

Source to Sink Numerical Modeling of Whole Dispersal Systems

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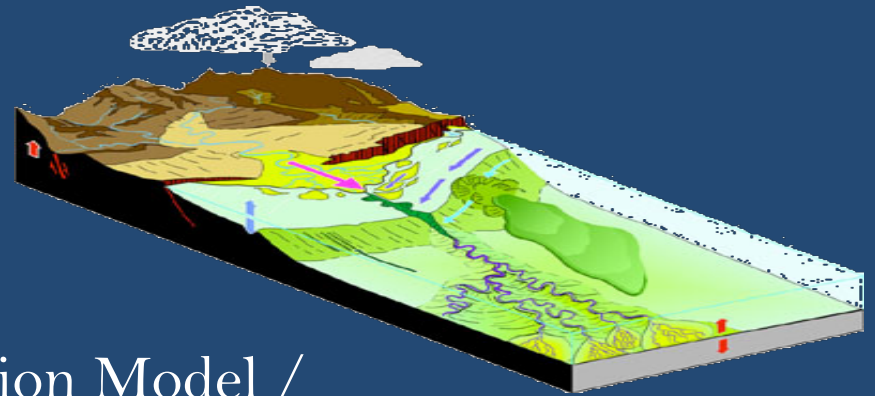
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Source to Sink Numerical Modeling

S2S models come in all shapes and sizes, depending on:

- i) intended goal,
- ii) scale of interest (space and time), and
- iii) processes & parameters being simulated

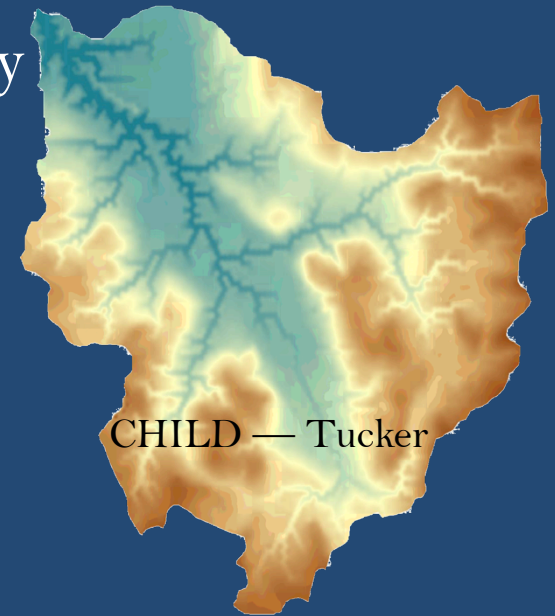


Three approaches are common:

- 1) LEM/SEM — Landscape Evolution Model /
Seascape or Stratigraphic Evolution Model
- 2) MDM — Morphodynamic Model
- 3) STM — Sediment Transport Model

S2S Modeling: 1) Landscape / Seascape Evolution Models LEM/SEM

- ✧ simulate geological time and space scales.
- ✧ incorporate geophysical & geochemical feedbacks: e.g. isostasy, eustasy, faulting, other tectonics, climate change, sea level, post-depositional compaction & cementation.
- ✧ time-integrated fluxes, or event-based, scaled to geology
- ✧ siliciclastic &/or carbonate; abiotic or biotic
- ✧ science domain: geomorphology & stratigraphy
- ✧ time step: $\sim 10^2 - 10^4$ y; duration: $\sim 10^4 - 10^7$ y
- ✧ pixel size: $\sim 10^2$ m - 10^4 m;
- ✧ spatial domain: $\sim 10^5$ m - 10^7 m
- ✧ CSDMS LEMs: CHILD, Siberia, Caesar, Erode, GOLEM, MarsSim, WILSim
- ✧ CSDMS SEMs: SedFlux, cyclopath



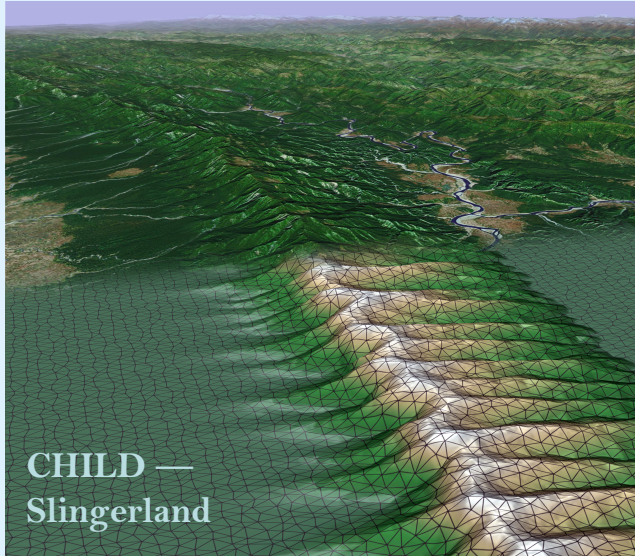
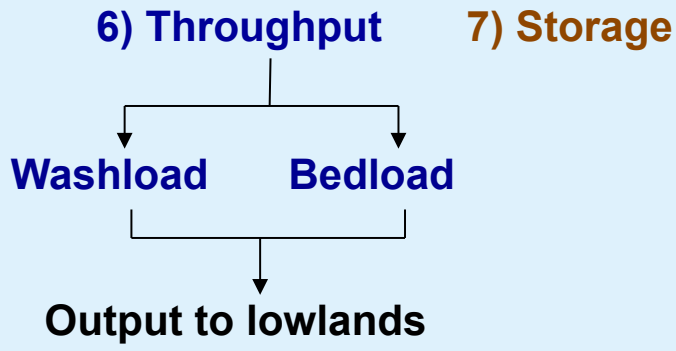
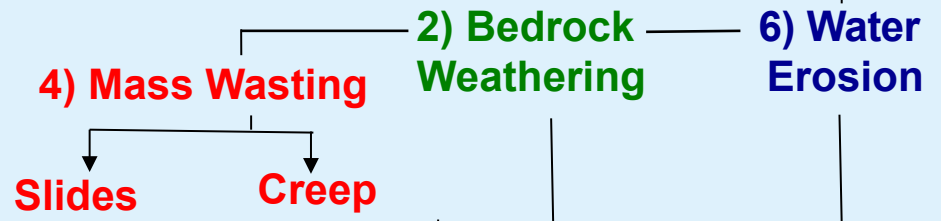
$$\underbrace{\frac{\partial z}{\partial t}}_1 = - \underbrace{\left(\frac{\sigma_r}{\sigma_s} - 1 \right) \frac{\partial e}{\partial t}}_2 - \underbrace{\frac{\partial i_{sx}}{\partial x}}_3 - \underbrace{\frac{\partial q_{sx}}{\partial x}}_4 + \underbrace{\frac{\sigma_r}{\sigma_s} U}_5 - \underbrace{E}_6 + \underbrace{D}_7$$

LEM generic example

3) Glacial sediment flux

Melt Runoff PPT Runoff

- Climate
- 5) Tectonics
- Lithology
- Eruptions
- 5) Isostasy
- Initial Geometry



CHILD — Slingerland

Each LEM term has many forms & options

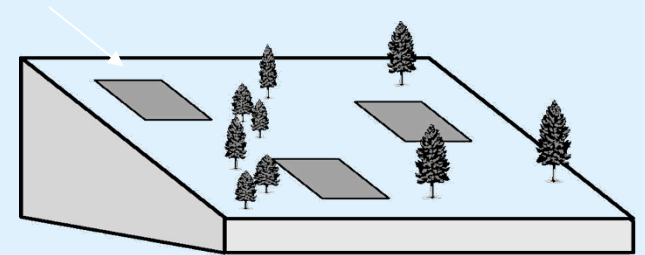
$$\frac{\partial z}{\partial t} = \underbrace{-\left(\frac{\sigma_r}{\sigma_s} - 1\right) \frac{\partial e}{\partial t}}_2 - \underbrace{\frac{\partial i_{sx}}{\partial x}}_3 - \underbrace{\frac{\partial q_{sx}}{\partial x}}_4 + \underbrace{\frac{\sigma_r}{\sigma_s} U}_5 - \underbrace{E}_6 + \underbrace{D}_7$$

$$F = \frac{c' + c + [(1 - m)\rho_b g d + m(\rho_{sat} - \rho) g d] \cos^2 \theta \tan \phi'}{[(1 - m)\rho_b + m\rho_{sat}] g d \sin \theta \cos \theta}$$

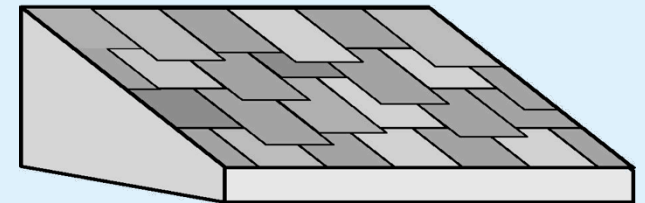
$$-\nabla q_s = \underbrace{\left(\frac{K_f S}{1 - (S/S_c)^\alpha} \right)}_{slides} - \underbrace{\left[\frac{\partial}{\partial x} \left(-K(z_x, t) \frac{\partial z}{\partial x} \right) \right]}_{creep} + \underbrace{\vartheta}_{other}$$

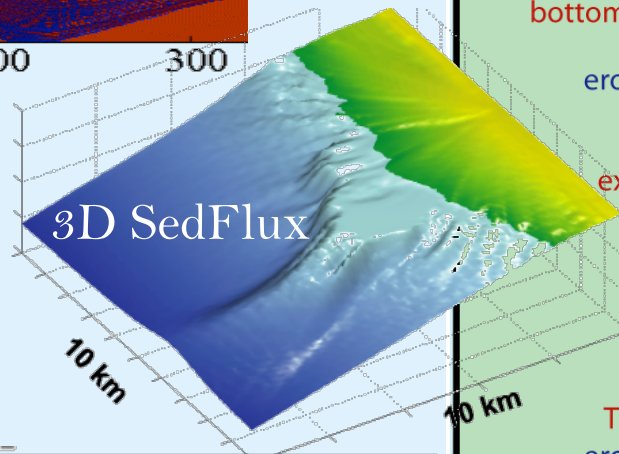
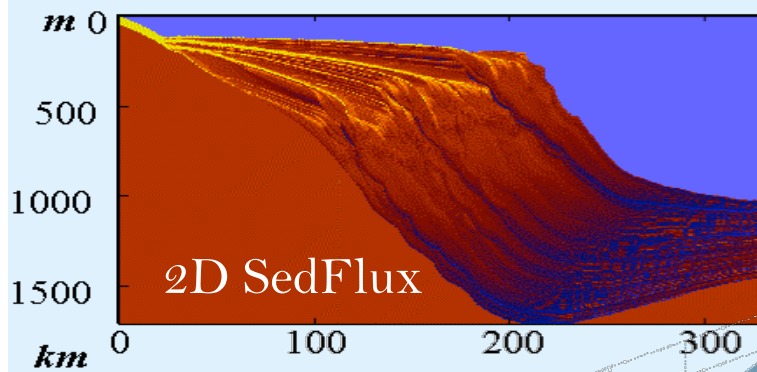
e.g. (term 4) Mass transport by gravitational processes

Landslides



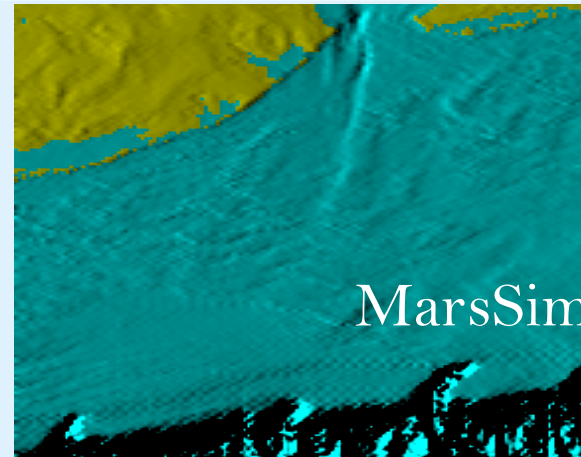
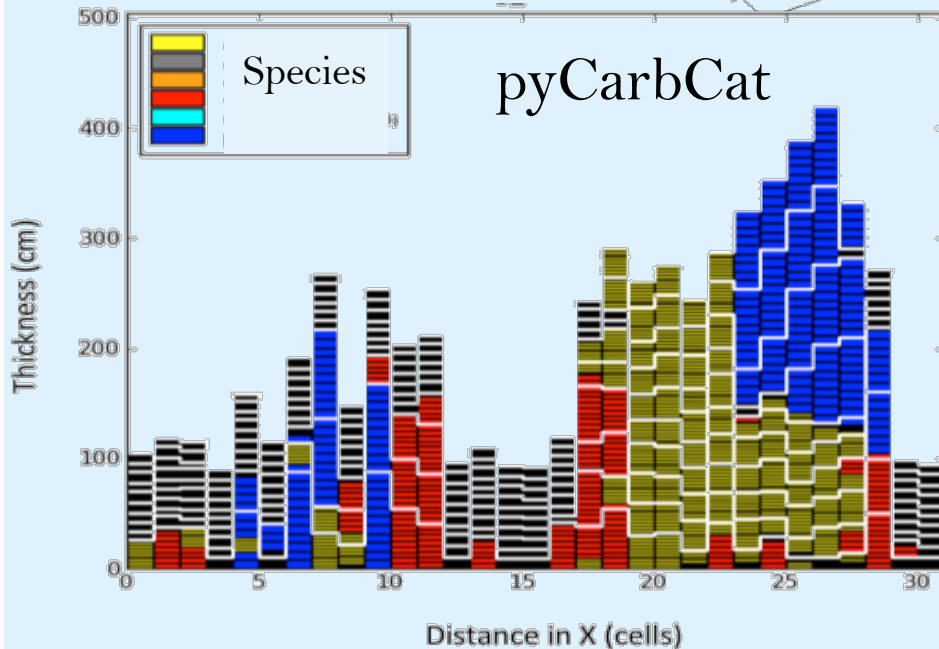
After a long time....





S2S SEM
examples:

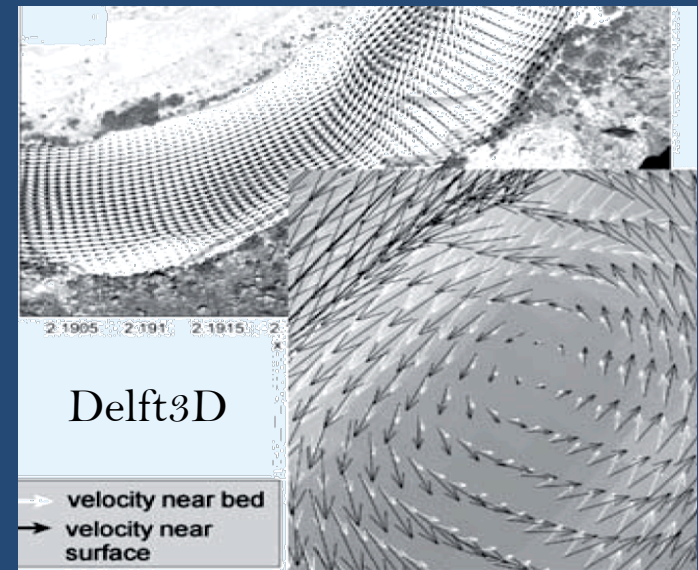
- Delta Models:**
distributary channel dynamics, channel hydraulics, bedload dynamics
longshore transport, tidal dynamics
- River Plume Models:**
hypopycnal plume dynamics, hyperpycnal plume dynamics
- Shelf Transport Models:**
bottom boundary layer dynamics (wave, current interactions)
fluid muds, upwelling, downwelling
erosion, deposition, seafloor properties, stratigraphy
- Geotechnical Models:**
compaction, porosity, permeability,
excess pore pressure, plasticity, sediment viscosity
- Slope Stability Models:**
sediment strength, potential failure planes
earthquake loading, sediment loading
Failure volume and properties
- Gravity Flow Models:**
Turbidity Current dynamics, Debris flow dynamics
erosion, deposition, seafloor properties, stratigraphy
- Geophysical Models:**
tectonics (folding, faulting), isostasy, flexural response



Howard
Fagherazzi
Wiberg

S2S Modeling: 2) Morphodynamic Models MDMs

- ✧ simulate the evolving transport pathway and mobile bed with dynamical feedback to fluid transport processes.
- ✧ may include ecodynamics.
- ✧ Advection-Diffusion Schemes, St. Venant Shallow Water Models, Reynolds-averaged Navier Stokes (RANS) models (few LES)
- ✧ both Newtonian to non-Newtonian fluids.
- ✧ science domains: engineering, hydraulics, sedimentology
- ✧ time step: $\sim 10^1 - 10^4$ s;
- ✧ duration: $\sim 10^5 - 10^8$ s
- ✧ pixel size: $\sim 10^1 - 10^3$ m;
- ✧ spatial domain: $\sim 10^3 - 10^6$ m
- ✧ CSDMS MDMs e.g.: MIDAS, CEM, Xbeach, SedFlux, Sakura, Hyper, Bing, & soon Delft3D, e-Parker

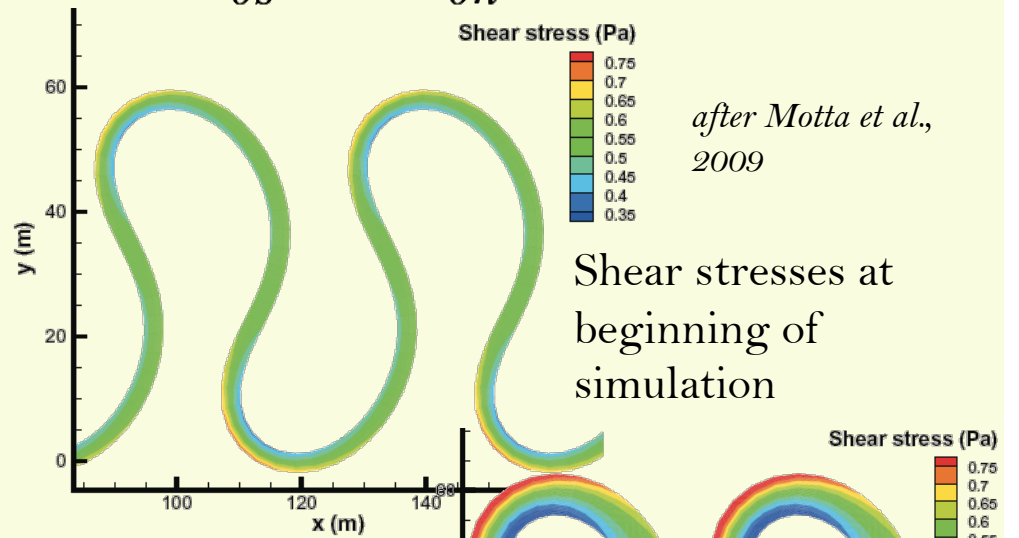
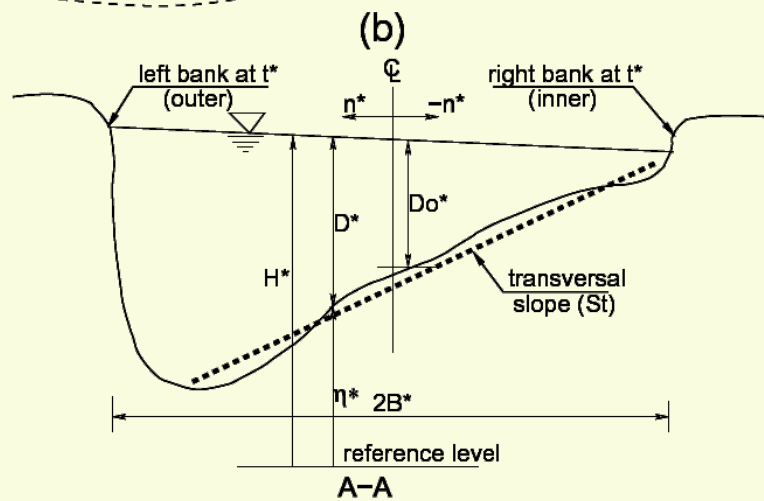
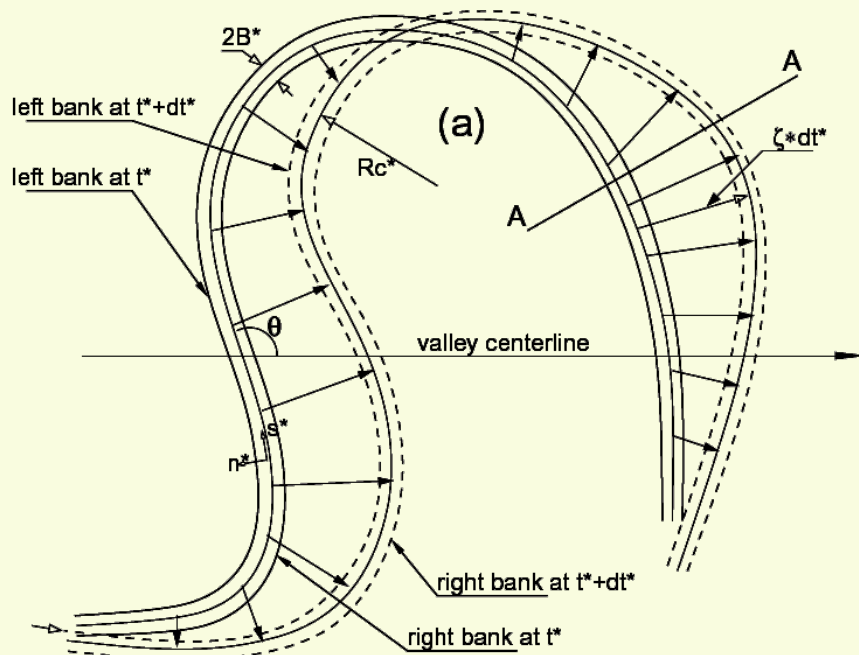


MDM Example: River meanders

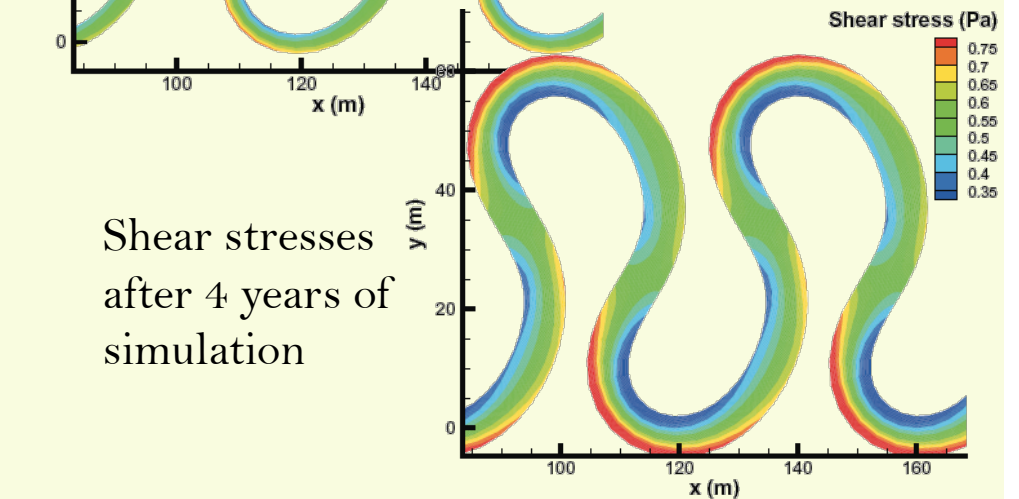
$$U \frac{\partial U}{\partial s} + V \frac{\partial U}{\partial n} + \frac{\partial H}{\partial s} + \frac{\beta \tau_s}{D} = \nu_0 f_{11}$$

$$U \frac{\partial V}{\partial s} + V \frac{\partial V}{\partial n} + \frac{\partial H}{\partial n} + \beta \frac{\tau_n}{D} = \nu_0 g_{11}$$

$$\frac{\partial(DU)}{\partial s} + \frac{\partial(DV)}{\partial n} = \nu_0 m_{11}$$



Shear stresses at beginning of simulation



Shear stresses after 4 years of simulation

BING: Lagrangian depth-averaged debris flow MDM model

Continuity

$$\underbrace{\frac{\partial h}{\partial t}}_{(a)} + \underbrace{\frac{\partial}{\partial x} \left[U_p h_p + \frac{2}{3} U_p h_s \right]}_{(b)} = 0$$

Flow height (1a)
inversely proportional
to velocity (1b).

**Momentum
(shear (s)
layer)**

$$\underbrace{\frac{2}{3} \frac{\partial}{\partial t} (U_p h_s) - U_p \frac{\partial h_s}{\partial t} + \frac{8}{15} \frac{\partial}{\partial x} (U_p^2 h_s) - \frac{2}{3} U_p \frac{\partial}{\partial x} (U_p h_s)}_{(a)} =$$

$$\underbrace{h_s g \left(1 - \frac{\rho_w}{\rho_m} \right) S}_{(b)} - \underbrace{h_s g \left(1 - \frac{\rho_w}{\rho_m} \right) \frac{\partial h}{\partial x}}_{(c)} - \underbrace{2 \left(\frac{\mu_m U_p}{\rho_m h_s} \right)}_{(d)}$$

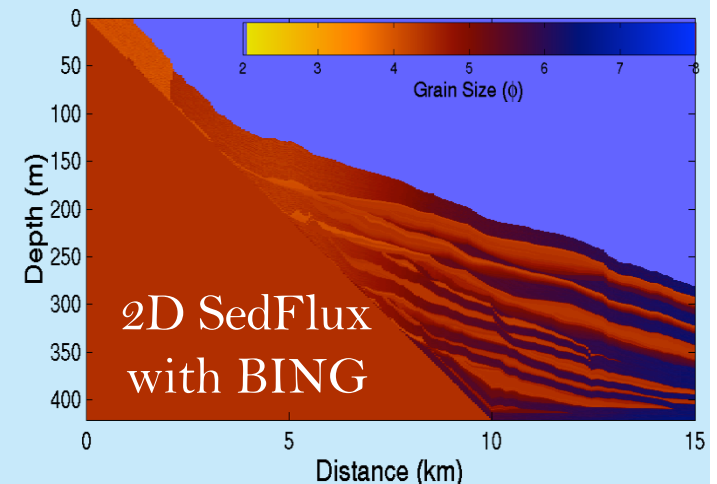
Momentum (a) balanced
by flow mass scaled by
seafloor slope (b); fluid
pressure forces produced
by flow height (c); and
friction (d).

**Momentum
(plug flow
(p) layer)**

$$\underbrace{\frac{\partial}{\partial t} (U_p h_p) + \frac{\partial}{\partial x} (U_p^2 h_p) + U_p \frac{\partial h_s}{\partial t} + \frac{2}{3} U_p \frac{\partial}{\partial x} (U_p h_s)}_{(a)} =$$

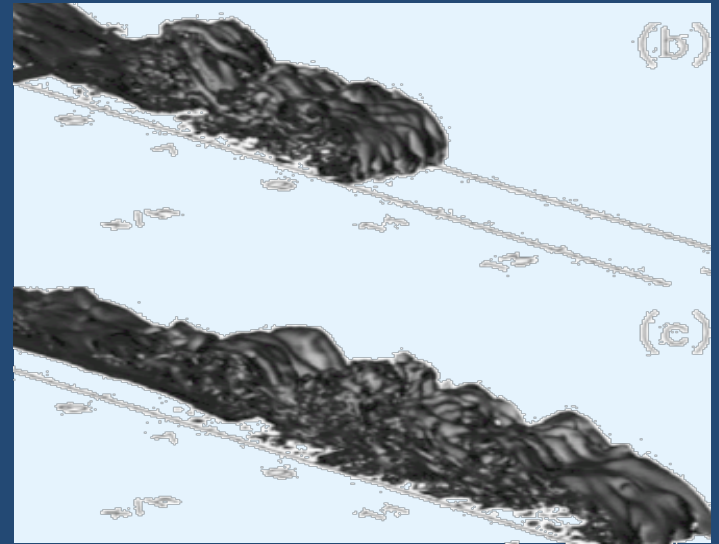
$$\underbrace{h_p g \frac{\partial}{\partial x} \left(1 - \frac{\rho_w}{\rho_m} \right) S}_{(b)} - \underbrace{h_p g \left(1 - \frac{\rho_w}{\rho_m} \right) \frac{\partial h}{\partial x}}_{(c)} - \underbrace{\frac{\tau_m}{\rho_w}}_{(d)}$$

h=height; U=layer-averaged velocity; g=gravity;
S=slope; ρ_w =ocean density; ρ_m =flow density;
 τ_m = yield strength, and μ_m =kinematic viscosity.



S2S Modeling: 3) Sediment Transport Models STMs

- ✧ material fluxes along a pathway.
- ✧ may cover multiple domains, e.g. river floods and ocean storms.
- ✧ computational fluid dynamics include Reynolds-averaged NS simulators, Large-Eddy Simulators, Direct Numerical Simulators, Boussinesq & non-hydrostatic approximations.
- ✧ science domains: oceanography, hydrology, sedimentology
- ✧ time step: $\sim 1 - 10^4$ s; duration: $\sim 10^5 - 10^8$ s
- ✧ pixel size: $\sim 10^1 - 10^5$ m; spatial domain: $\sim 10^6$ m - 10^{10} m
- ✧ CSDMS STMs e.g.: WBM-BQART, TopoFlow-Psi, HydroTrend, QUAL2K, OTEQ, OTIS, SPARROW, GNE, HSPF, LOADEST, RHESSys, SWAT, ROMS, ADCIRC



STM e.g. ROMS

$$\begin{aligned} & \frac{\partial(H_z u)}{\partial t} + \frac{\partial(u H_z u)}{\partial x} + \frac{\partial(v H_z u)}{\partial y} + \frac{\partial(\Omega H_z u)}{\partial s} - f \\ H_z v &= -\frac{H_z}{\rho_0} \frac{\partial p}{\partial x} - H_z g \frac{\partial \eta}{\partial x} - \frac{\partial}{\partial s} \left(\overline{u'w'} - \frac{v}{H_z} \frac{\partial u}{\partial s} \right) \\ & - \frac{\partial(H_z S_{xx})}{\partial x} - \frac{\partial(H_z S_{xy})}{\partial y} + \frac{\partial S_{px}}{\partial s} \end{aligned} \quad (1)$$

$$\begin{aligned} & \frac{\partial(H_z v)}{\partial t} + \frac{\partial(u H_z v)}{\partial x} + \frac{\partial(v H_z v)}{\partial y} + \frac{\partial(\Omega H_z v)}{\partial s} + f \\ H_z u &= -\frac{H_z}{\rho_0} \frac{\partial p}{\partial y} - H_z g \frac{\partial \eta}{\partial y} - \frac{\partial}{\partial s} \left(\overline{v'w'} - \frac{v}{H_z} \frac{\partial v}{\partial s} \right) \\ & - \frac{\partial(H_z S_{yx})}{\partial x} - \frac{\partial(H_z S_{yy})}{\partial y} + \frac{\partial S_{py}}{\partial s} \end{aligned} \quad (2)$$

$$\overline{u'w'} = -K_M \frac{\partial u}{\partial z}, \quad \overline{v'w'} = -K_M \frac{\partial v}{\partial z},$$

$$\overline{\rho'w'} = -K_H \frac{\partial \rho}{\partial z}$$

$$\begin{aligned} S_{xx} &= kE \left[\frac{k_x k_x}{k^2} F_{CS} F_{CC} + F_{CS} F_{CC} - F_{SS} F_{CS} \right] \\ &+ \frac{k_x k_x}{k} \frac{c^2}{L} A_R R_z \end{aligned}$$

$$S_{xy} = S_{yx} = kE \left[\frac{k_x k_y}{k^2} F_{CS} F_{CC} \right] + \frac{k_x k_y}{k} \frac{c^2}{L} A_R R_z$$

$$\begin{aligned} S_{yy} &= kE \left[\frac{k_y k_y}{k^2} F_{CS} F_{CC} + F_{CS} F_{CC} - F_{SS} F_{CS} \right] \\ &+ \frac{k_y k_y}{k} \frac{c^2}{L} A_R R_z \end{aligned} \quad (7)$$

$$0 = -\frac{1}{\rho_0} \frac{\partial p}{\partial s} - \frac{g}{\rho_0} H_z \rho \quad (3)$$

with continuity as

$$\frac{\partial \eta}{\partial t} + \frac{\partial(H_z u)}{\partial x} + \frac{\partial(H_z v)}{\partial y} + \frac{\partial(H_z \Omega)}{\partial s} = 0 \quad (4)$$

and scalar transport:

$$\begin{aligned} & \frac{\partial(H_z C)}{\partial t} + \frac{\partial(u H_z C)}{\partial x} + \frac{\partial(v H_z C)}{\partial y} + \frac{\partial(\Omega H_z C)}{\partial s} \\ &= -\frac{\partial}{\partial s} \left(\overline{c'w'} - \frac{v_\theta}{H_z} \frac{\partial C}{\partial s} \right) + C_{source} \end{aligned} \quad (5)$$

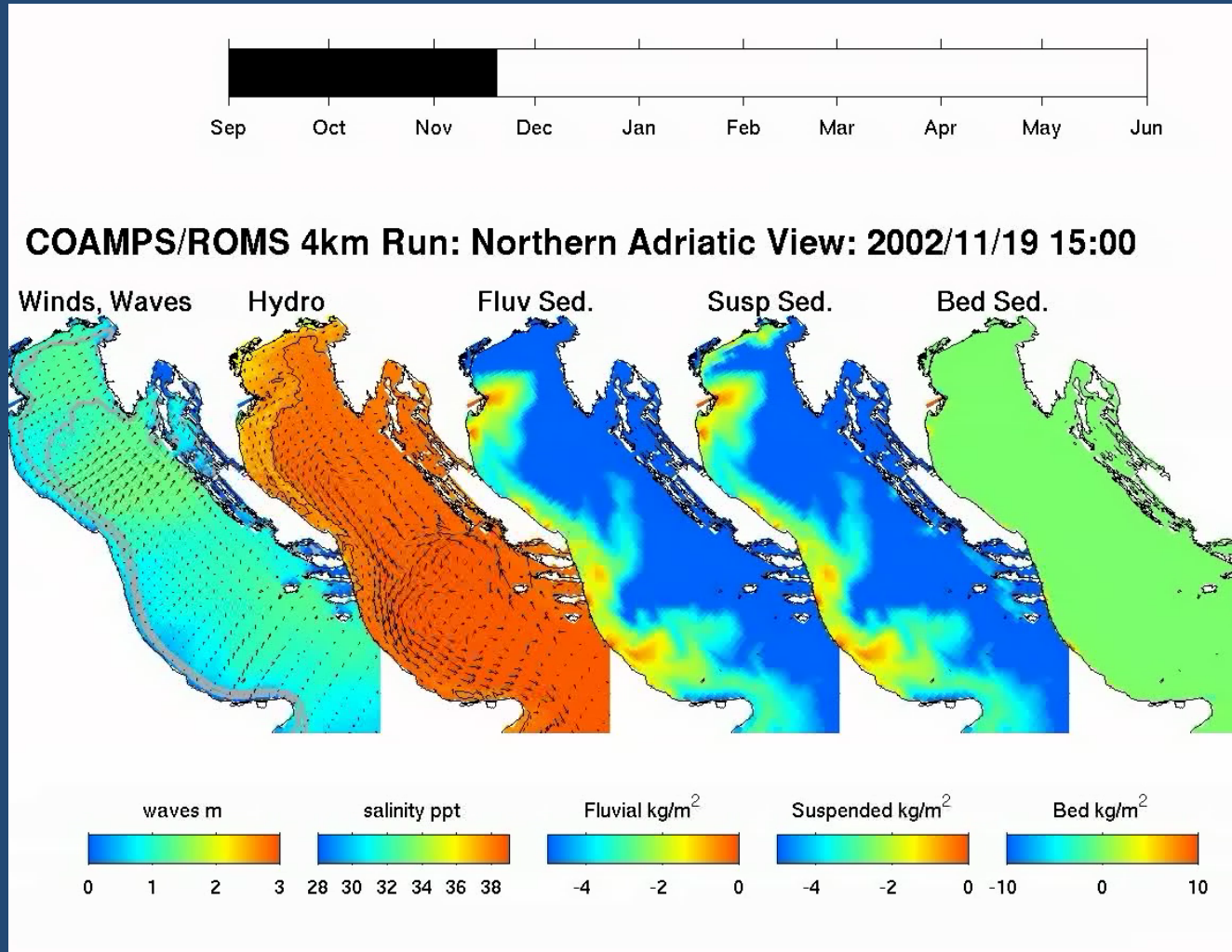
$$C_{source,m} = -\frac{\partial w_{s,m} C_m}{\partial s} + E_{s,m}$$

$$E_{s,m} = E_{0,m} (1 - \phi) \frac{\tau_{sf} - \tau_{ce,m}}{\tau_{ce,m}}, \quad \text{when } \tau_{sf} > \tau_{ce,m}$$

SWAN (wave action density)

$$\frac{\partial N}{\partial t} + \frac{\partial c_x N}{\partial x} + \frac{\partial c_y N}{\partial y} + \frac{\partial c_\sigma N}{\partial \sigma} + \frac{\partial c_\theta N}{\partial \theta} = \frac{S_w}{\sigma}$$

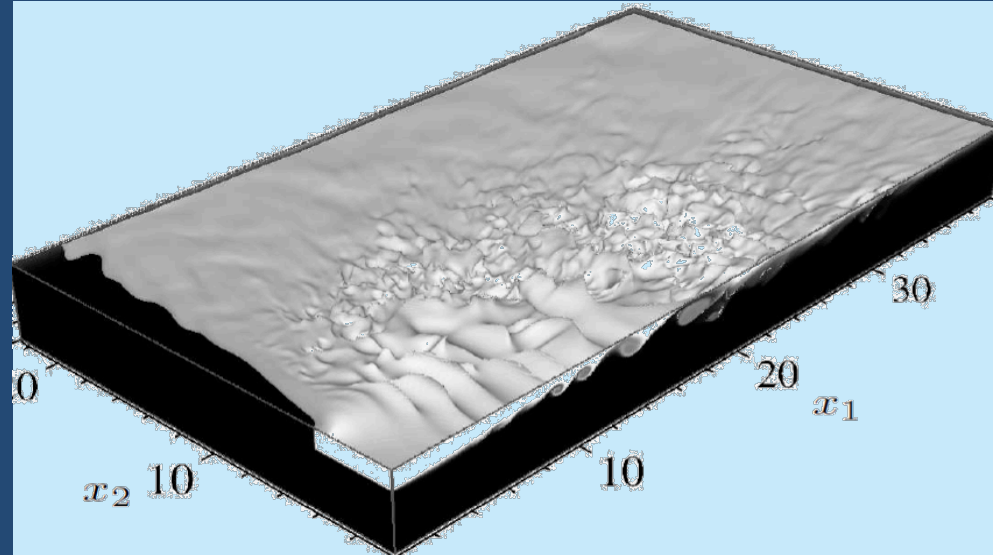
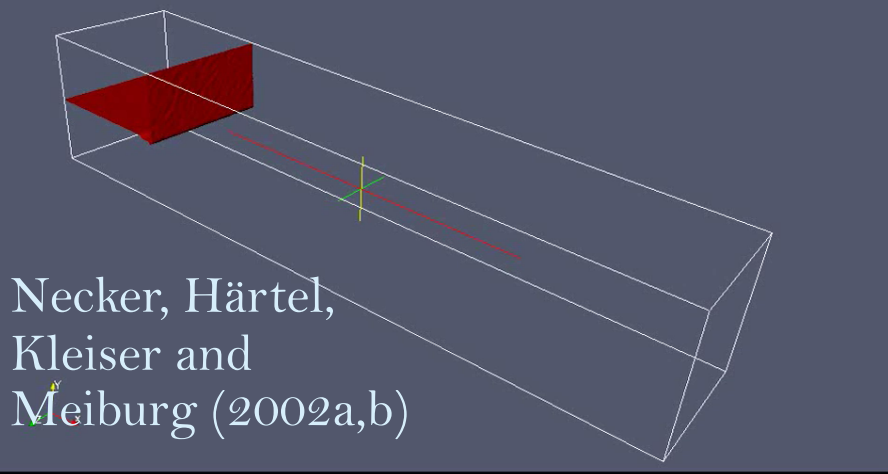
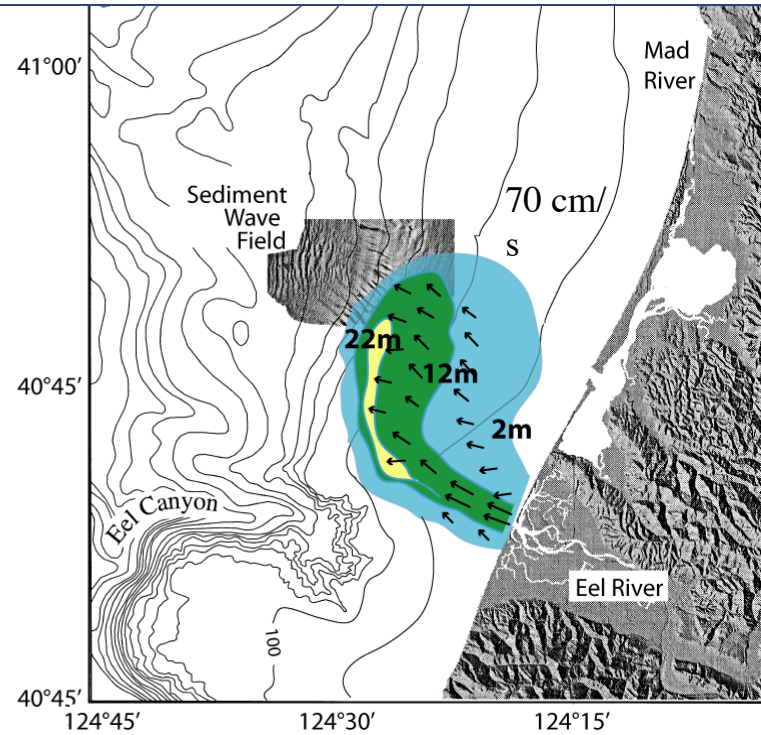
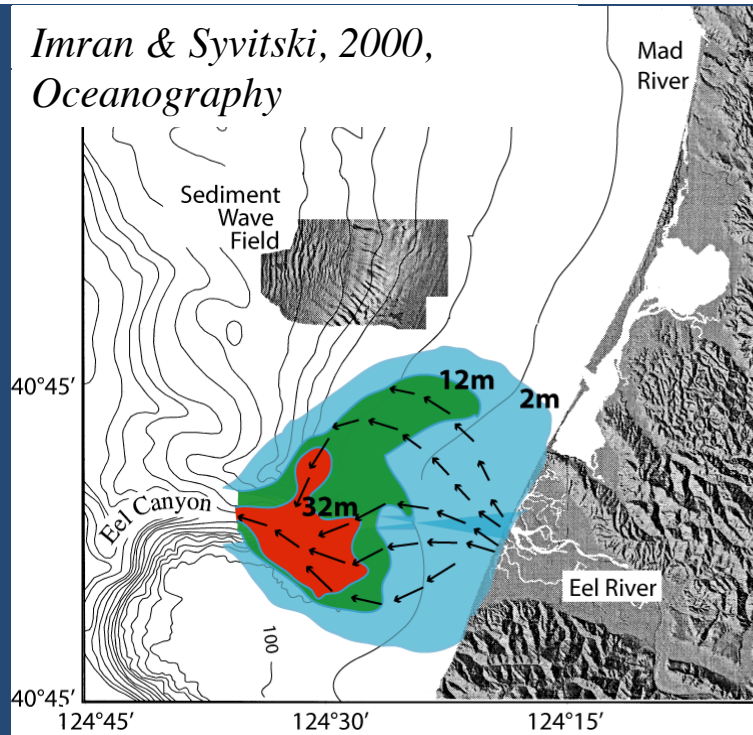
STM model nesting



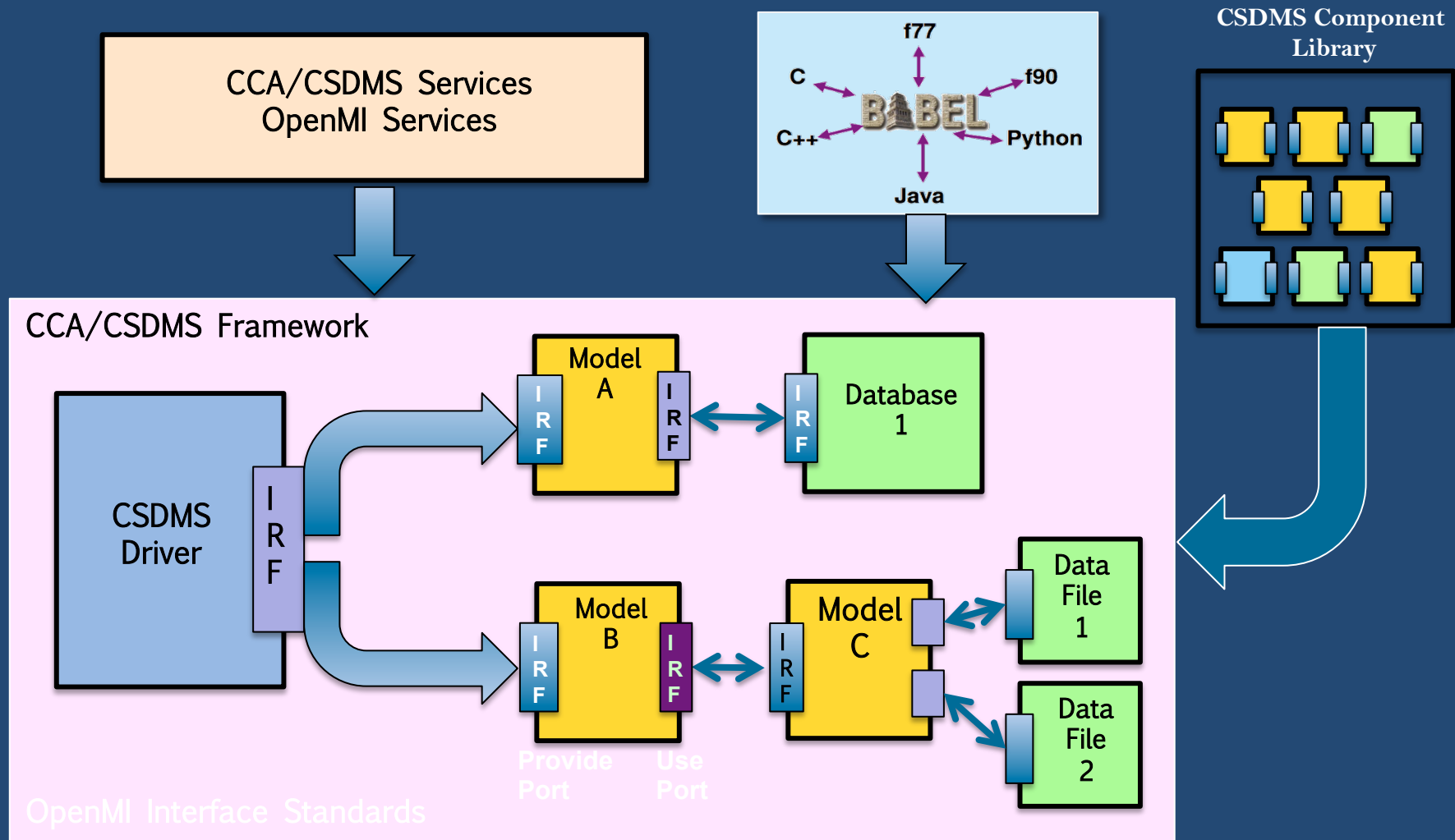
Application of multiple model nesting, including HydroTrend, ROMS, SWAN, COAMPS, NOGAPS, CSTMS. Duration 1 year

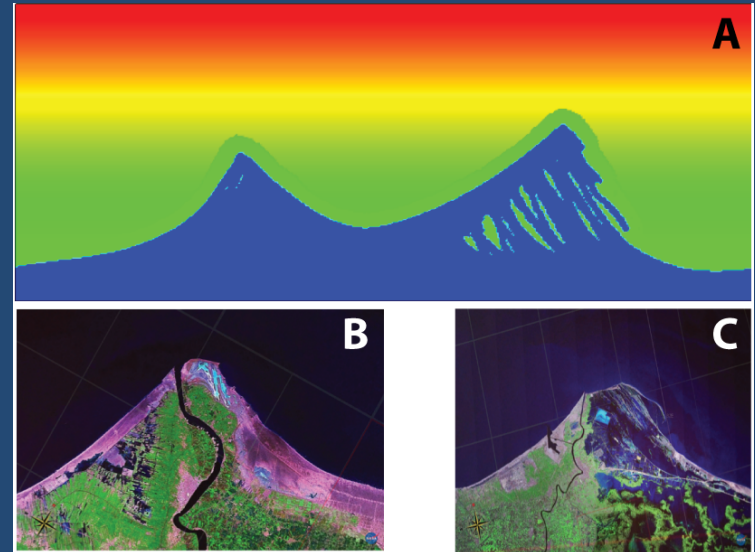
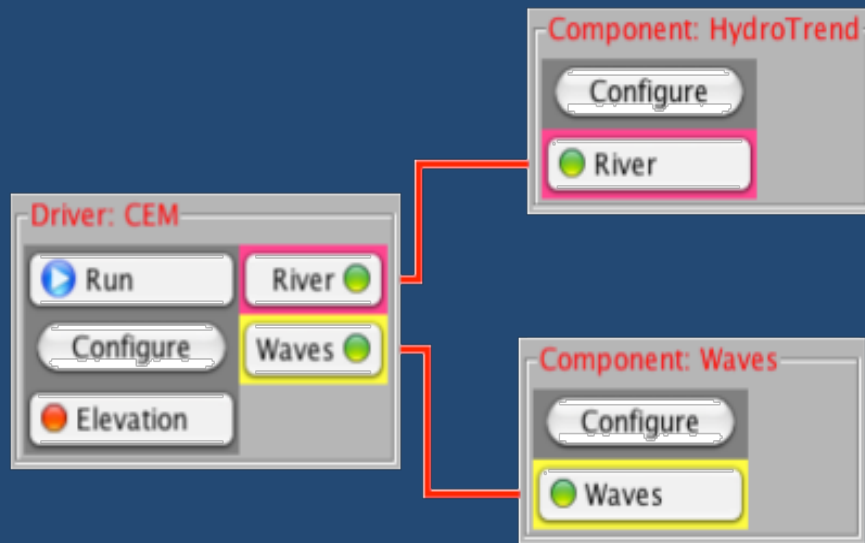
C. Sherwood & R Signell

Imran & Syvitski, 2000,
Oceanography



The CSDMS Modeling Tool, CMT, allows S2S components to be linked to similar open-source components, with due consideration of appropriate time & space resolution and process requirements.





CSDMS CMT S2S Coupling

- 1) LEM/SEM: CHILD + SedFlux
- 2) STM + MDM: HydroTrend + CEM + Waves
- 3) STM: GC2D + TopoFlow; HydroTrend + ROMS;
WBM + BQART/PSI
- 4) STM + SEM: HydroTrend + SedFlux

CSDMS models mostly used in stand alone mode, ie >8000 downloads
 49 of 164 CSDMS models are now CMT components
 S2S coupled examples are being developed annually

Summary of S2S Modeling

- Complete S2S modeling has a distance to go
- LEM/SEM coupling has great potential with CHILD to SedFlux being the first 'type' example, but many components are missing
- MDM model coupling is in its infancy and the next decade will see examples limited to couplings of 2 or 3 environments
- STM model coupling also has great potential as global earth-system modeling develops. These models however will never offer stratigraphy or geomorphology. Geodynamics will be missing, but the models offer important linkages to geochemistry, and ecosystem dynamics

