

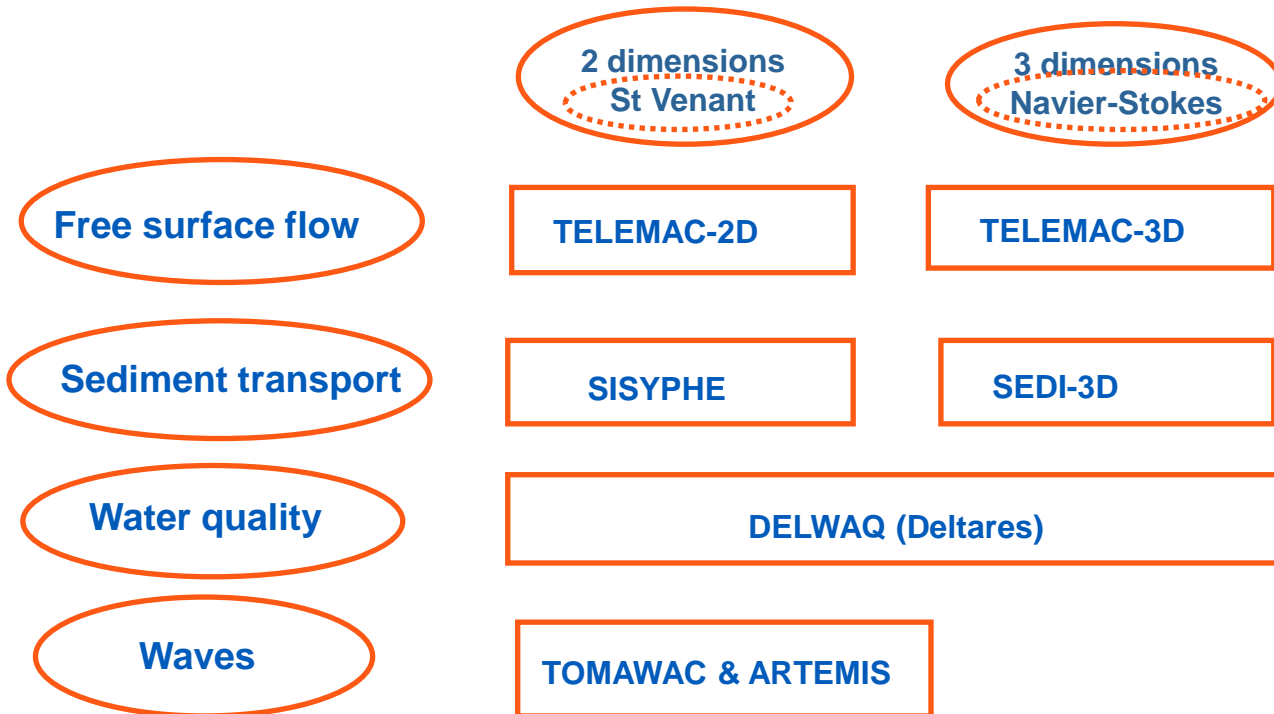
The Telemac system

From small scale processes...

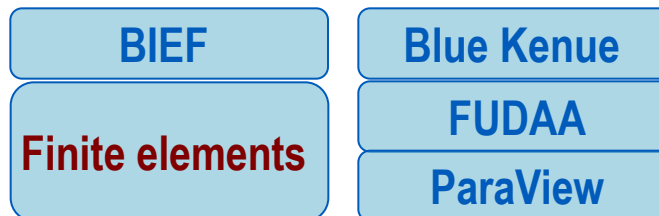
.... to large scale applications



User club (October 2011): 130 participants
2000 users in more than 100 Countries



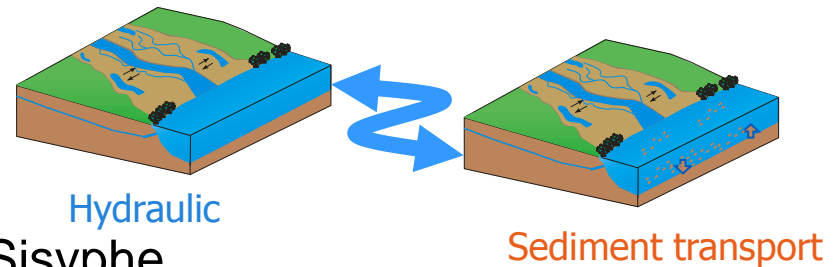
Libraries, pre- and post-processors



Multi-scale, multi-physics

► Coupling of models

- Chaining
- Internal coupling
 - Telemac-2D or Telemac-3D/Sisyphe
 - Telemac-2D/Tomawac



■ Platform (Open MI)

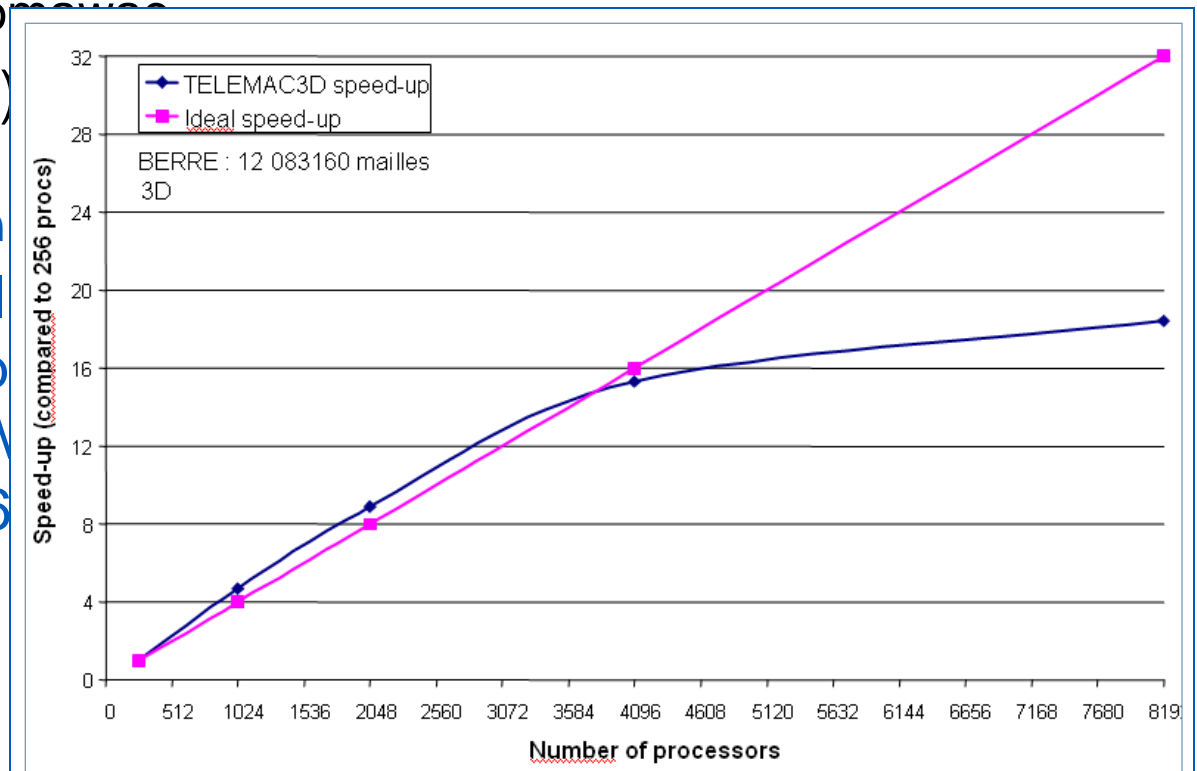
Parallelism with domain

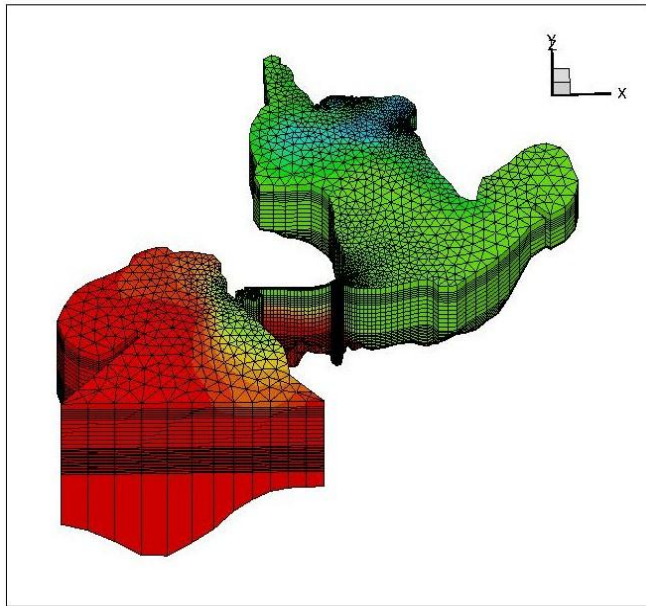
All options parallel

With one million p

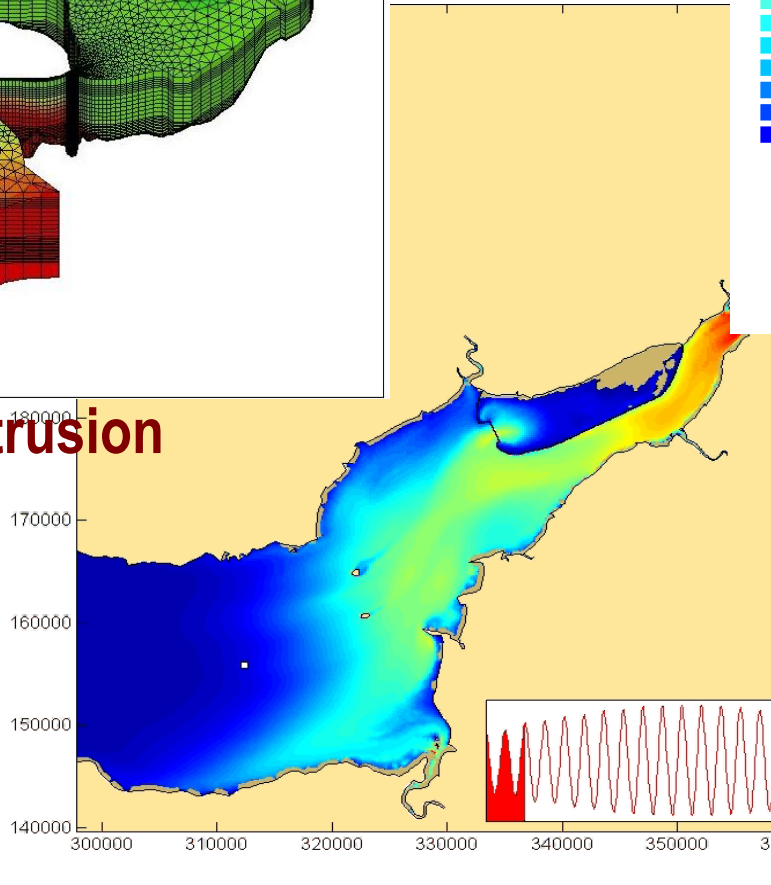
processors, on IBM

Tested up to 8096

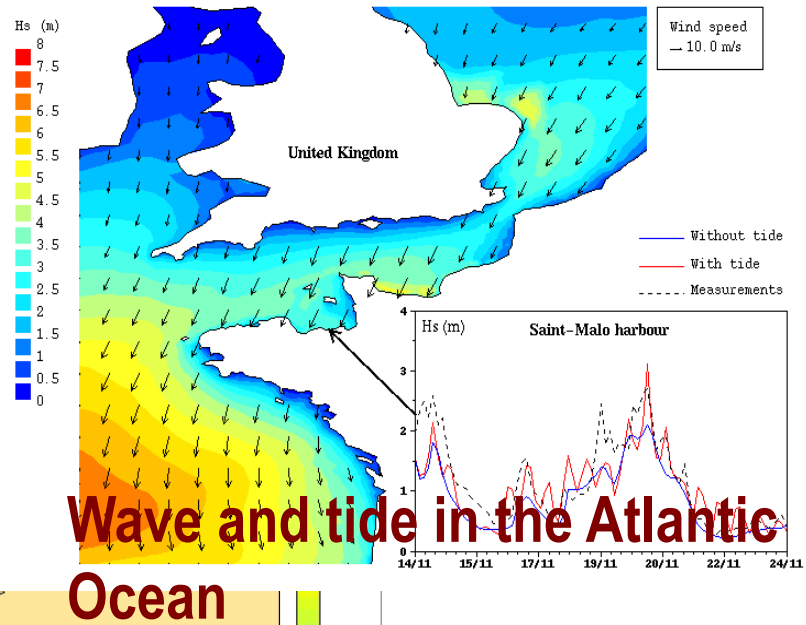




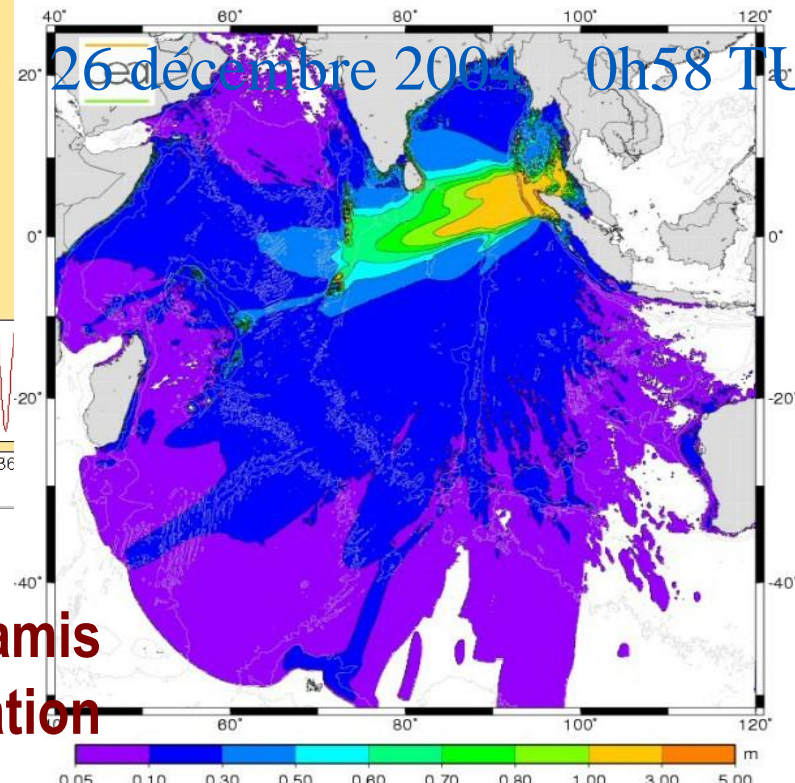
Salinity intrusion



Sediment in estuaries



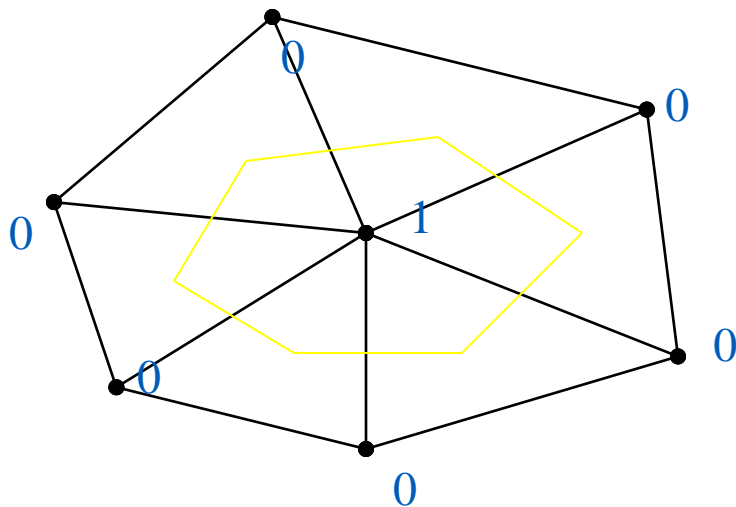
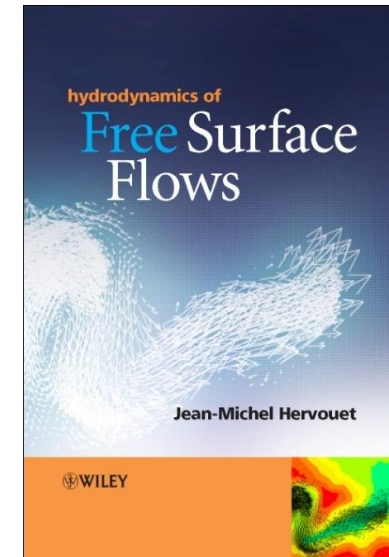
Wave and tide in the Atlantic Ocean



Tsunamis propagation

Bief Library

- ▶ Unstructured grids
- ▶ FORTRAN 90, PERL, MPI
- ▶ Finite elements / Finite volumes
- ▶ Implicit schemes
- ▶ Fundamental operation on matrix, vectors, scalars



- Definition of basis function:

$$\sum_{j=1}^n \Psi_j = 1$$

- Decomposition of each variable:

$$f = \sum_{j=1}^n f_j \Psi_j$$

- Variational principles:

$$f = 0 \Leftrightarrow MF = 0$$

- Mass matrix:

$$M_{ij} = \iint_{\Omega} \Psi_i \Psi_j d\Omega$$



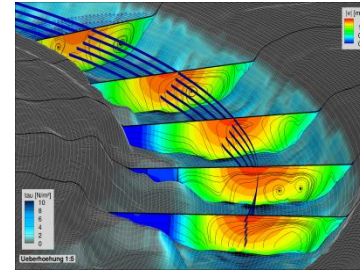
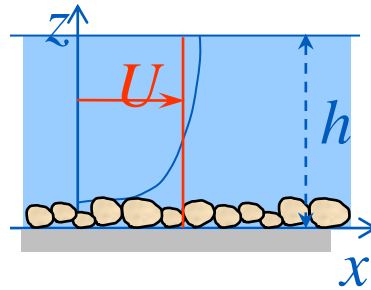
Riad Ata

Telemac-2D / Telemac-3D



Chi-Tuàn Pham

$$(U, V) = \frac{1}{h} \int (u, v) dz$$



$$\mathbf{U} = (u, v, w)$$

- $h \ll L$
- Hydrostatic pressure
- Non recirculating, well mixed

- Turbulent flow
- Hydrostatic
- non-hydrostatic pressure

Equations

Shallow water (St venant)

RANS

$$\frac{\partial h}{\partial t} + \nabla h \bar{\mathbf{U}} = 0$$

$$\nabla \mathbf{U} = 0$$

$$\frac{\partial \bar{\mathbf{U}}}{\partial t} + \bar{\mathbf{U}} \cdot \nabla \bar{\mathbf{U}} = -g \nabla Z_s + \frac{1}{h} \nabla (h \mathbf{D}) - \frac{\boldsymbol{\tau}_b}{\rho h} + \frac{\boldsymbol{\tau}_s}{\rho h}$$

$$\frac{\partial \mathbf{U}}{\partial t} + \mathbf{U} \cdot \nabla \mathbf{U} = \vec{g} + \nabla p + \nabla((\nu + \nu_t) \nabla \mathbf{U})$$

Bottom friction

- Quadratic friction law

$$\boldsymbol{\tau}_b = \frac{1}{2} \rho C_D \bar{\mathbf{U}}^2$$

- Logarithmic velocity profile (first plan)

- Logarithmic velocity profile

$$\frac{\bar{U}}{u_*} = \frac{1}{\kappa} \text{Log} \left(\frac{11h}{k_s} \right)$$

$$\boldsymbol{\tau} = \rho u_*'^2 = \rho \left[\frac{\kappa}{\log 30(\Delta / k_s)} \right] (u^2 + v^2)$$

Telemac-2D / Telemac-3D

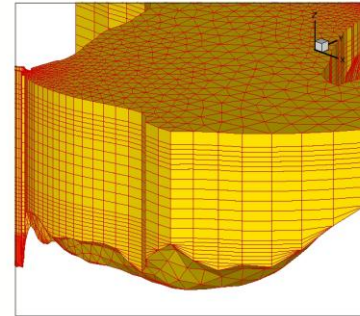
▶ Other Important features

- Cartesian or spherical coordinates
- Courant numbers up to 10

▶ Robust and efficient

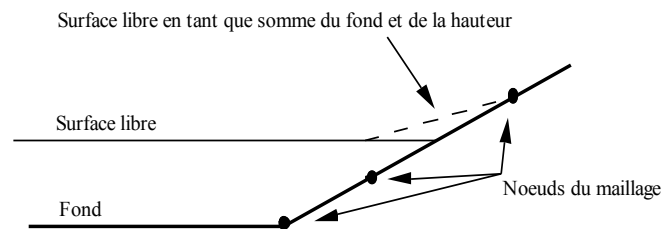
▶ Sensitivity of model results

- Turbulence model (k- ϵ , mixing length)
- Vertical grid resolution

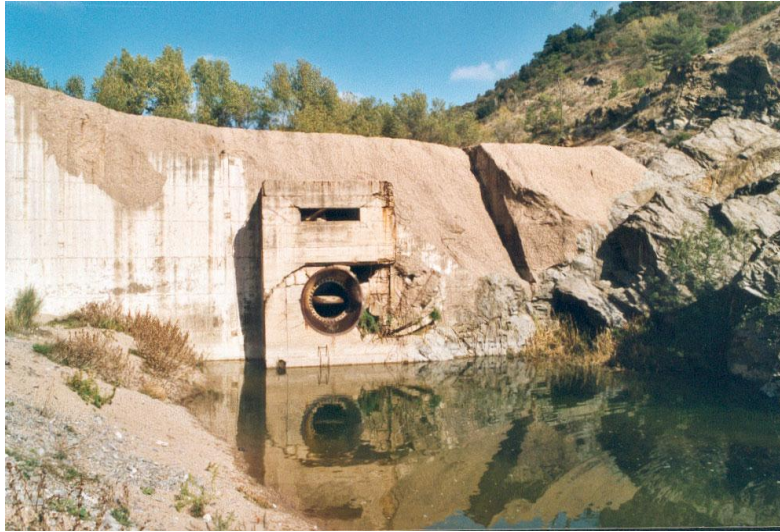


▶ Treatment of dry zones

- No element removal, all points treated even if dry
- Continuity, positivity of depth, conservation and monotonicity of tracers ensured by an edge-based treatment of fluxes (*Hervouet et al., AIRH congres, 2011*)



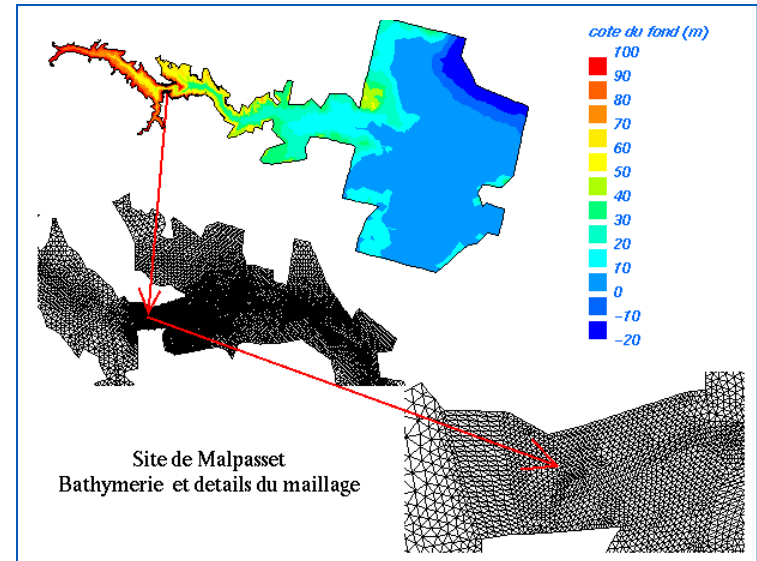
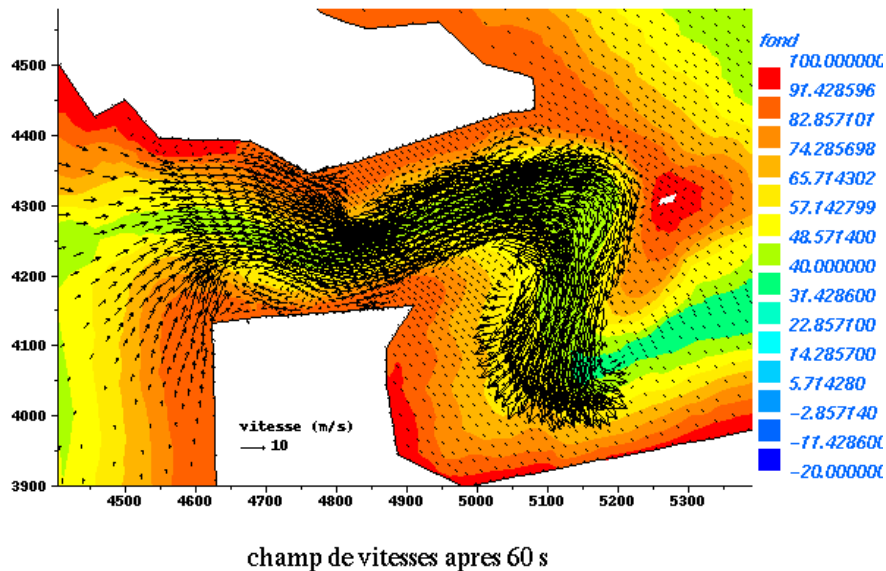
Malpasset dam break



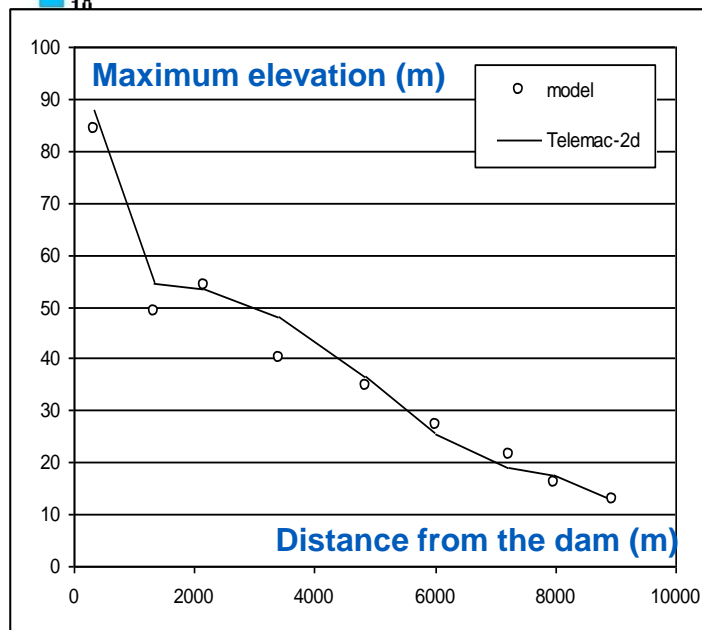
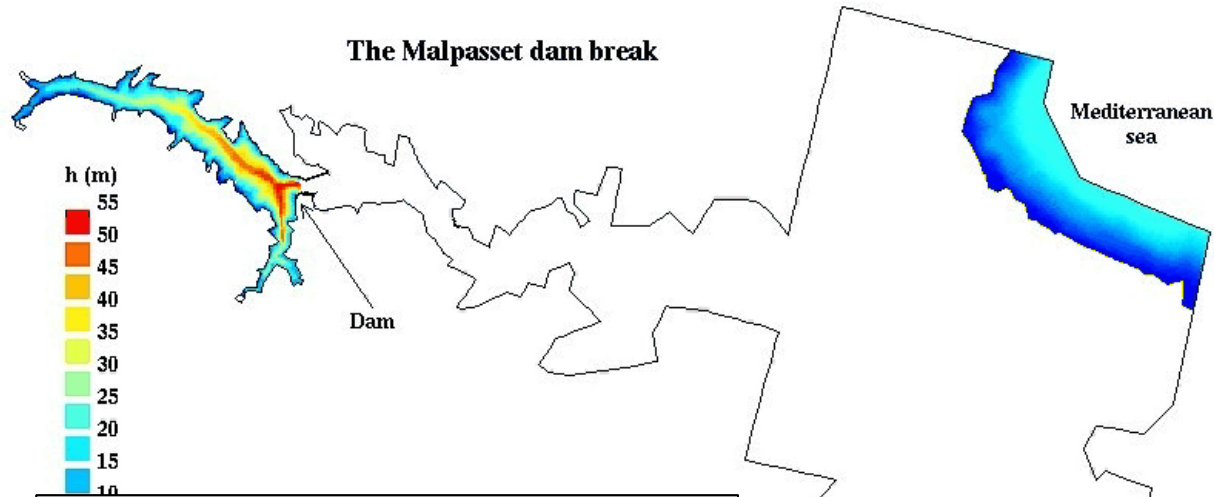
Malpasset dam, 48 million m³, broke on 2 December 1959, there were 433 casualties.

Mesh

- 26 000 elements
- DT=4s
- 100 DT



Malpasset dam break



Linux	Telemac-2D	Telemac-3D
HP Z600		(2 planes)
1 proc.	52 s	188 s
8 proc.	11 s	36 s

Tomawac



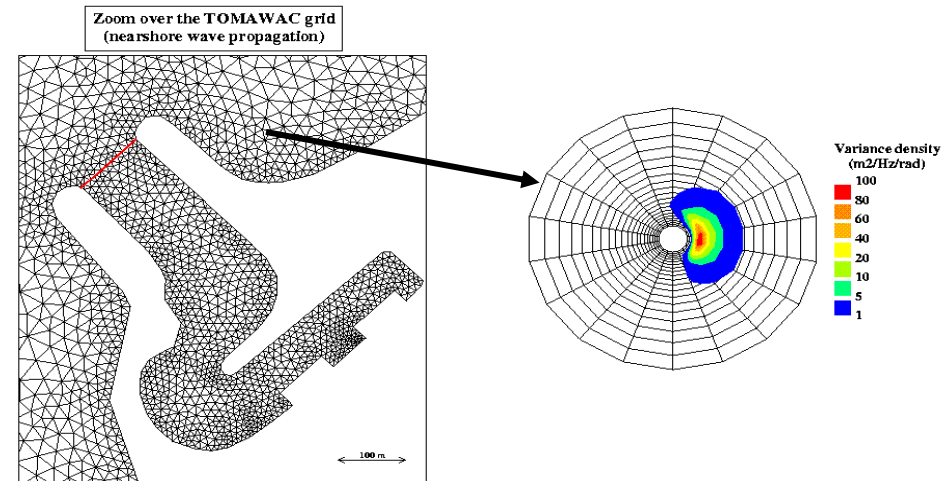
Giovanni Mattarolo

▶ Third generation spectral wave model

- F: variance density directional spectrum

▶ Conservation of the wave action:

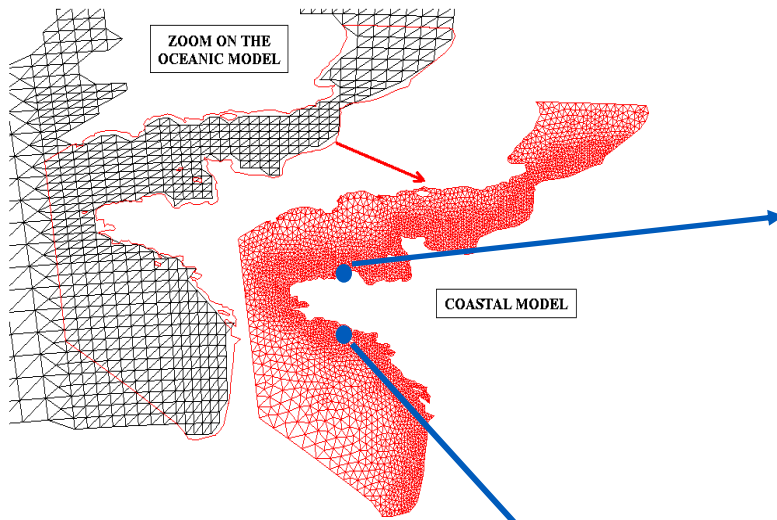
- Shoaling
- Refraction
- Non-linear interactions
- Wind generation
- Wave dissipation (breaking, white capping)



▶ Wave-current interaction (Telemac-2d/Tomawac)

▶ Applications: oceanic to coastal zones

Waves in the Atlantic Ocean



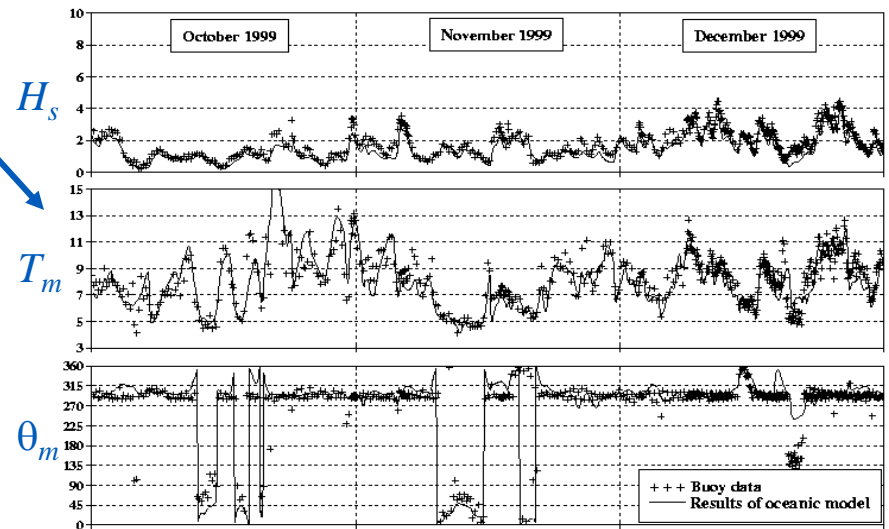
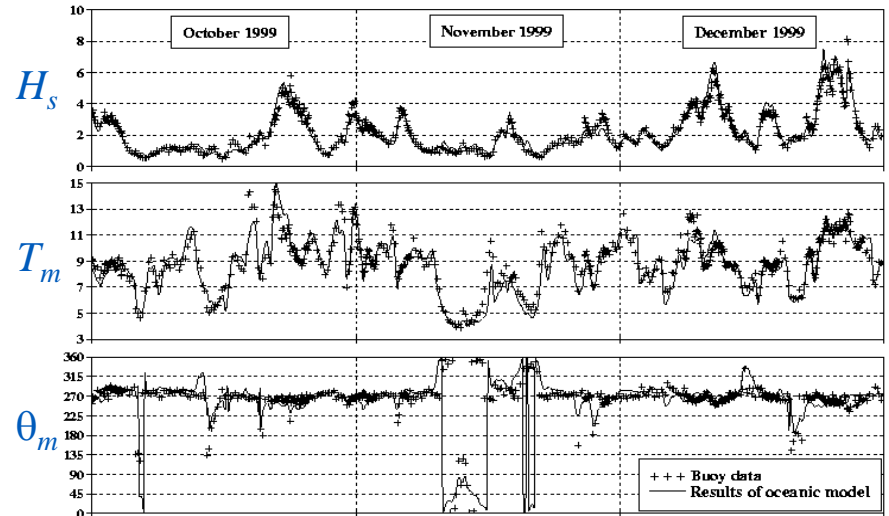
Oceanic wave model

- 25 500 elements
- DT=600s
- 1 year computation

Processors	CPU time (s)
1	90 000
8	18 000
16	6 500
20	5 500
24	6 000

Dec 1999

++ Observé
--- Simulé





Sisyphe / Sedi 3d



Pablo Tassi

Catherine Villaret

► Bed load

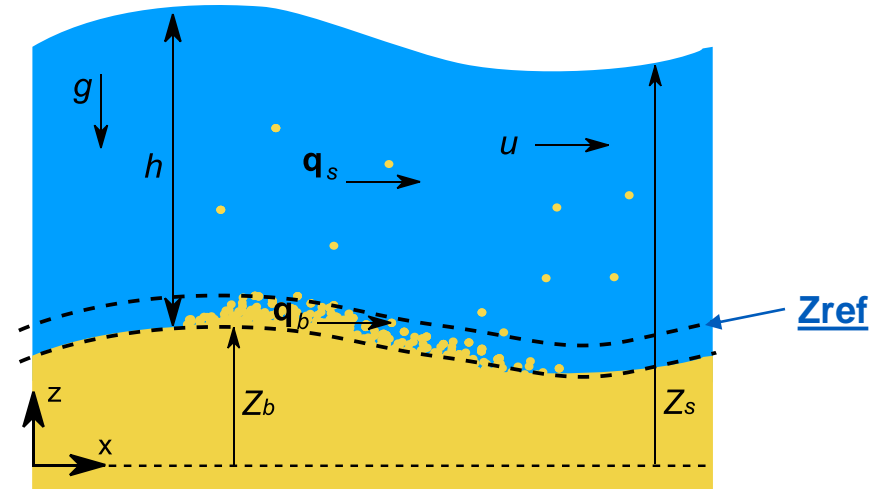
→ Total load /bed load formula

→ Exner equation

$$(1-n) \frac{\partial Z_b}{\partial t} + \text{div} \vec{Q}_s = 0$$

• 2D suspended load

$$\frac{\partial \bar{C}}{\partial t} + \vec{\nabla}(\bar{C}\bar{U}) - \frac{1}{h} \nabla(K_t \vec{\nabla} \bar{C}) = \frac{E-D}{h}$$



3D suspended load

$$\frac{\partial C}{\partial t} + \vec{u} \cdot \vec{\text{grad}}(C) + \underbrace{\frac{\partial(W_s C)}{\partial z}}_{\text{Settling}} = \underbrace{\text{div}(\gamma_t \vec{\text{grad}}(C))}_{\text{Turbulent diffusion}}$$

$$(1-n) \frac{\partial Z_b}{\partial t} + (E-D) = 0$$

↓ Erosion rate

→ Deposition rate

Non cohesive

$$D_{50} > 60 \mu\text{m}$$

- Erosion-deposition rates
- Equilibrium concentration formula

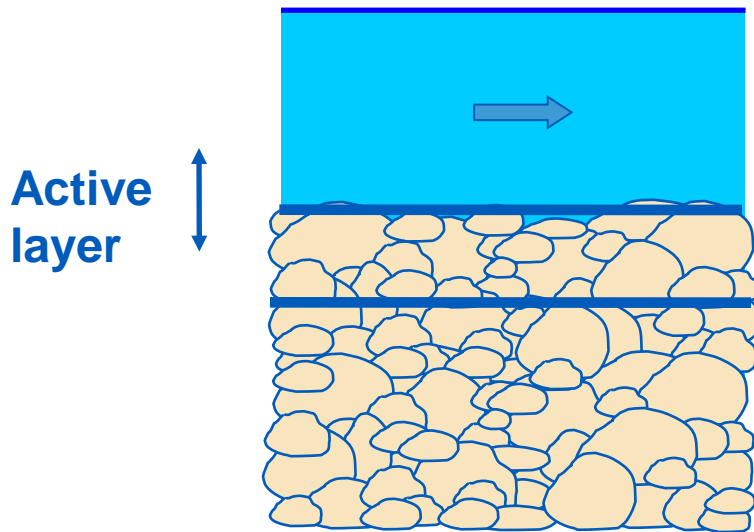
$$E = W_s C_{eq}$$

(e.g. Van Rijn, 1984)

- Deposition rate (implicit):

$$D = W_s C_{zref}$$

- Sand grading effects



Cohesive

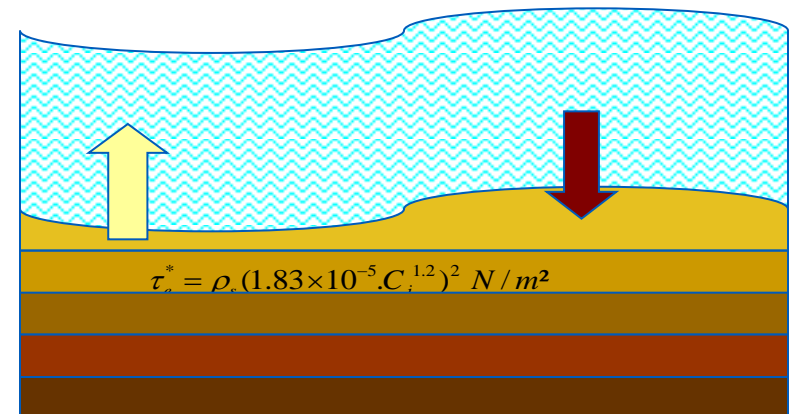
$$D_{50} < 60 \mu\text{m}$$



- Erosion-deposition laws (Krone and Partheniades)

$$E = M \left[\left(\frac{\tau_0}{\tau_e} \right)^2 - 1 \right]$$
$$D = W_s C \left[1 - \left(\frac{\tau_0}{\tau_d} \right)^2 \right]$$

- Consolidation model



Sisyphé / Sedi-3D

2D suspended load

Correction on the convection

(Huybrechts, Villaret, and Tassi, River Flow 2010)

$$\overline{CU} = \alpha \overline{C} \overline{U} < \overline{C} \overline{U}$$

Assuming:

- Log velocity profile
- Rouse concentration profile

$$\alpha = h \frac{\int_a^h U(z) C(z) dz}{\int_a^h U(z) dz \int_a^h C(z) dz} \leq 1$$

3D suspended load

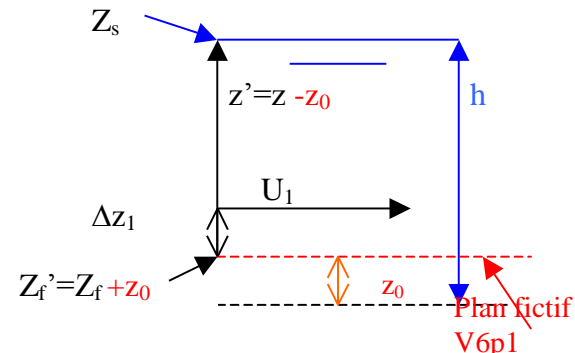
Treatment of boundary condition

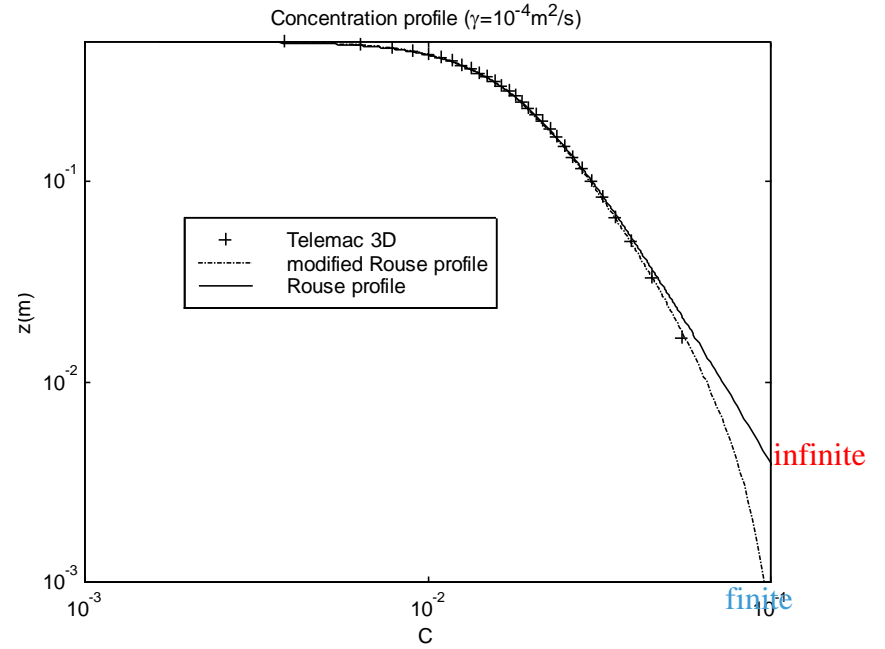
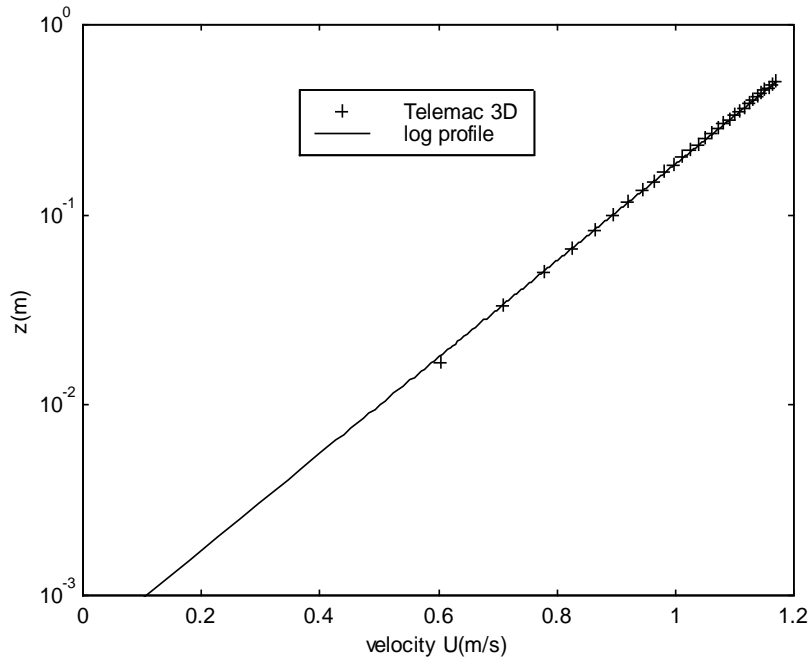
$$E = \left(v_t \frac{\partial C}{\partial z} \right)_{z_b}$$

0 inf

Sensitivity of model results to

- turbulence model (k-ε, ...)
- Vertical grid resolution





Finite values \longrightarrow

$$C = C_{h/2} \left[\frac{h - z}{z + \frac{\gamma}{\kappa u_*}} \right]^{\frac{-W_c}{\kappa u_*}}$$

γ : laminar diffusivity

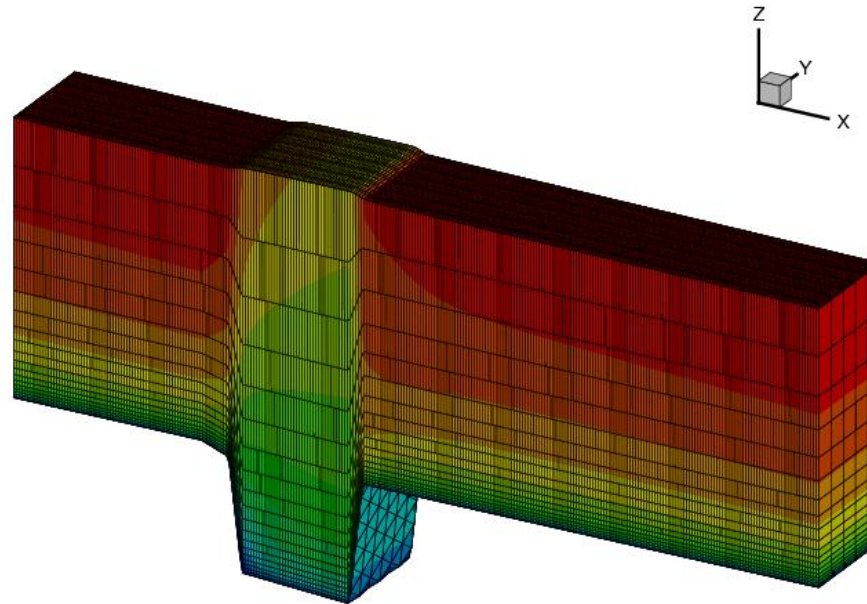
Trench evolution in 2D/3D

van Rijn (1987)

$h = 0.39 \text{ m}$

$U = 0.51 \text{ m/s}$

$d_{50} = 0.16 \text{ mm}$



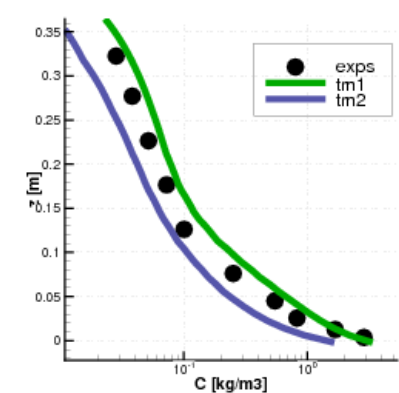
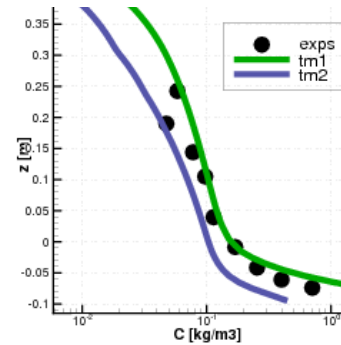
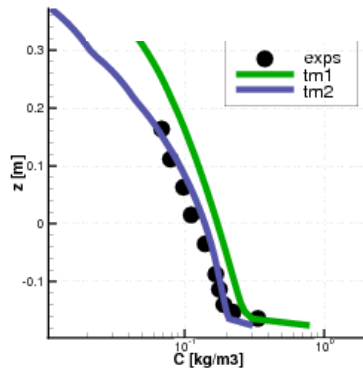
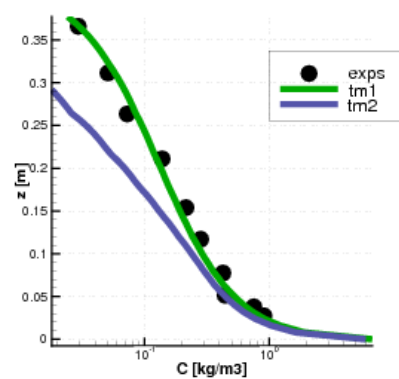
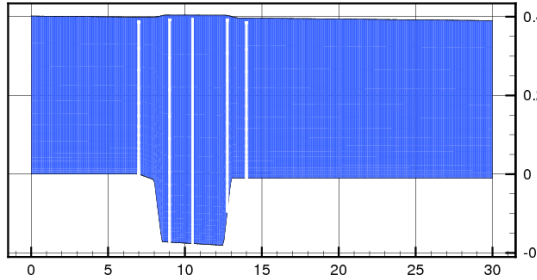
3D model

16 planes

non-hydrostatic

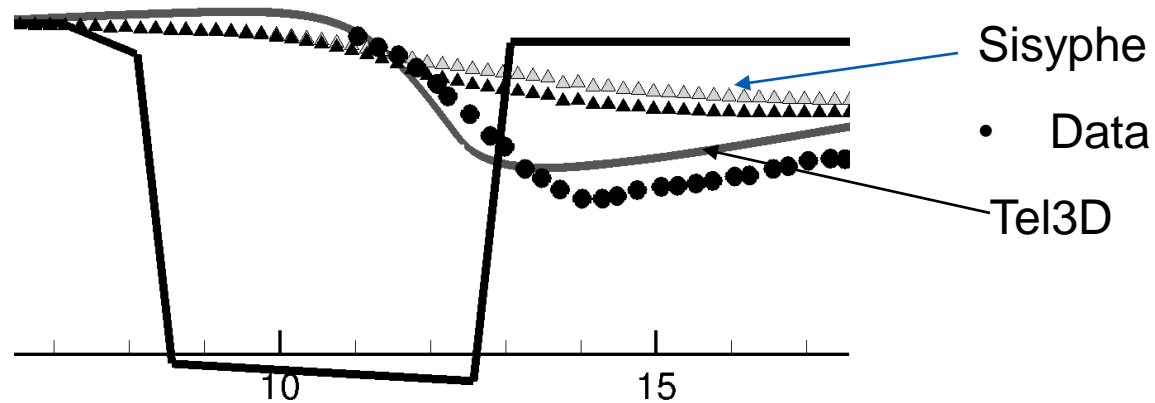
pressure

P1 P2 P3 P4 P5



concentration profiles (tm1= $k-\epsilon$; tm2=mixing length)

Trench evolution in 2D/3D



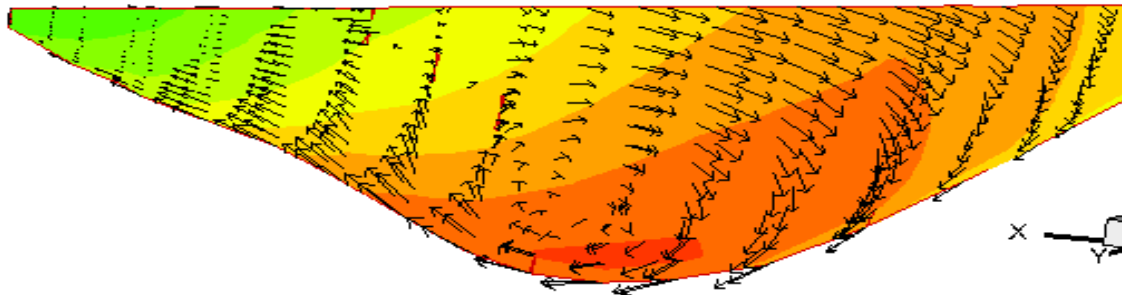
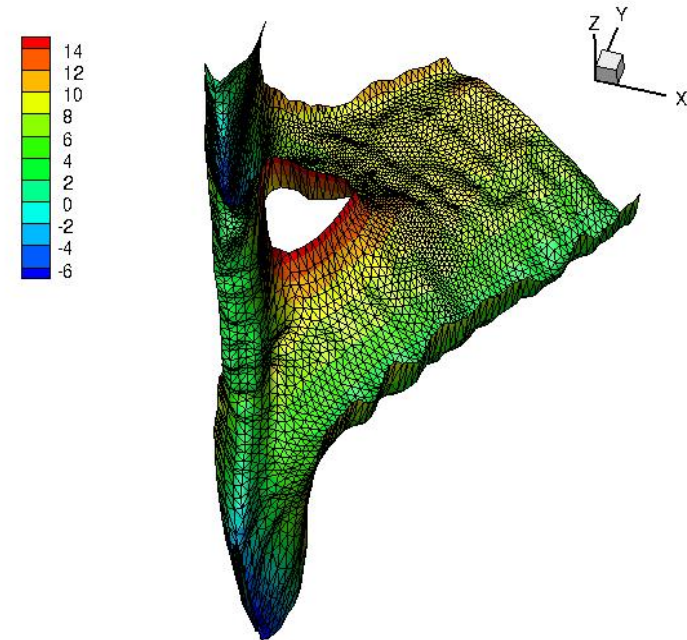
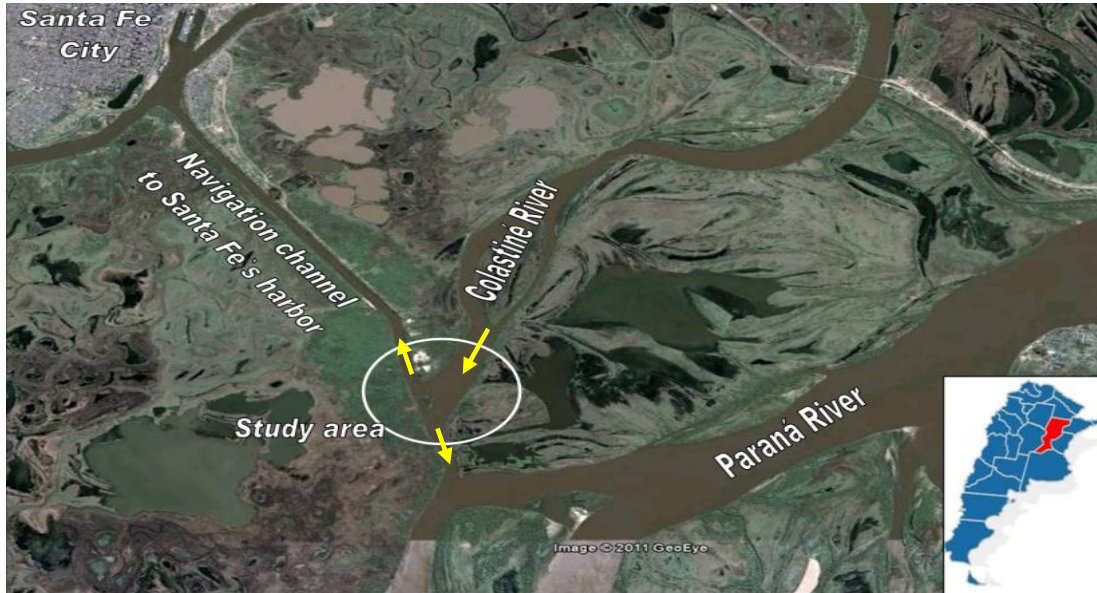
Bed evolution after $t=15$ hs

- ▶ 2D model overestimates transport rates
- ▶ Convection velocity correction
 - Improves the results
 - 2D model : good compromise between model accuracy and computational time for non-recirculating flow

Secondary flow pattern in river



Telemac-3d : flow patterns at a river diffluence
(Tassi, Vionnet and Morell, 2011)



- 6,623 elements x 15 layers
- time step = 0.1 s
- steady state 100,000 time steps

Computed velocities along XS-3

Meandering channels

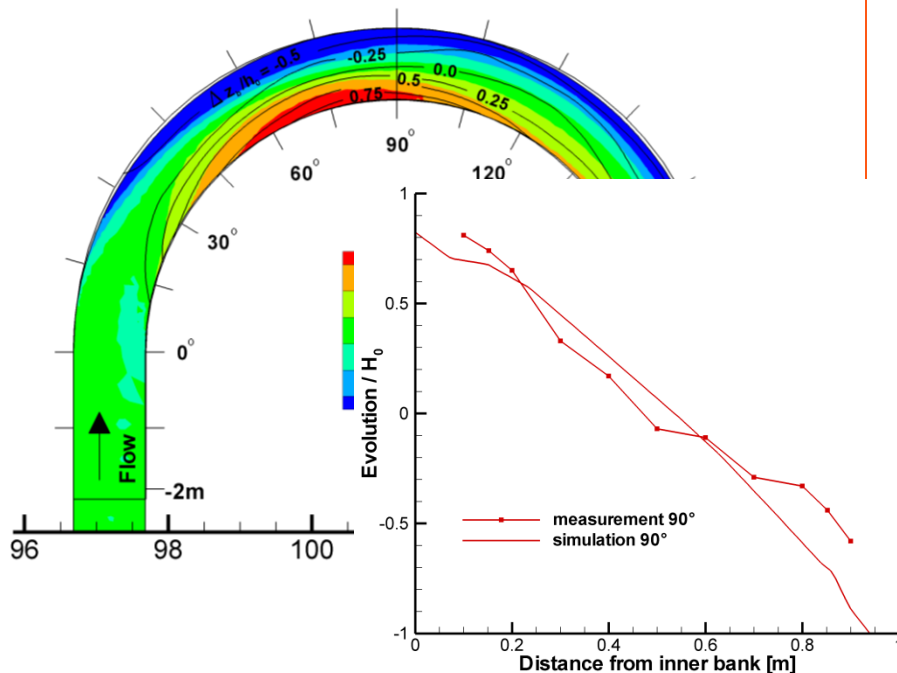


Telemac 2D/Sisyphe

→ Secondary current parameterization in 2D

Yen's experiments (1995)

- bedload only

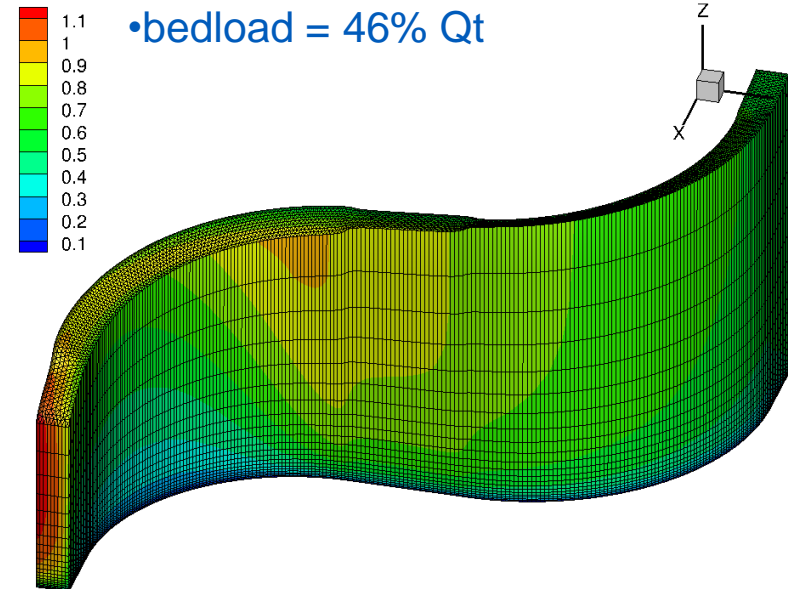


Telemac 3D/Sisyphe

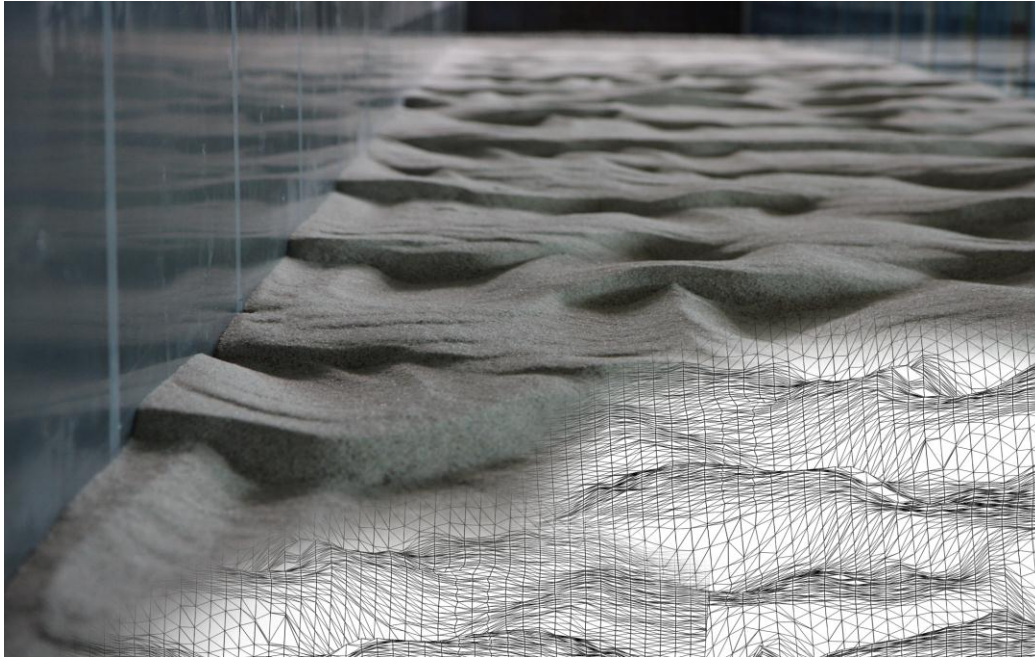
→ Turbulence model

Onishi's experiments (1972, 1976)

- suspension = 54% Q_t
- bedload = 46% Q_t

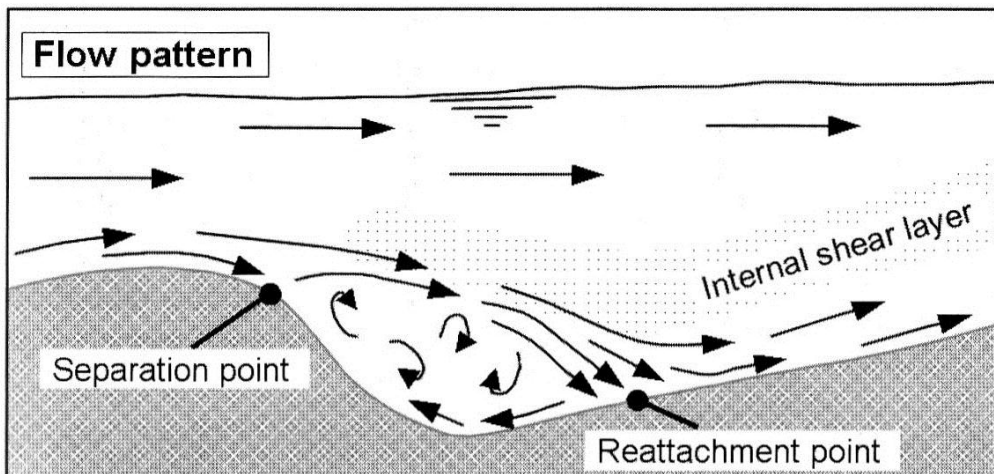
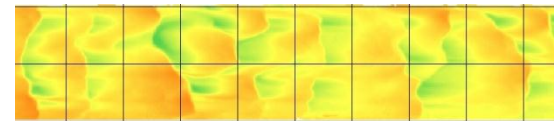


Numerical simulation of bedforms



Flume experiments

- Length: 30m
- Width: 5m (2x2m)
- Discharges: 77-240 l/s
- Bed-load: sand ($D_{50} \approx 1\text{mm}$)



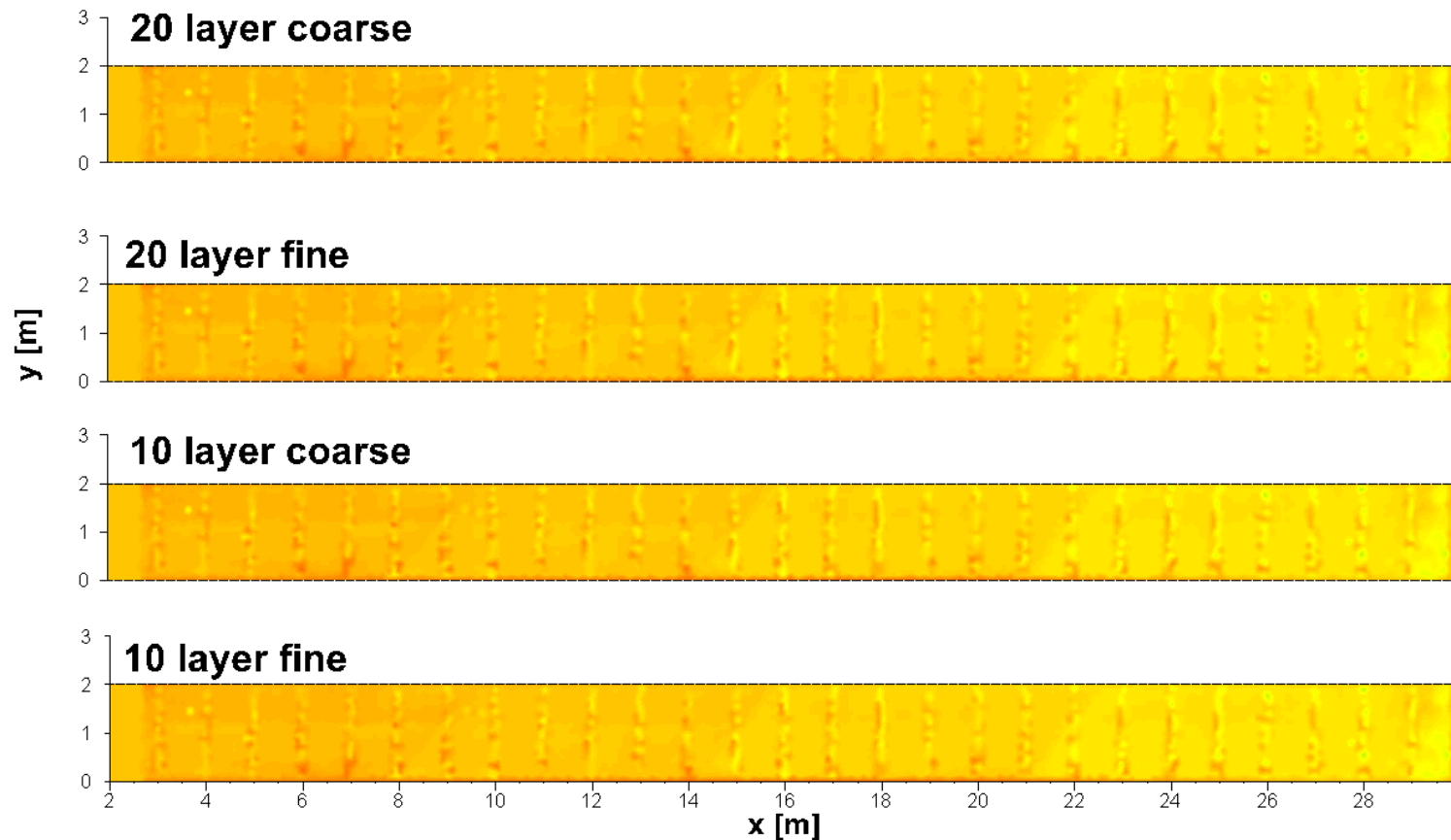
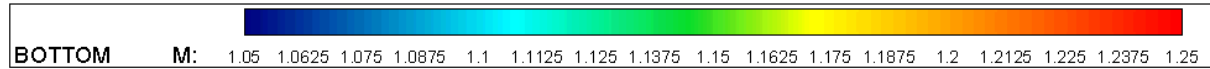
Numerical modelling with Telemac3D / Sisyphé

Analena Goll, PhD student

Numerical simulation of bedforms



0.00 hours



Analena Goll, PhD student

Method of feedback for the bed roughness



Telemac2D

Compute flow using **total** roughness

Total bed roughness

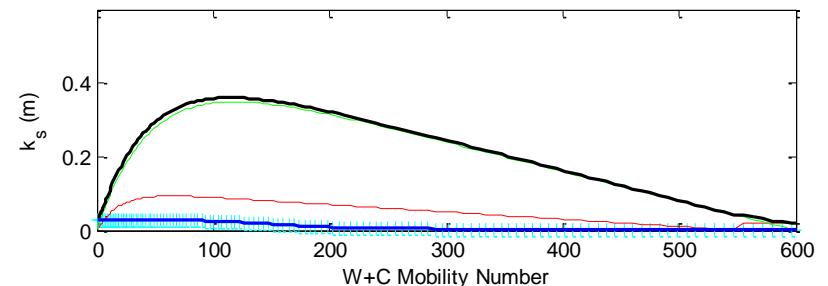
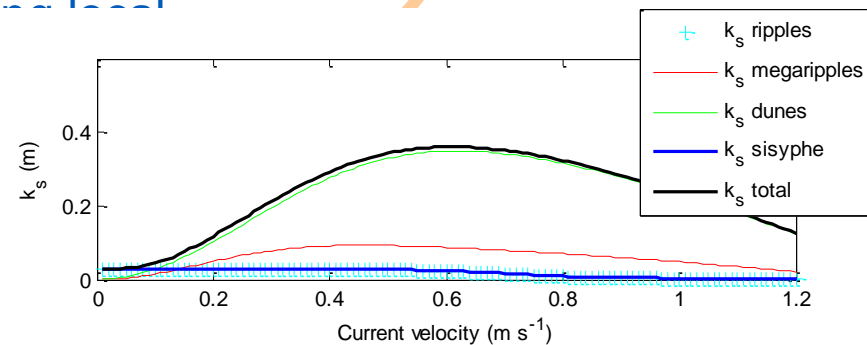
Sisyphé (in ride.f)

Compute the transport using **small-scale** ripple roughness

Flow based on total bed roughness

- **bed roughness predictor (dunes + megaripples + small-scale ripples), variable in time and space (Van Rijn, 2007)**

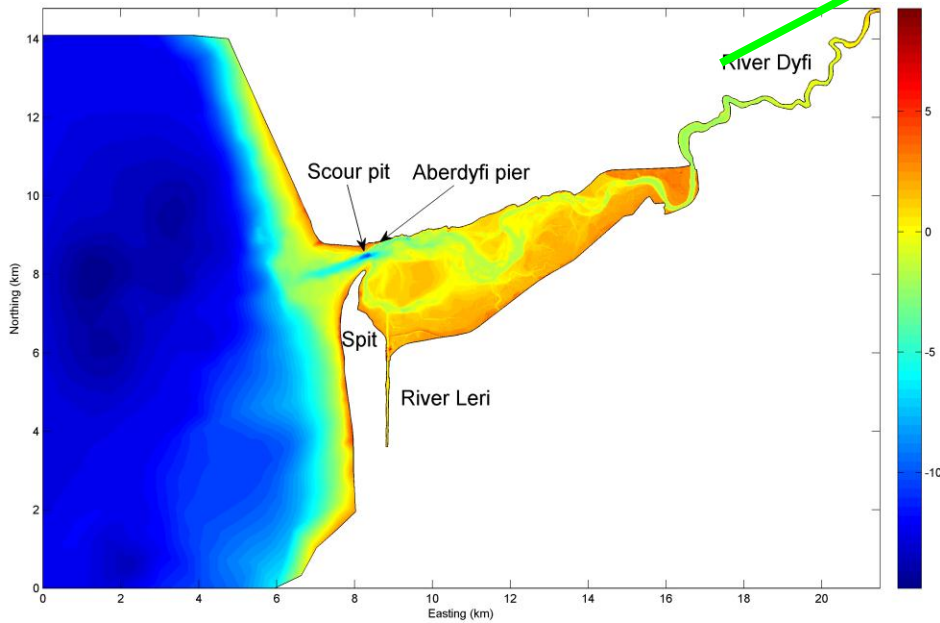
$$k_s = \sqrt{(k_{s,r}^2 + k_{s,m}^2 + k_{s,d}^2)}$$



Large scale morphodynamics

■ Dyfi Estuary (Wales, UK)

- Shallow sandy macro-tidal estuary
- Multiple banks and channels
- Tidal range : 2 to 4.3 m offshore
- Sediment : sand 0.2-0.25mm
- River input : 25 m³/s annual mean
400 m³/s 1 in 100 yr

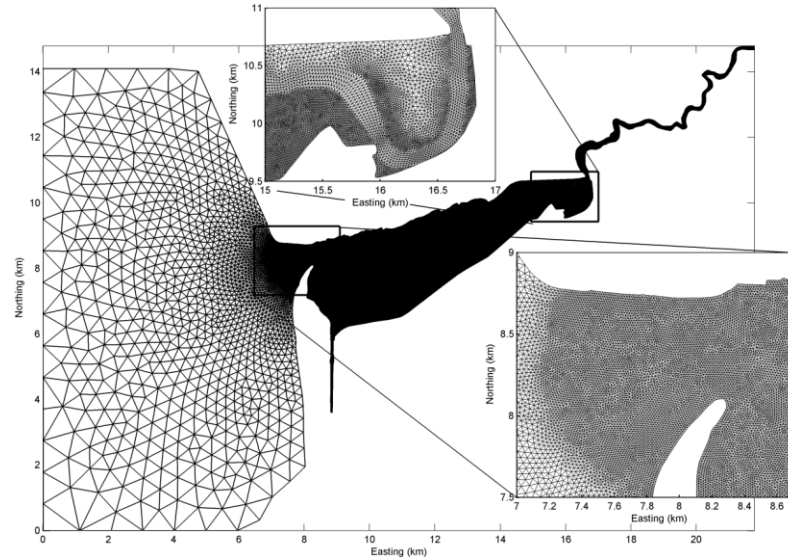


→ **Field validation of the modelled bed roughness (for dunes)**

Dify estuary morphodynamics

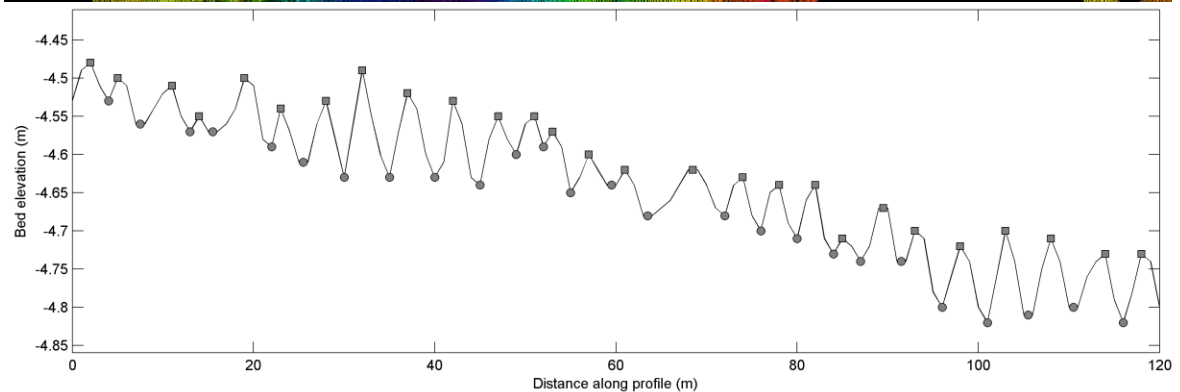
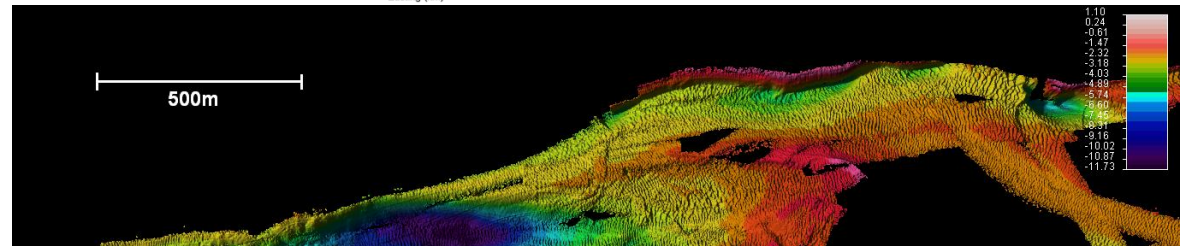
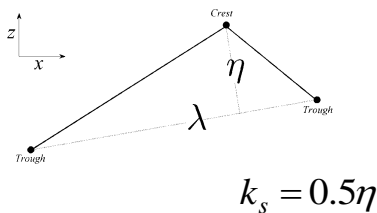
Triangular Mesh

BlueKenue 91,000 nodes,
resolution :1km / 15m

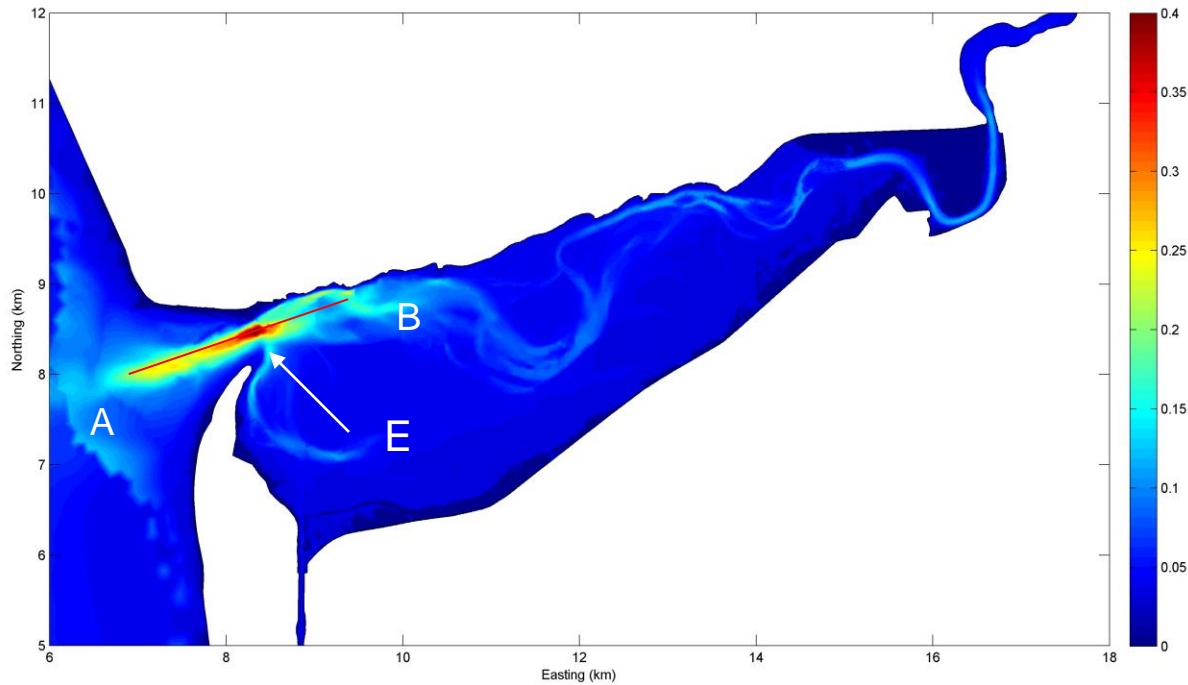


Bathymetry

LiDAR survey (2004) +
Multibeam Multibeam(2007)
→ Bedforms measurements



Dify estuary morphodynamics

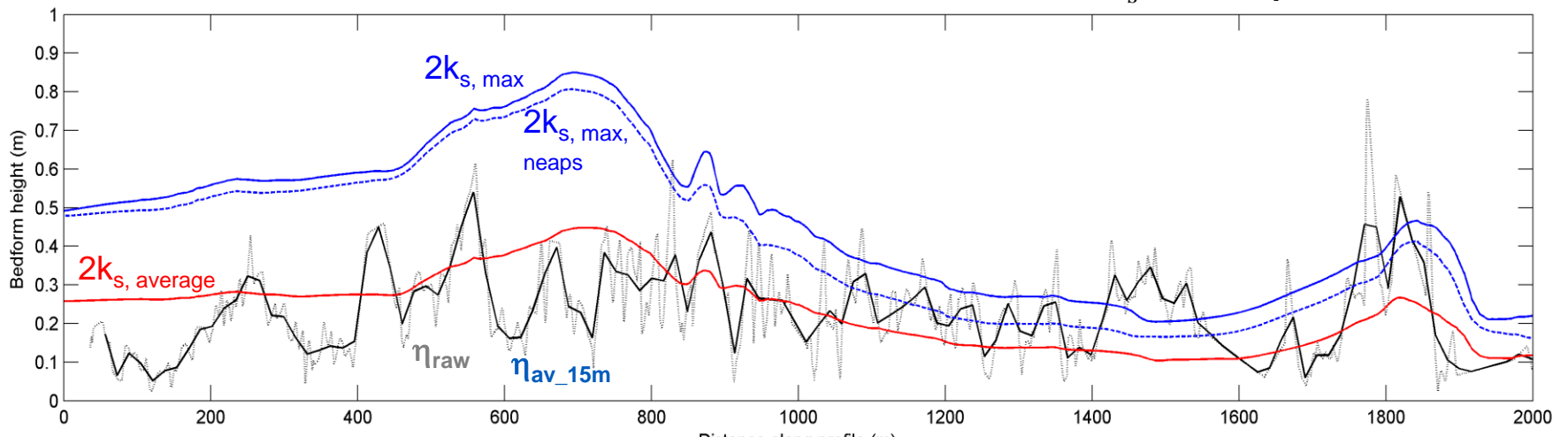


Predicted k_s (m)
(max values during spring tide)
VanRijn method (2007)

- dune roughness in channels
- ripple roughness over tidal flats

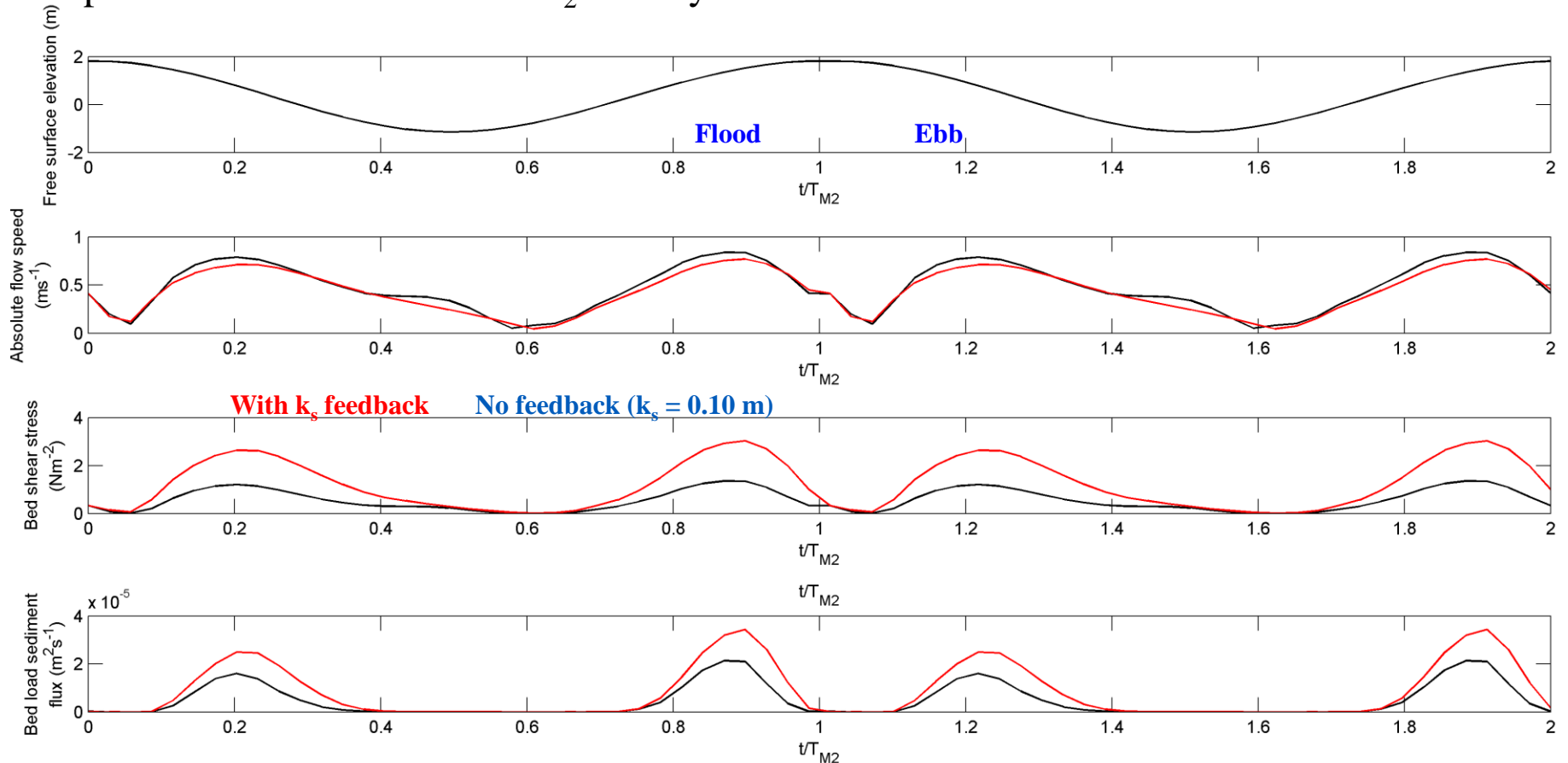
Comparison with measurements along transect AB (m)

$$k_s = 0.5\eta$$



Dify estuary morphodynamics

Comparison at Point E for two M_2 tidal cycles



Effect of feedback method for bed roughness

→ Bottom shear stress increases (by 122%)

→ Total sediment transport rate increases (by 74% on average)

Conclusion

- ◆ Diversity of applications in complex environment:
 - Meandering channels, Macro-tidal estuaries, littoral applications, ...
 - Dune formation to mesoscale morphodynamics (10-100 km)
- ◆ Bed roughness predictor
 - reduces some of the uncertainty in model results
 - avoids possible inconsistency between hydrodynamics and sediment transport
- ◆ More physical processes
 - Sand grading algorithm and mixed sediments
 - Mud consolidation and flocculation

Uncertainty in the sediment transport models >>> hydrodynamics models

→ New validation test cases

→ Uncertainty analysis (automatic differentiation)

Emile Razafindrakoto



Jean-Michel Hervouet