EH} \tau_{form}^*}{R^{3/2} C_f^{1/2}} Q_{bf} S$ 



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CHAPTER 25:

## LONG PROFILES OF RIVERS, WITH AN APPLICATION ON THE EFFECT OF BASE LEVEL RISE ON LONG PROFILES

Parameters

- $\eta$  = mean elevation of channel-floodplain complex
- x,  $x_v$  = down-channel, down-valley distance
- $\Omega$  = channel sinuosity
- $\Lambda$  = unit mud (wash load) deposited per unit sand (bed material load)
  - in channel-floodplain complex

## Exner equation of sediment balance





$$(1 - \lambda_p)B_f \frac{\partial \eta}{\partial t} = -\Omega I_f (1 + \Lambda) \frac{\partial Q_{tbf}}{\partial x}$$



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## **REDUCTION OF THE EXNER EQUATION**

The Exner equation can be expressed as

$$\frac{\partial \eta}{\partial t} = -\frac{I_{f}\Omega(1+\Lambda)}{(1-\lambda_{p})B_{f}}\frac{\partial Q_{tbf}}{\partial x}$$

Reducing with the sediment transport relation

$$Q_{tbf} = \frac{\alpha_{EH} \tau_{form}^*}{RC_f^{1/2}} Q_{bf} S$$

it is found that

$$\frac{\partial \eta}{\partial t} = \kappa_{d} \frac{\partial^{2} \eta}{\partial x^{2}} \quad , \quad \kappa_{d} = \frac{I_{f} \Omega (1 + \Lambda)}{(1 - \lambda_{p}) B_{f}} \frac{\alpha_{EH} \tau_{form}^{*} Q_{bf}}{RC_{f}^{1/2}}$$

where  $\kappa_d$  denotes a kinematic sediment diffusivity. Note that the resulting form is a *linear* diffusion equation. 28

#### **BASE LEVEL RISE AS DOWNSTREAM BOUNDARY CONDITION**

 $\dot{\xi}_{d}$  = rate of base level rise (here 3.5 mm/year) L = reach length

$$\eta(\mathsf{L},\mathsf{t}) = \xi_{\mathsf{do}} + \dot{\xi}_{\mathsf{d}}\mathsf{t}$$

Deviatoric bed elevation  $\eta_{dev}(x,t) = \eta - \eta(L,t)$ 

$$\eta = \xi_{do} + \dot{\xi}_{d}t + \eta_{dev}(\mathbf{x}, t)$$

$$\eta_{dev}(L,t) = 0$$

$$\frac{\partial \eta_{dev}}{\partial t} + \dot{\xi}_{d} = -\frac{I_{f}\Omega(1+\Lambda)}{(1-\lambda_{p})B_{f}}\frac{\partial Q_{tbf}}{\partial x} \quad \text{or} \quad \frac{\partial \eta_{dev}}{\partial t} + \dot{\xi}_{d} = \kappa_{d}\frac{\partial^{2}\eta_{dev}}{\partial x^{2}} \quad \text{,} \quad \kappa_{d} = \frac{I_{f}\Omega(1+\Lambda)}{(1-\lambda_{p})B_{f}}\frac{\alpha_{\text{EH}}\tau_{\text{form}}^{*}Q_{bf}}{\text{RC}_{f}^{1/2}}$$

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#### **AVULSION FREQUENCY AND FLOODPLAIN WIDTH VARIATION**

- $F_a$  = avulsion frequency
- $B_{fo}$  = base floodplain width
- $\epsilon_{\text{BF}}$  = dimensionless amplitude of floodplain width fluctuation
- n = number of width variation wavelengths within total reach length L

$$F_{a} = \frac{1}{2} \left( \frac{\partial \eta}{\partial t} \right) / H_{bf}$$
$$B_{f} = B_{fo} \left[ 1 + \varepsilon_{BF} \sin \left( 2\pi n \frac{x}{L} \right) \right]$$

## CALCULATIONS WITH MODIFIED VERSION OF

RTe-book1DRiverwFPRisingBaseLevelNormal.xls

We look only at quasi-equilibrium aggradation, e.g. of the following form (ignore the numbers)

Long Profiles of Bed Elevation



today's river with 3.5 mm/year of imposed sea level rise, constant floodplain width

**Bankfull Width** 



today's river with 3.5 mm/year of imposed sea level rise, constant floodplain width

Slope



#### CASE: today's river with 3.5 mm/year of imposed sea level rise, constant floodplain width

#### **Bankfull Depth**



# today's river with 3.5 mm/year of imposed sea level rise, constant floodplain width

**Bed Material Load** 



today's river with 3.5 mm/year of imposed sea level rise,

constant floodplain width



#### **Mean Avulsion Frequency**



## UPSTREAM ON AMAZON RIVER, BRAZIL, WE FIND MEANDERING RIVER ~ present-day Mississippi without levees?

"smaller"  $B_{bf}/H_{bf}$  ?

![](_page_36_Picture_2.jpeg)

![](_page_37_Picture_0.jpeg)

## PARANÁ RIVER, ARGENTINA

Wandering Closer to Mississippi River, 10,000 – 4,000 BP? "Larger B<sub>bf</sub>/H<sub>bf</sub>"

## DOWNSTREAM AMAZON RIVER, BRAZIL

## 10,000 to 4,000 BP with 3.5 mm/year of imposed sea level rise, constant floodplain width: *much wider*

**Bankfull Width** 

![](_page_38_Figure_3.jpeg)

# 10,000 to 4,000 BP with 3.5 mm/year of imposed sea level rise, constant floodplain width: *much steeper*

Slope

![](_page_39_Figure_3.jpeg)

# 10,000 to 4,000 BP with 3.5 mm/year of imposed sea level rise, constant floodplain width: *much shallower*

**Bankfull Depth** 

![](_page_40_Figure_3.jpeg)

10,000 to 4,000 BP with 3.5 mm/year of imposed sea level rise, constant floodplain width: *higher load* 

**Bed Material Load** 

![](_page_41_Figure_3.jpeg)

![](_page_42_Figure_1.jpeg)

## **Mean Avulsion Frequency**

![](_page_42_Figure_3.jpeg)

#### A MODERN ANALOG ??? TO MISSISSIPPI RIVER 10,000 TO 4,000 BP: Kosi River, India (recently avulsed)

![](_page_43_Picture_1.jpeg)

10,000 to 4,000 BP with 3.5 mm/year of imposed sea level rise, varied floodplain width, n = 2,  $\epsilon_{BF}$  = 0.7

**Mean Avulsion Frequency** 

![](_page_44_Figure_3.jpeg)

10,000 to 4,000 BP with 3.5 mm/year of imposed sea level rise, varied floodplain width, n = 2,  $\varepsilon_{BF}$  = 0.7: BACKDIRT CURVE?

Planform View of Floodplain Width and Detrended Avulsion Frequency

![](_page_45_Figure_3.jpeg)

Higher avulsion rate upstream of contraction: lower rate downstream!

![](_page_46_Picture_0.jpeg)