



# SCOR Working Group 122 Mechanism of sediment retention in estuaries

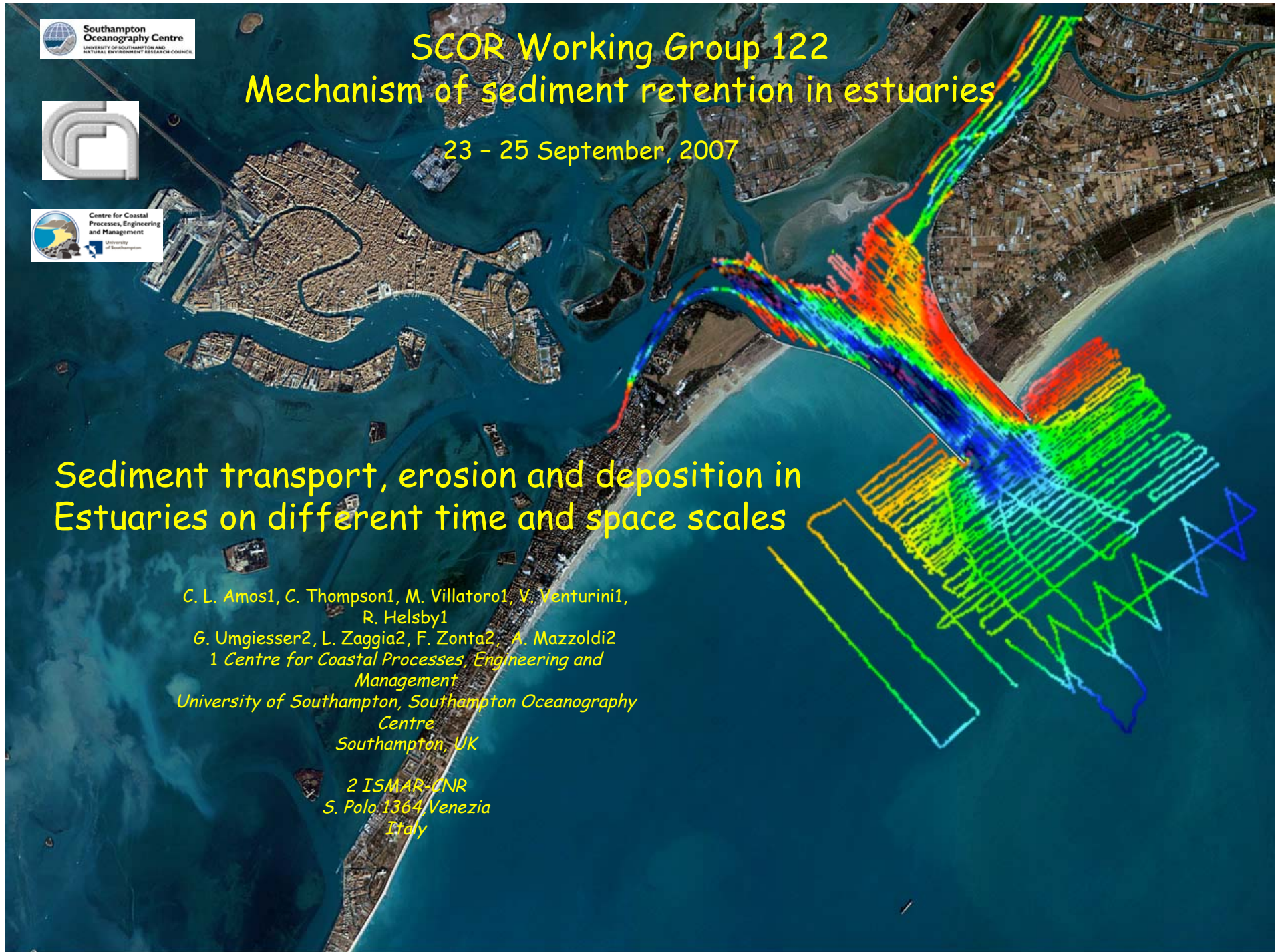
23 - 25 September, 2007



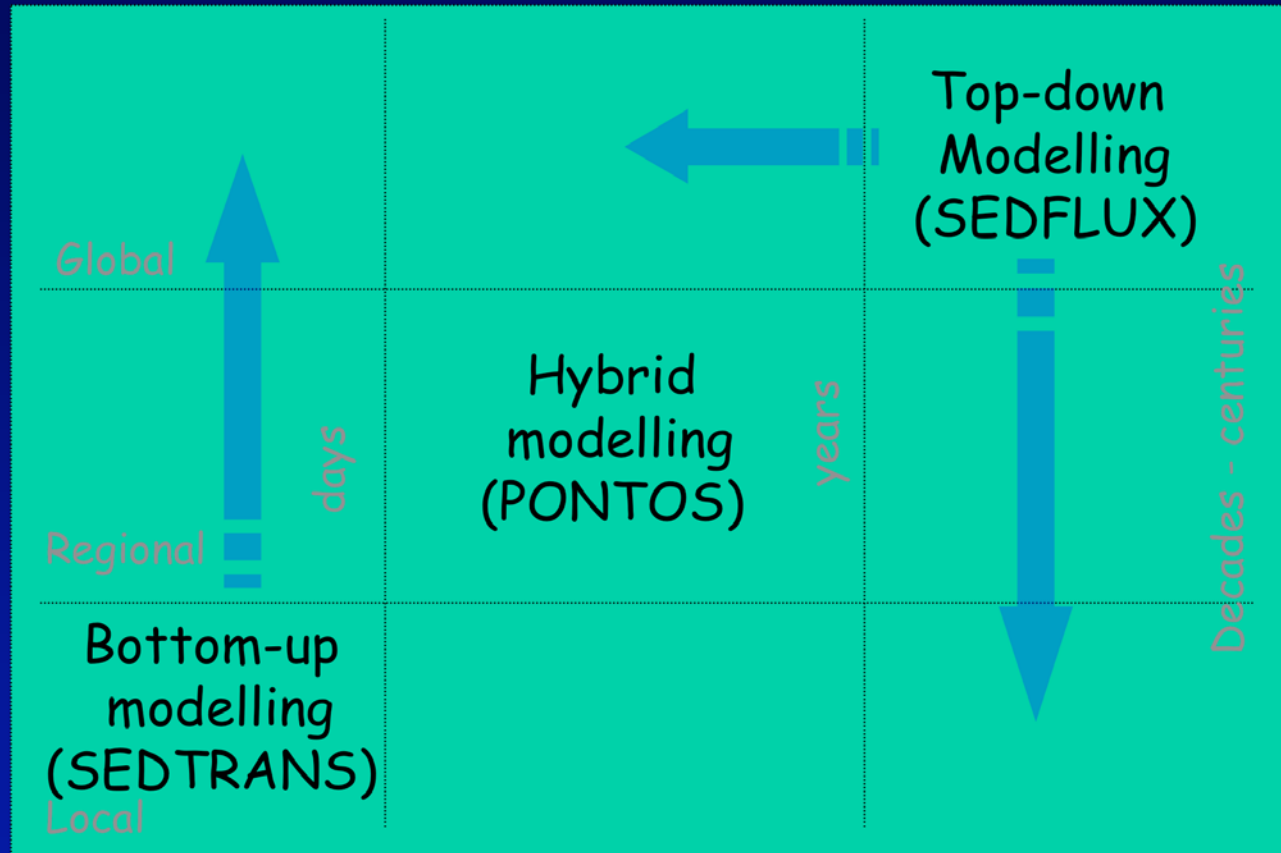
## Sediment transport, erosion and deposition in Estuaries on different time and space scales

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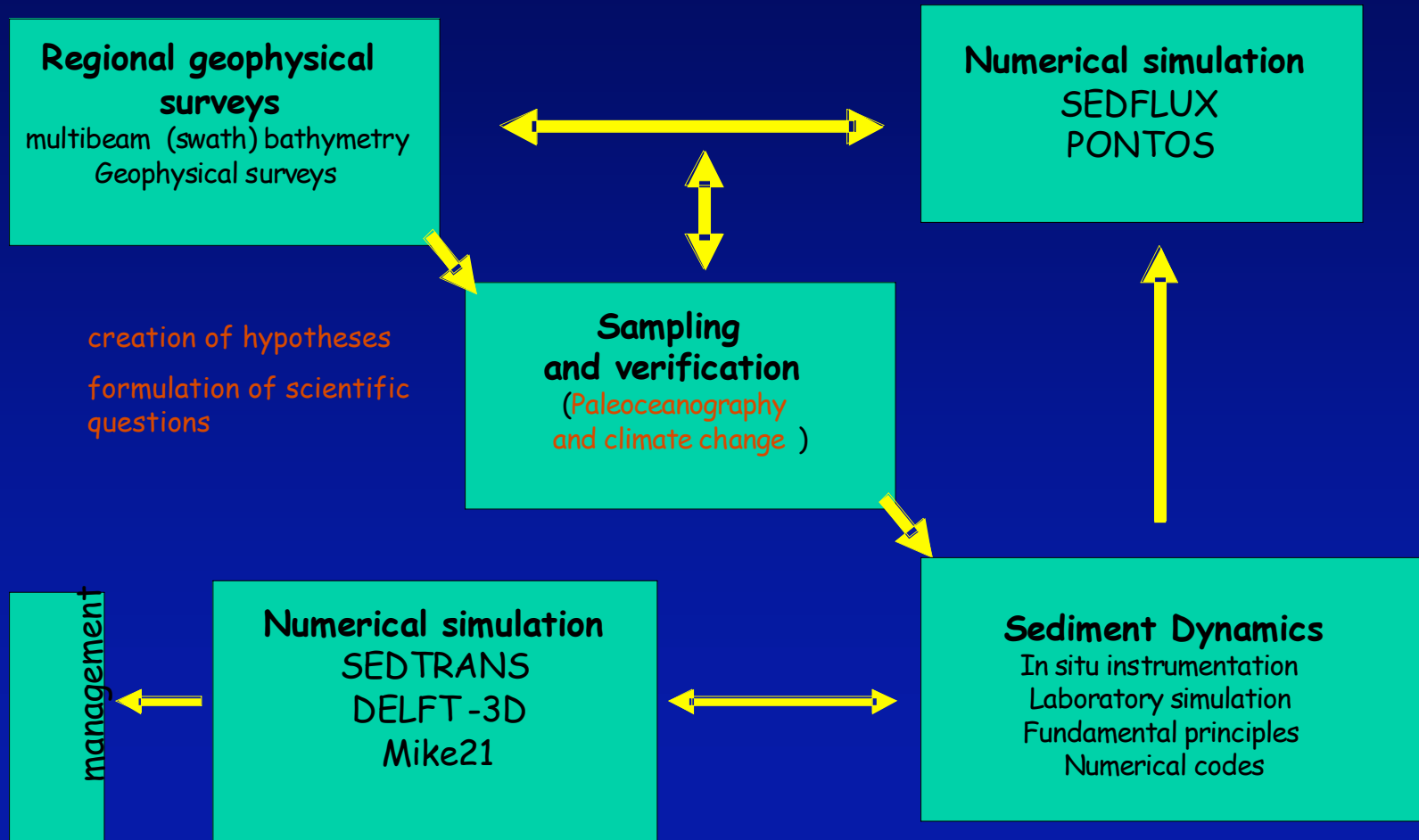


Space scale



Time scale

# Modelling in sediment dynamics



# Bottom-up modelling sediment transport in estuaries

- **Types of models**
  - box models
  - 1-D models (time, distance)
  - 2-D models (x,y, depth-averaged; time versus x-axis)
  - 3-D models (x,y, time; x,y,z)
  - 4-D models (x,y,z, time)
- **Box models - monitor continuity of mass with simple input/output controls**
  - simple and effective in sensitivity analyses, can be time-stepped easily
  - no hydrodynamics, spatially-averaging, poor open boundaries
- **1-D models - spatial gradients in sedimentation, concentration**
  - easily set up, minimum hydrodynamics, offer practical solutions
  - poor open boundary conditions
- **2-D models - provides links between sedimentation and hydrodynamics**
  - valuable insights into fundamental processes, engineering solutions possible
  - labour intensive (99% rule), difficult to calibrate, difficult to programme

## Short term estuarine retention

Best method - direct measurements + numerical/physical simulations + "experience"  
Next best method - direct measurements + numerical simulations + "experience"  
Next best method - direct measurements + "experience"  
Next best method - numerical simulation + "experience"  
Etc, etc.....



"Long term predictions will become within reach when supercomputers are more generally available"

"fundamental problems which remain to be solved are the schematization of the boundary conditions"

"Calibration and verification of mathematical models require a detailed set of synoptic data. Much effort should be put in field surveys to obtain these data." (van Rijn, 1999)

## Fundamental equations

- Sediment continuity equation (3-D):

(Closed system) 
$$\frac{\partial S}{\partial t} + U \frac{\partial S}{\partial x} + V \frac{\partial S}{\partial y} + W \frac{\partial S}{\partial z} + \overline{W}_s S = 0$$

- Mass continuity equation (3-D) (Exner):

(Open to the bed)

$$\gamma_b (1 - e) \frac{\partial z}{\partial t} = \overline{W}_s S$$

$$\overline{W}_s S = D - E$$

- where D is net deposition, E is net erosion, S is suspended sediment concentration, e is sediment porosity,  $\gamma_b$  is sediment unit weight, h is bed elevation,  $W_s$  is mean settling rate, and U, V, W are the three components of mean flow.

## Instrumentation development to calibrate models - suspension

- benthic landers (RALPH)
- benthic flumes (Sea Carousel)
- remote sensing tools (backscatter)
- self-contained packages (Zedhead)

- acoustical
- optical
- electro-magnetic/peizo-electric
- x-ray

time-series, usually from fixed location (1)

Velocity field (3-D) (2)

Mass settling rate (3)

Sediment concentration gradients (3-D) (6)

$$\frac{\partial S}{\partial t} + U \frac{\partial S}{\partial x} + V \frac{\partial S}{\partial y} + (W - W_s) \frac{\partial S}{\partial z}$$

$$\frac{\partial S}{\partial t} + \overline{W}_s S + F_1 + F_n = 0$$

Benthic flux (4)

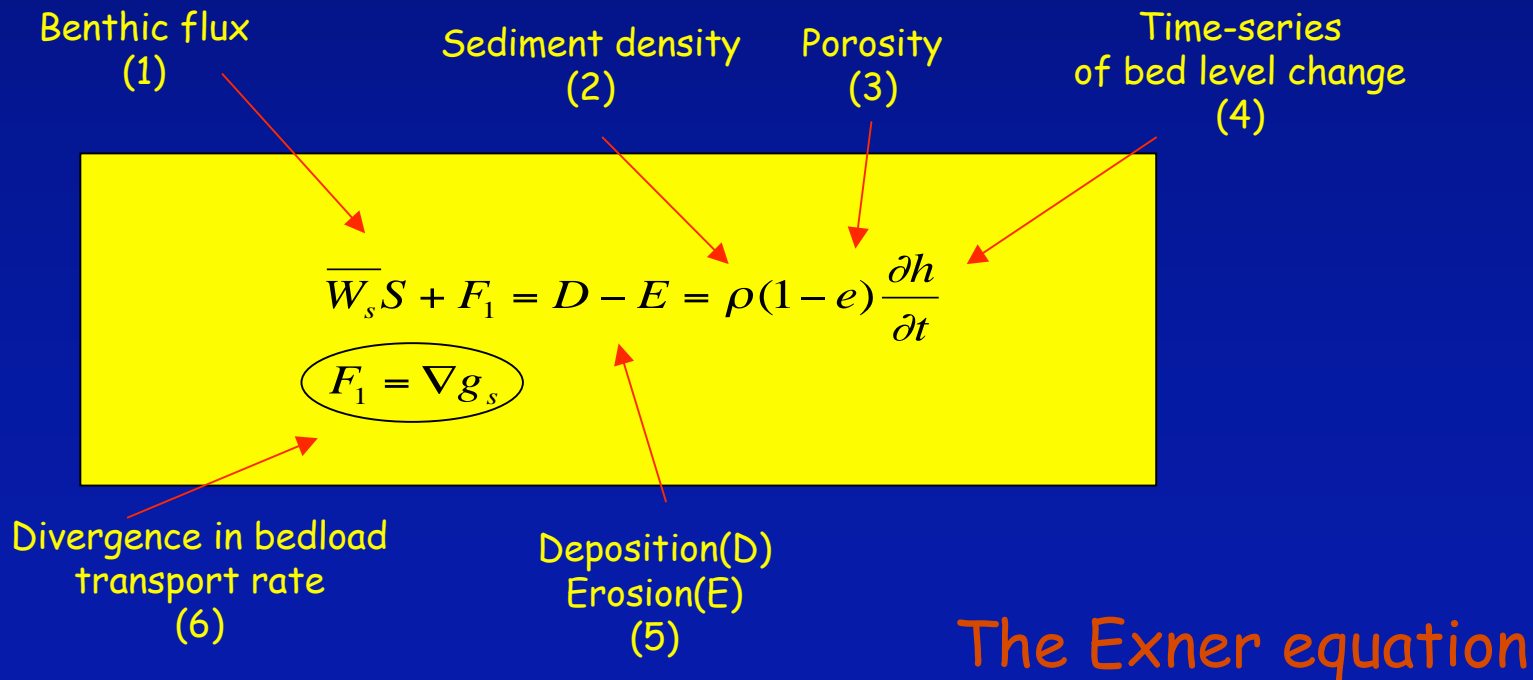
External sources/sinks (5)

The sediment continuity equation = sediment budget

## Morphological-dynamics and sediment dynamics - suspension and bedload

- (1) only possible in closed system !!! (mesocosm)
- (2) bottom sampling
- (3) acoustic velocity, resistivity, CT scanning
- (4) acoustic altimeter, 2-axis sector scanning sonar, repetitive swath bathymetry

- (5i) Deposition (D) from cores (Pb<sub>210</sub> or Cs<sub>137</sub>) or sediment traps or altimeter measures
- (5ii) Erosion (E) (closed systems) or acoustic profiling or long-term swath bathymetry
- (6) Sediment traps, geophysical surveys of bedform migration





## AGE

" The time that has elapsed since the water parcels enters an estuary";  
Bolin and Rodhe (1973).

## TRANSIT TIME

" The period between the times a particle entering and leaving an estuary ";  
Bolin and Rodhe (1973).

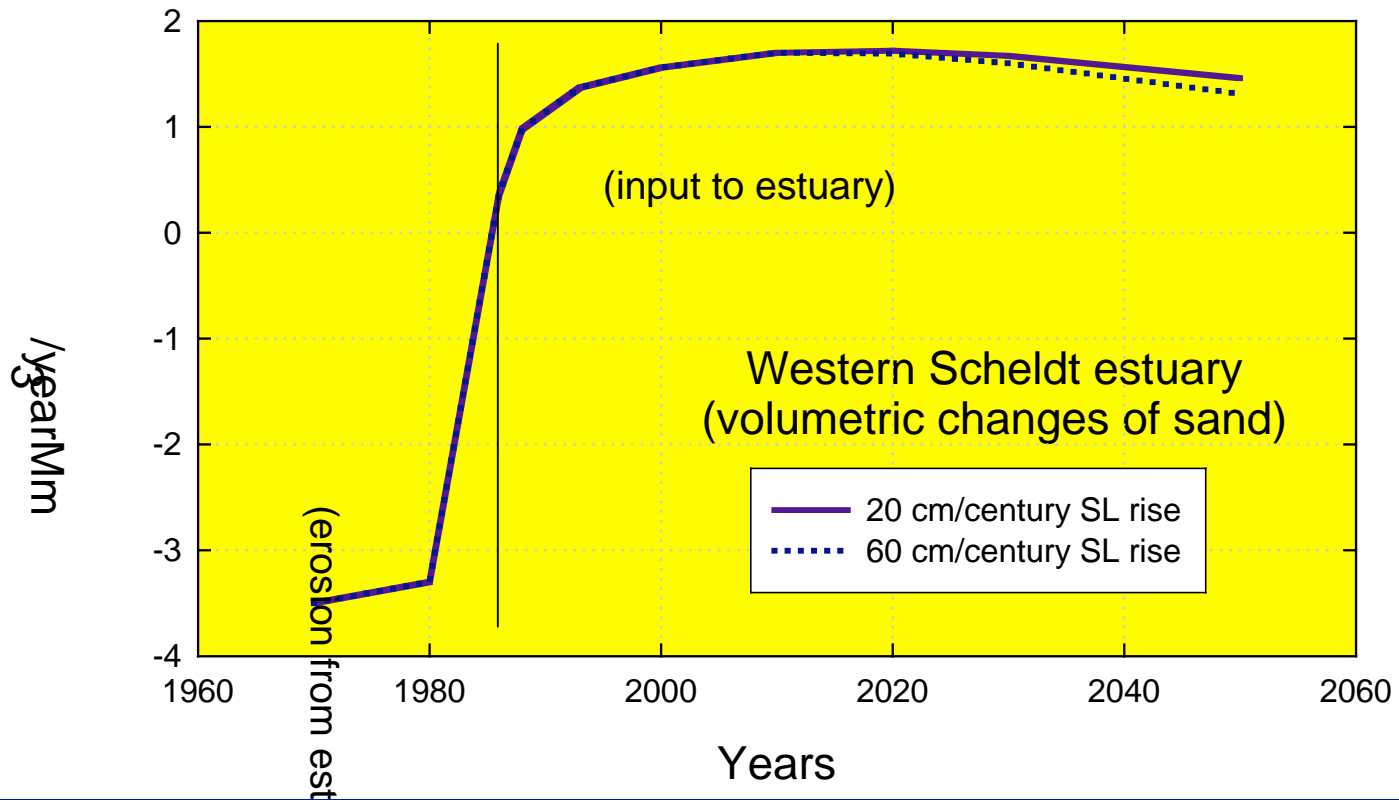
## EXPOSURE TIME

" The total amount of time a particle spends in the domain";  
Monsen et al. (2002).

## RESIDENCE TIME

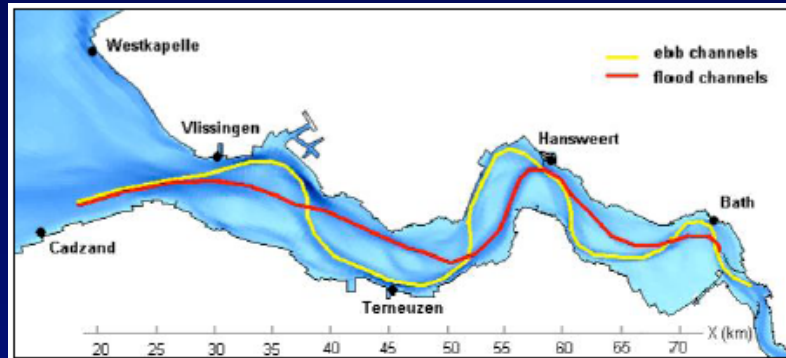
" The time it takes for any water particles of the sample to leave the lagoon  
through its outlet to the sea "; Dronkers and Zimmerman (1982); Prandle (1984).

" The time required for the total mass of a conservative tracer originally within the whole or a  
segment of the estuary to be reduced to a factor  $1/e$  ";  
Sanford et al. (1992); Luketina, (1998).



Prior to 1986 - export of sand from estuary to ebb tidal delta  
 After 1986 - import of sand into estuary

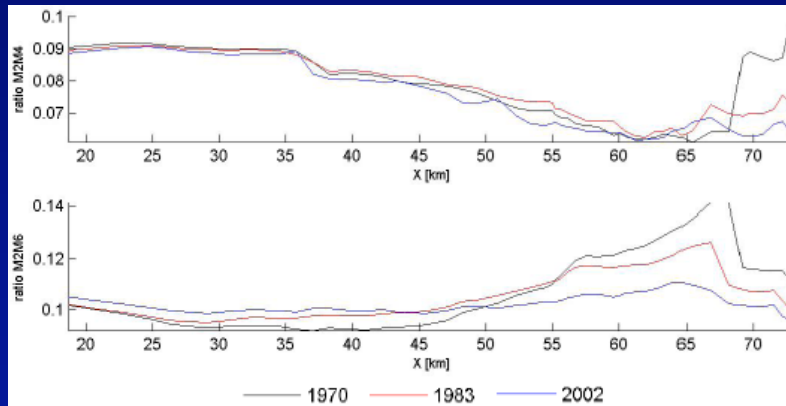
# Western Scheldt, Belgium - DELFT-3D



Flood and ebb dominance due to interplay of Semi-diurnal

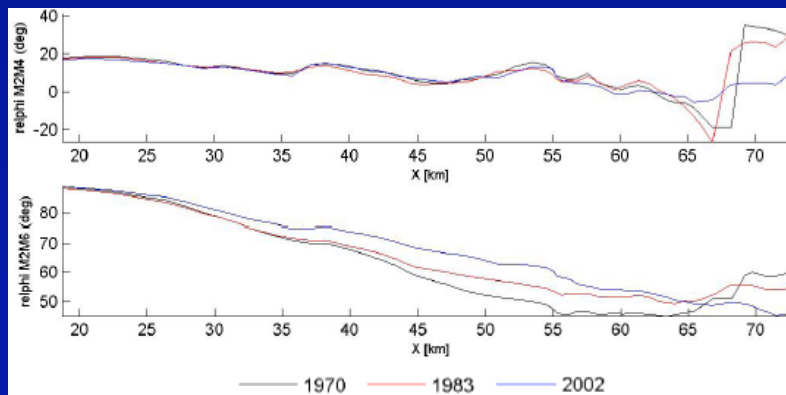
Amplitude ratio:  $M_2/M_4$ ,  $M_2/M_6$

Phase shift:  $2(\varphi_2 - \varphi_4)$ ,  $3(\varphi_2 - \varphi_6)$



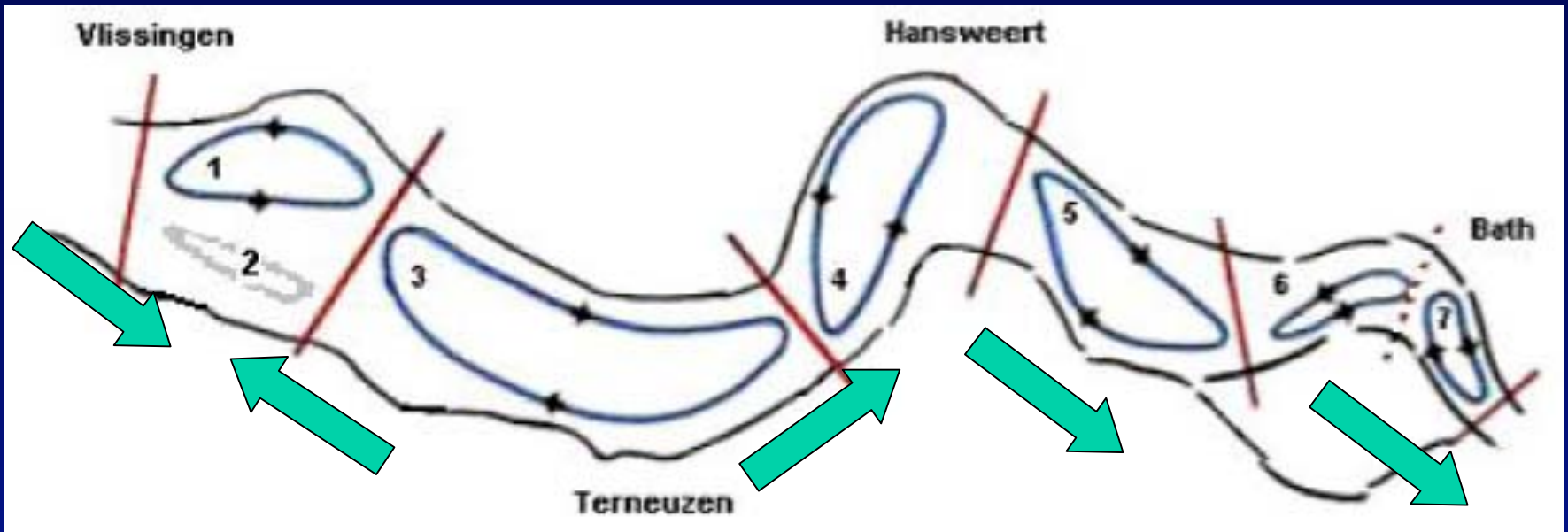
Major change in inner estuary

Major changes on central estuary



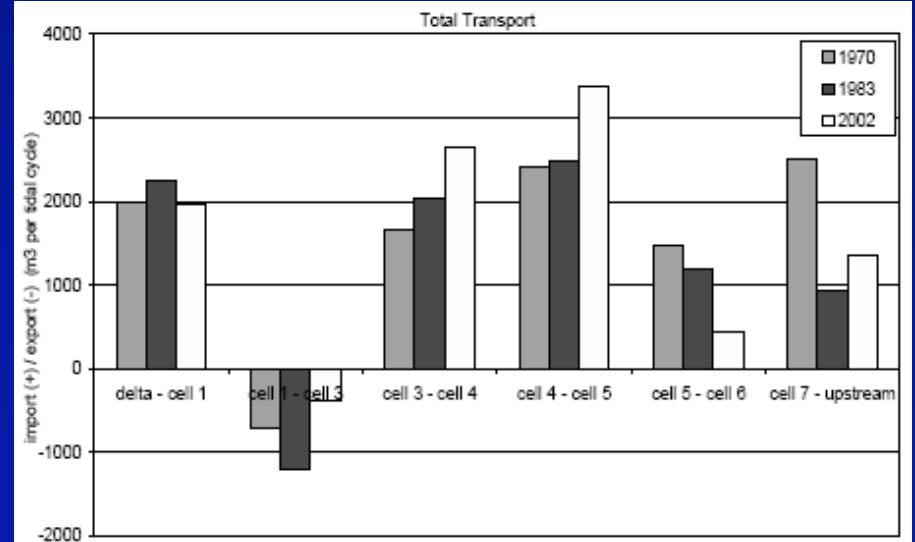
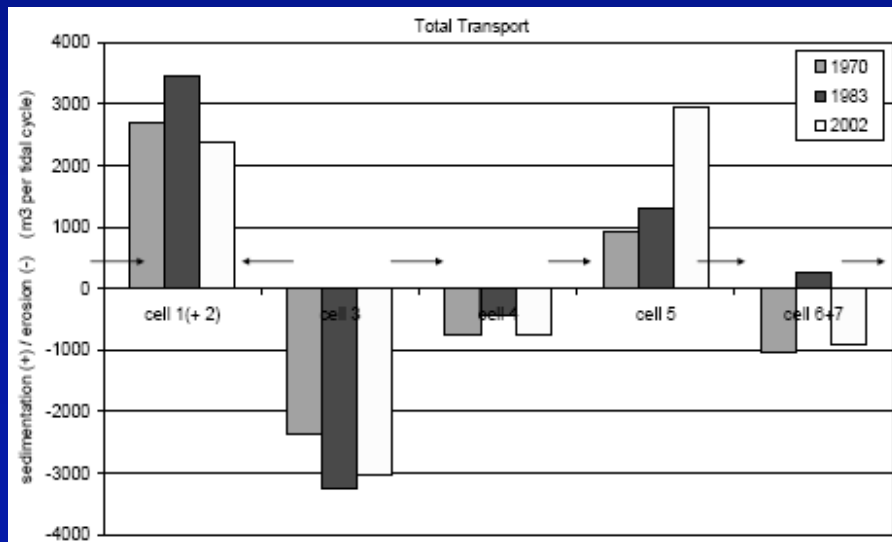
Major changes in inner estuary

Changes throughout estuary

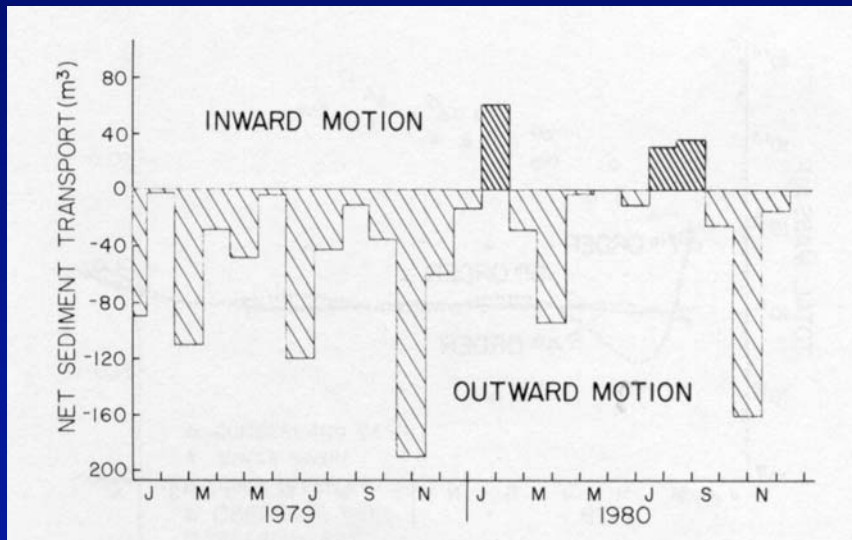


**Sedimentation/erosion**

**import/export**

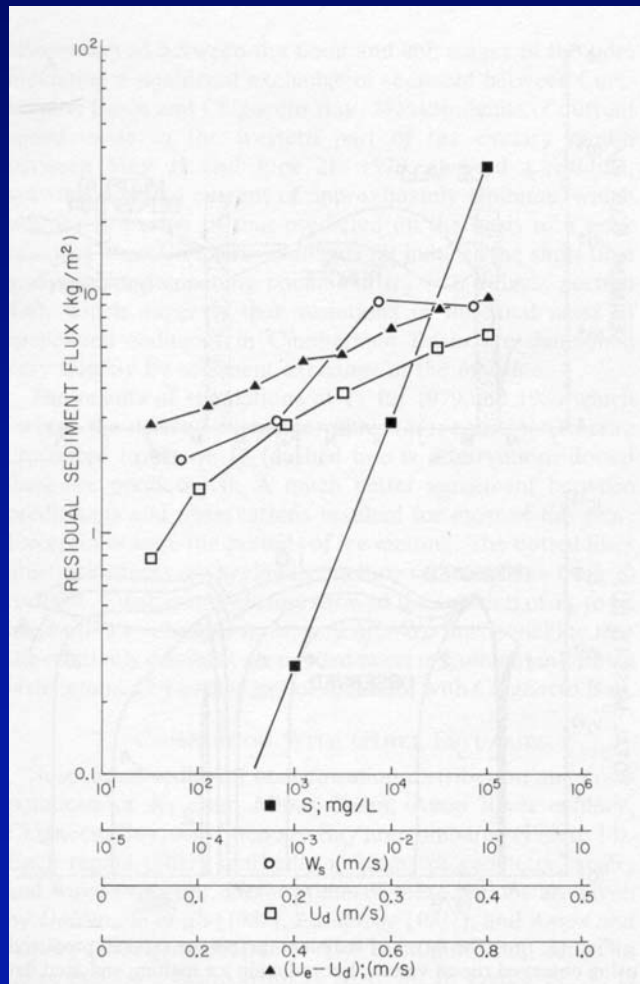


# The open boundary problem

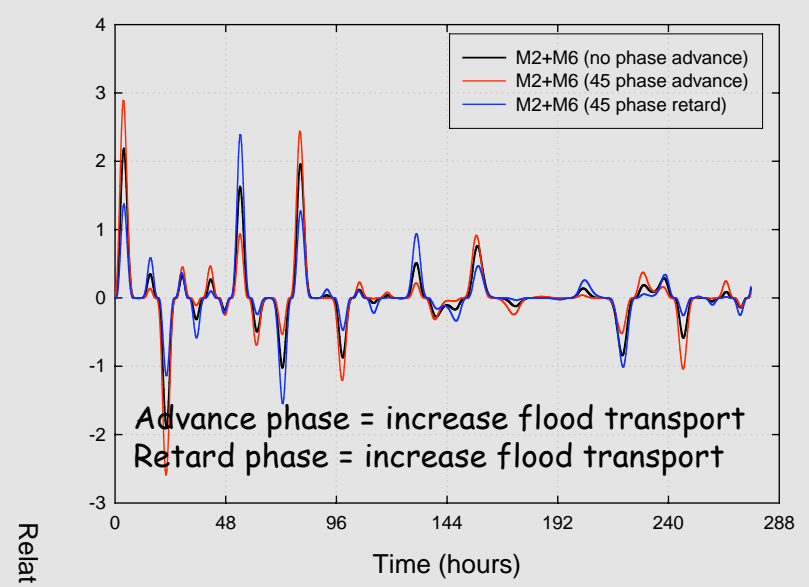
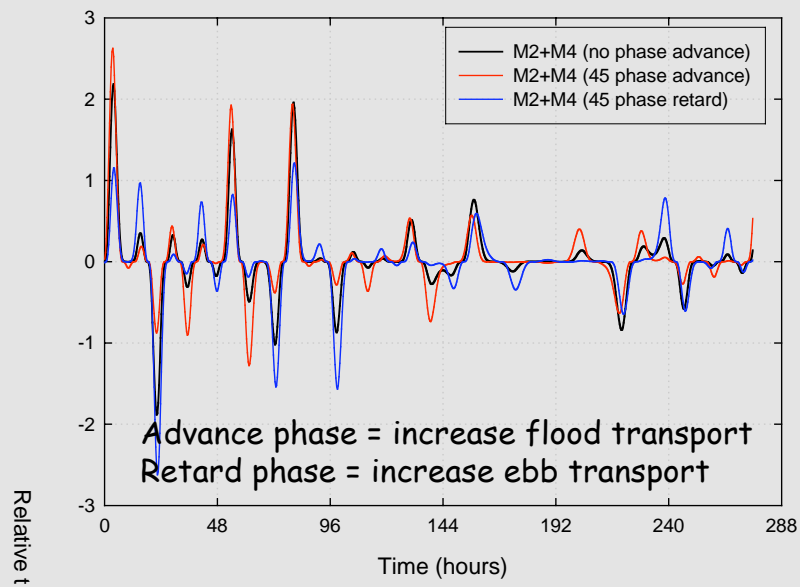
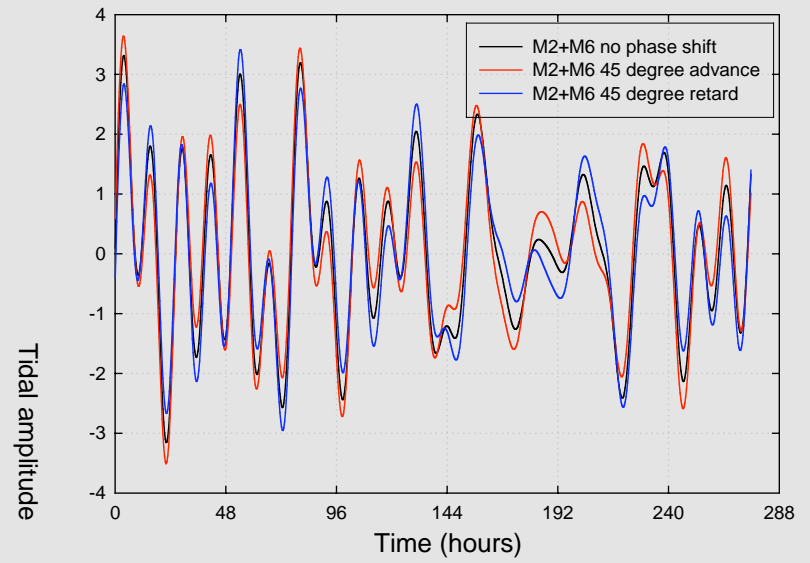
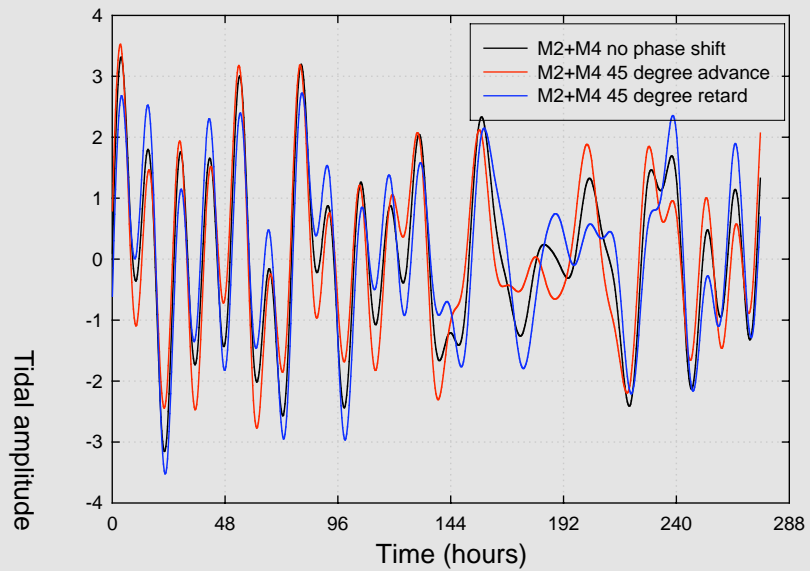


- The open boundary offers the greatest difficulty to measure and to predict accurately
- note the change from importing to exporting with time
- import and export linked to  $S$  and more importantly to  $S(x)$
- an estuary can change trapping efficiency depending on  $S$  gradient
  - caused by wave resuspension
  - dredging
  - tidal variations
  - construction, etc

## Sensitivity analysis of sediment flux rates at open boundary

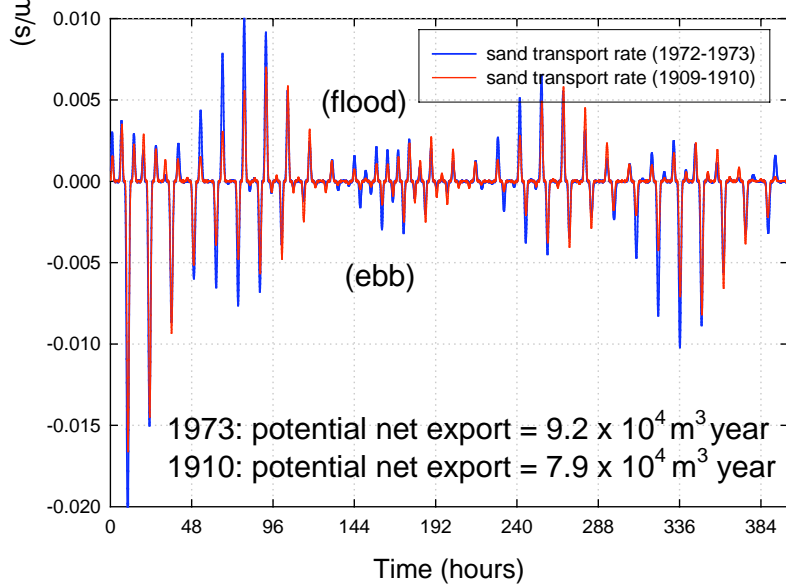
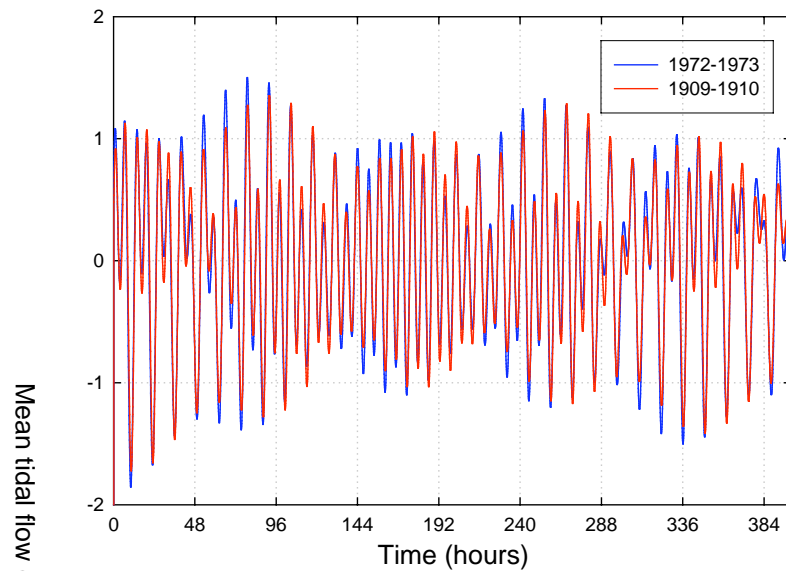


- $S$  - sediment concentration dominates
  - flux increases as  $S$  increases
- $W_s$  - flux increases with increased settling rate
- $U_d$  - deposition threshold
  - flux increases as threshold increases
- $U_e$  - erosion threshold
  - flux increases as threshold increases
- NOTE:  $S$  dominates the signal so should be the focus of measurement, input and calibration in model



tidal constituent	phase	relative transport
M2	--	--
M2+S2	--	--
M2+S2	45(S2)	.00082
M2+S2	-45(S2)	-0.0000942
M2+S2+M4	--	0.0153
M2+S2+M4+M6	--	0.0246
M2+S2+M4+M6	45(S2)	0.0228
M2+S2+M4+M6	-45(S2)	-7.7E-3
M2+S2+M4+M6	45(M4)	0.044
M2+S2+M4+M6	-45(M4)	-0.016
M2+S2+M4+M6	45(M6)	.0241
M2+S2+M4+M6	-45(M6)	0.024



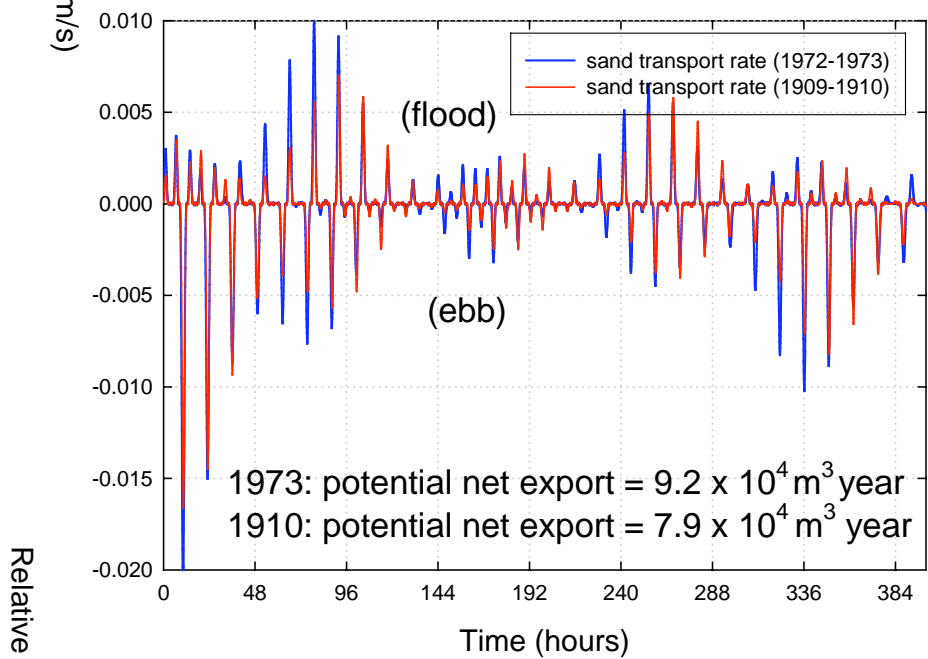
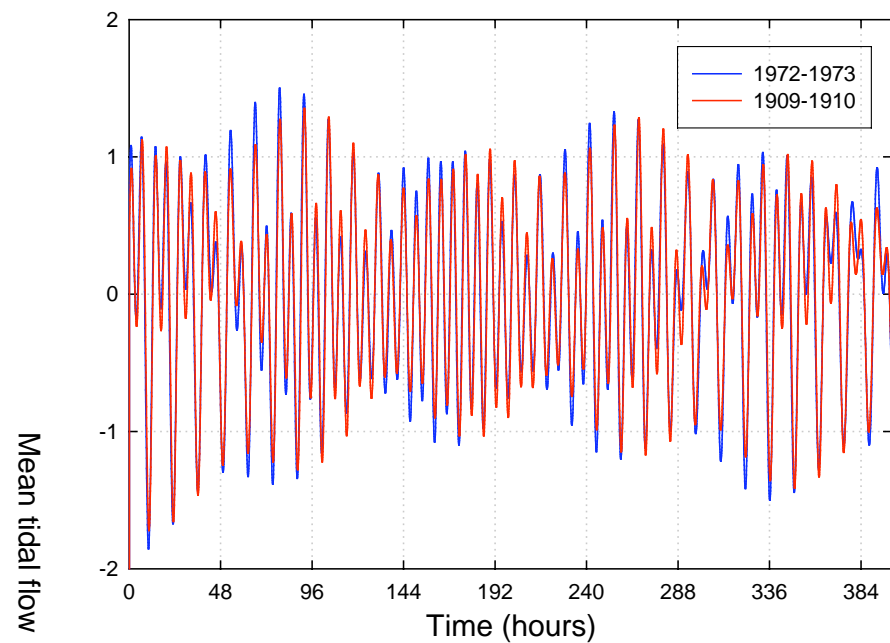


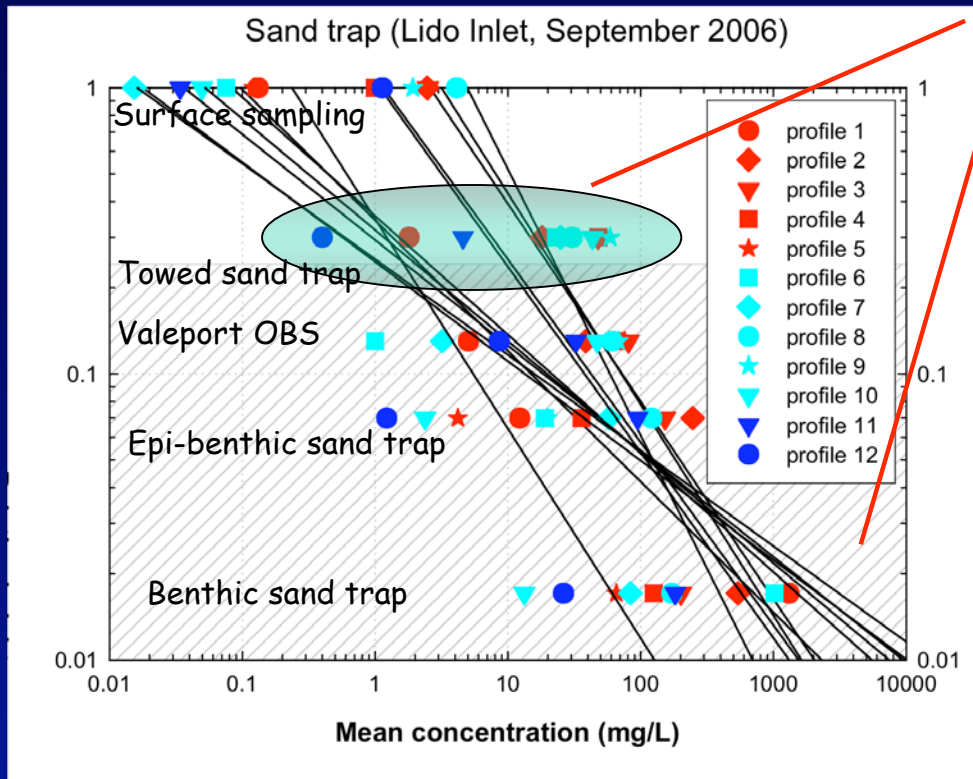
### 1909-1910

tidal constituent	amplitude(m)	phase	period(hours)
M2	0.22	305	12.421
S2	0.127	312	12
N2	0.036	301	12.658
K2	0.035	315	11.97
K1	0.169	87	23.934
O1	0.05	67	25.819
P1	0.053	82	24.07

### 1972-1973

M2	0.242	310	12.421
S2	0.143	319	12
N2	0.042	310	12.658
K2	0.041	310	11.97
K1	0.175	87	23.934
O1	0.052	79	25.819
P1	0.057	85	24.07





Lido Sud (fixed ADCP site)  
Shaded region is the shadow zone of ADCP

PROFILE #	R-squared	1/m	b
1	0.91	1.45	0.2
2	0.98	0.89	-0.16
3	0.82	0.79	-0.49
4	0.65	0.94	-0.51
5	0.47	1.45	-0.59
6	0.77	1.59	-0.15
7	0.66	1.79	-0.71
8	0.26	1.02	-1.1
9	0.99	0.26	-0.01
10	0.26	2.08	-1
11	0.89	1.49	-0.38
12	0.55	0.86	-0.02

$$\log_{10}(z) = m \log(C) + b$$

$$C = (z)^{\frac{1}{m}} 10^{\frac{-b}{m}}$$

$$z = \frac{h}{H - a}$$

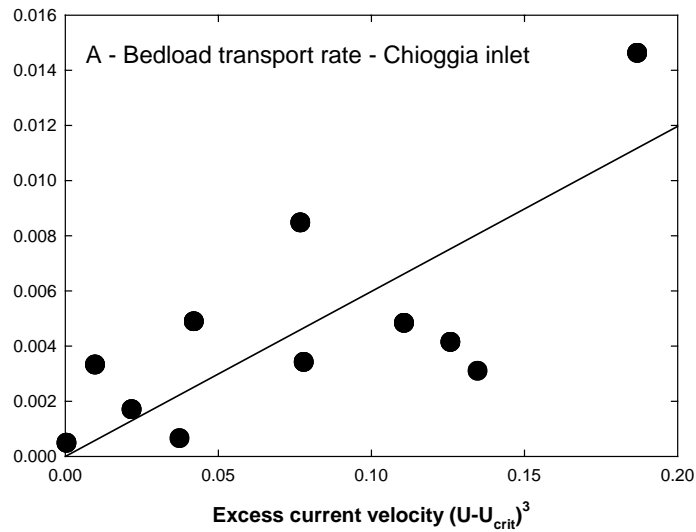
Suspension number  
Our results  $1/m = -0.93$

$C$  = concentration (sand)  
 $Z$  = relative height  
 $h$  = sample height  
 $H$  = water depth  
 $a$  = reference conc. height

$$\frac{1}{m} = \left( \frac{W_s}{\beta \kappa U_*} \right) \approx 0.93$$

$$\left| \frac{W_s}{U_*} \right| = 0.93 \beta \kappa \approx 0.38$$

$$k = 0.4; \beta = 1$$

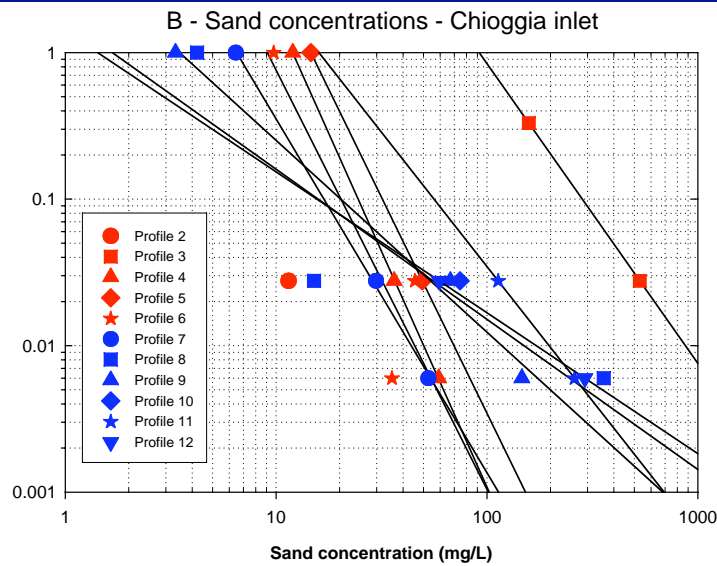


$$G_s = 0.06(\bar{U} - U_{crit})^3 \text{ kg / m / s (Chioggia)}$$

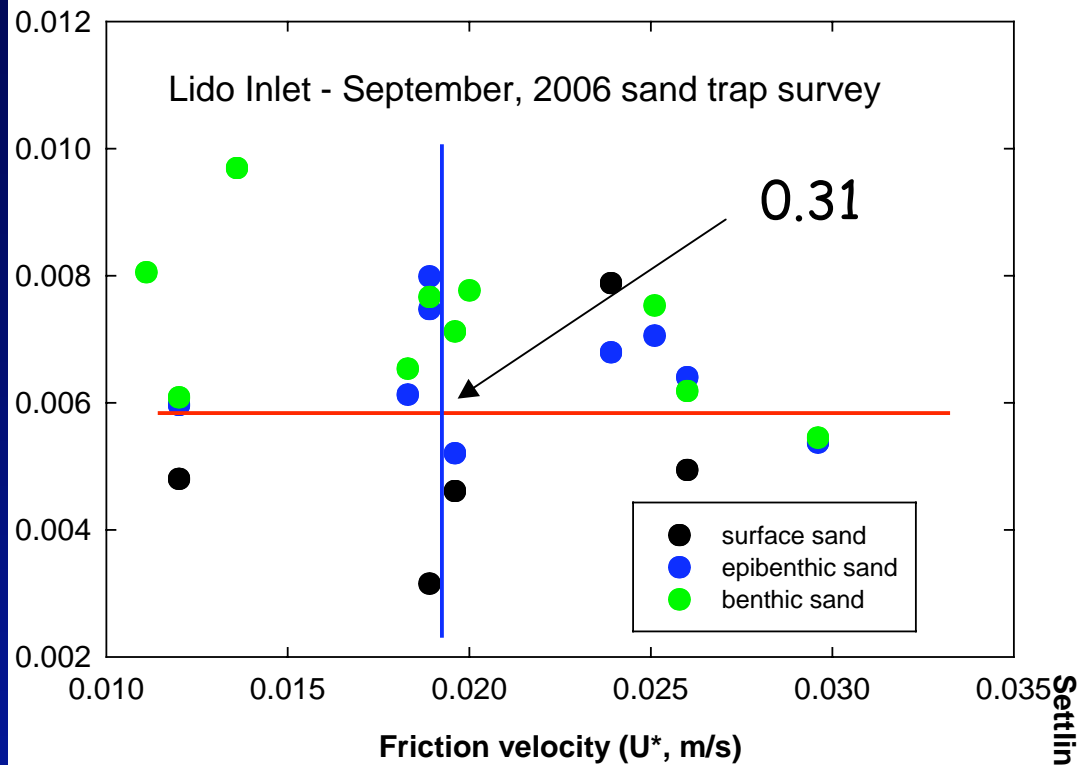
$$G_s = 0.52(\bar{U} - U_{crit})^3 \text{ kg / m / s (Lido)}$$

Gadd *et al.* (1976) relationship for fine sand coefficient from 1.73 to 7.33 (wave-dominated shelf)

$Ws/U^*$  is evaluated as  $0.4 * m = 0.23$



PROFILE	U (m/s)	STAGE OF TIDE	1/m
3	0.77	EBB	-0.49
4	0.71	FLOOD	-0.31
5	0.7	FLOOD	-0.34
6	0.63	FLOOD	0.35
7	0.48	FLOOD	-0.41
8	0.27	EBB	-0.97
9	0.42	EBB	-0.76
11	0.62	EBB	-0.54
12	0.68	EBB	-1.04



Settling rate measured in NOC sedimentation column (1.8 m)

$U_*$  derived from TKE method on ADV (25 Hz) time-series (7500 data points)

Linear (inverse) relationship between friction velocity ( $U_*$ ) and settling rate ( $W_s$ )

Inverse relationship i.e. Faster flows have finer grains !!!

$W_s/U_*$  given by van Rijn et al. (1997) as 2.5 (turbulent rough)

$W_s/U_*$  given by Bagnold (1966) as 1.25 (turbulent rough)

Using measured values from Lido yields a value of 0.38 (turbulent smooth)

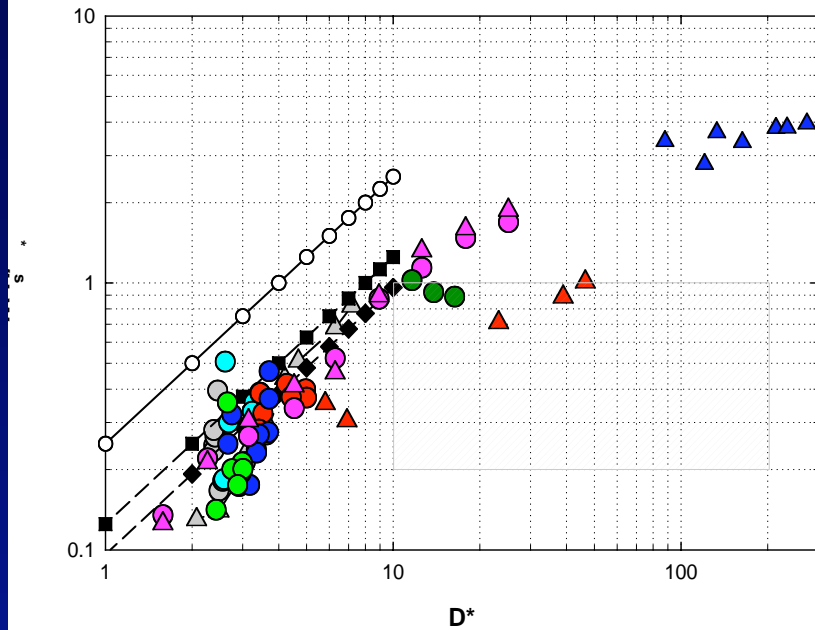
Using measured values from Chioggia yields a value of 0.29 (turbulent smooth)

$$\frac{W_s}{U_*} = 0.38 \text{ (Lido)}$$

$$\frac{W_s}{U_*} = 0.29 \text{ (Chioggia)}$$

## Summary of results ( $Ws/U^*$ ) - Venice lagoon, 2006

	Lido Inlet	Chioggia Inlet
Measured from SSC profiles	0.38	0.29
Measured from samples	0.31	0.23
$D^* = 10$	1.0	1.0



- △— Roe (2007) natural beach sand (sieved)
- epi-benthic, Venice lagoon, Lido (2006)
- van Rijn (1993), ( $D^*/4$ )
- Bagnold (1966) ( $V^{\text{up}} = 1.56V$ ), ( $D^*/8$ )
- ◆— Bagnold (1966) ( $V^{\text{up}} = 0.6V$ ) ( $D^*/10$ )
- benthic, Venice lagoon, Lido (2006)
- Benthic, Chioggia (2006)
- Epi-benthic traps, Chioggia (2006)
- Surface traps, Chioggia (2006)
- Blair (2007) Jamaica beach carbonate sand (susp)
- Blair (2007) Jamaica beach quartz sand (suspens)
- Ridley (2004) natural sand (suspension)
- Ridley (2004) fish feed pellets
- Ridley (2004) bakelite granules

$D^*$  is dimensionless grain diameter

$W_s$  = still water fall velocity

$U^*$  = critical friction velocity

$$D_* = \left| \frac{(\rho_s - \rho)g}{\rho v^2} \right|^{0.333} d_{50}$$

$$\frac{W_s}{U_*} = \frac{\chi}{D_*}, D_* < 10$$

$$\frac{W_s}{U_*} = \text{const.}, D_* > 10$$

$$\theta_{crit,susp} = \frac{\chi^2}{D_*^2} \left[ \frac{\rho}{\rho_s - \rho} \right] \frac{W_s^2}{gd_{50}}, D_* < 10$$

$$\theta_{crit,susp} = \text{const.} \left[ \frac{\rho}{\rho_s - \rho} \right] \frac{W_s^2}{gd_{50}}, D_* > 10$$

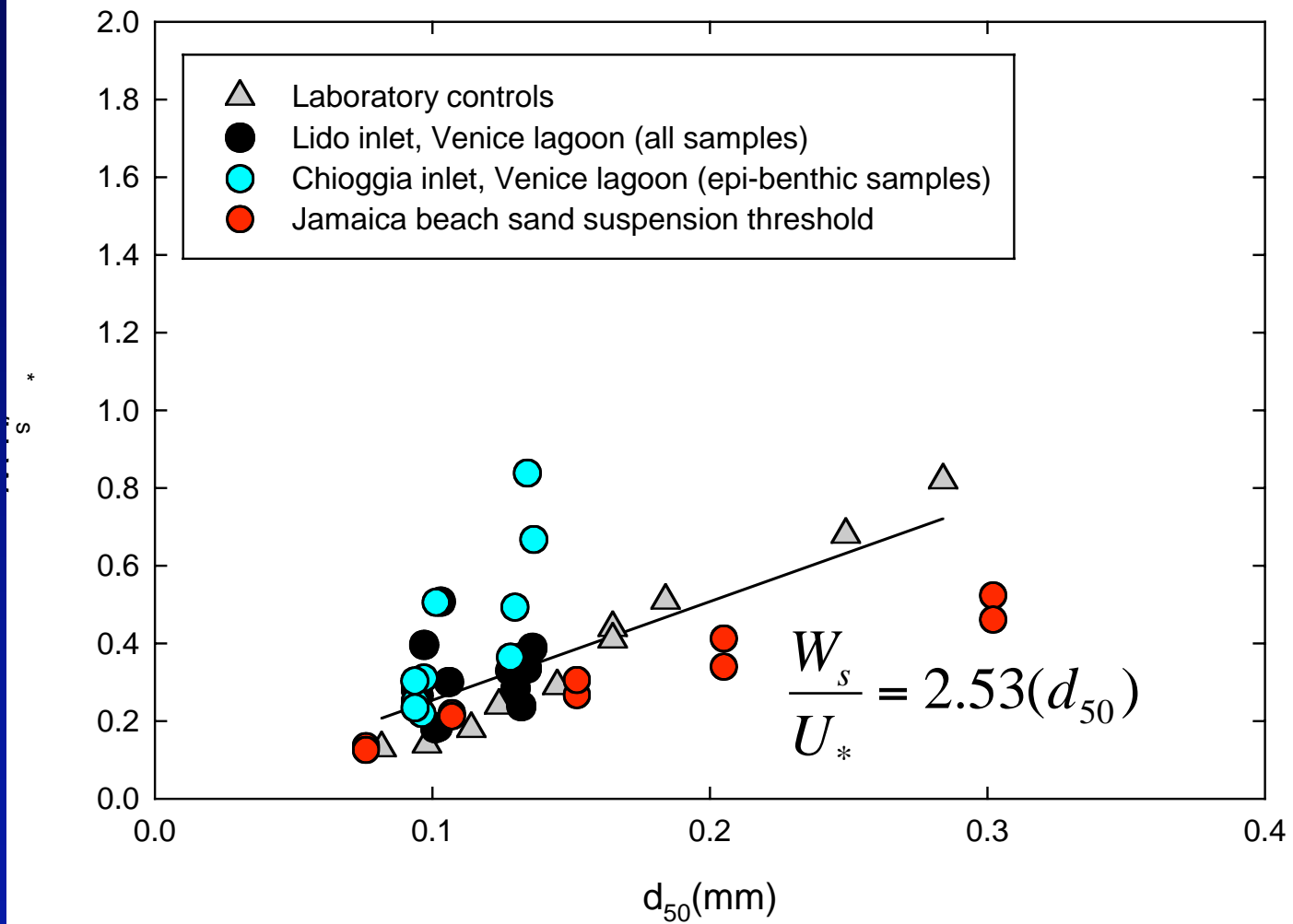
$W_s/U^* = 10/D^*$   
Lower than van Rijn ( $4/D^*$ )

Critical Shields parameter for suspension lower than Bagnold (1966)

Yields good separation between bedload and suspended load samples from Lido inlet.

$$\Theta_{crit,susp} = 0.043D_*^{1.152}, D_* < 10$$





## Fundamental issues and questions regarding estuarine retention - short term prediction

Can we accurately define the transport pathways, depo-centres, and concentration profiles of (1) fines, and (2) sands in estuaries?

Do we understand the links between sand and fines along a transport pathway?

Can we predict morphodynamical evolution?

Do we understand the link between morphodynamical changes and hydrodynamics (waves and tidal currents)?

What is the true relevance of biological feedbacks to estuarine evolution

What controls the trapping efficiency (F) of an estuary?

### Estuarine filtering efficiency (F)

where  $Q_{loss}$  is the net export from the inlets  
while  $Q_{total}$  is the total mass balance  
and  $Q_{total} = Q_{onshore} + Q_{offshore} + Q_{longshore}$

$$F = \left[ 1 - \frac{Q_{loss}}{Q_{total}} \right]$$

Fundamental issues and questions regarding estuarine retention  
- long term prediction

Largely empirical based

Can we accurately define the morphological evolution of an estuary?  
Does predicted morphological change fit with "regime" based theories?

Does predicted evolution fit with theories of sediment dynamics?

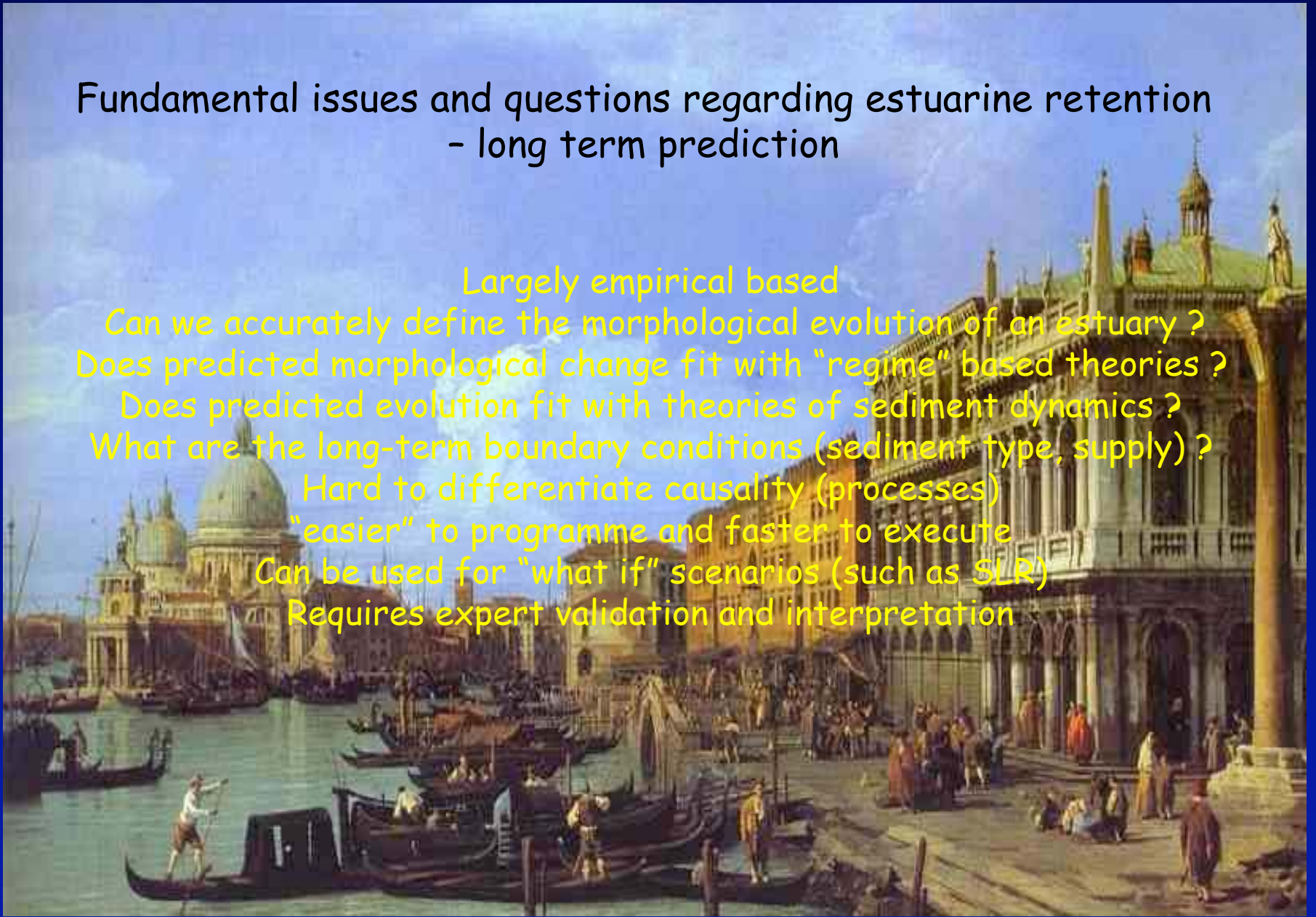
What are the long-term boundary conditions (sediment type, supply)?

Hard to differentiate causality (processes)

"easier" to programme and faster to execute

Can be used for "what if" scenarios (such as SLR)

Requires expert validation and interpretation



# THE NUMERICAL MODEL

## • Shallow Water Finite Element Model (SHYFEM)

$$\frac{\partial U}{\partial t} - fV + gH \frac{\partial \zeta}{\partial x} + RU + F_x = 0$$

$$\frac{\partial V}{\partial t} + fU + gH \frac{\partial \zeta}{\partial y} + RV + F_y = 0$$

$$\frac{\partial \zeta}{\partial t} + \frac{\partial U}{\partial x} + \frac{\partial V}{\partial y} = 0$$

$$U = \int_{-h}^{\zeta} u \partial z$$

Barotropic transport

$$V = \int_{-h}^{\zeta} v \partial z$$

$$R = \frac{c_b}{H} \sqrt{u^2 + v^2}$$

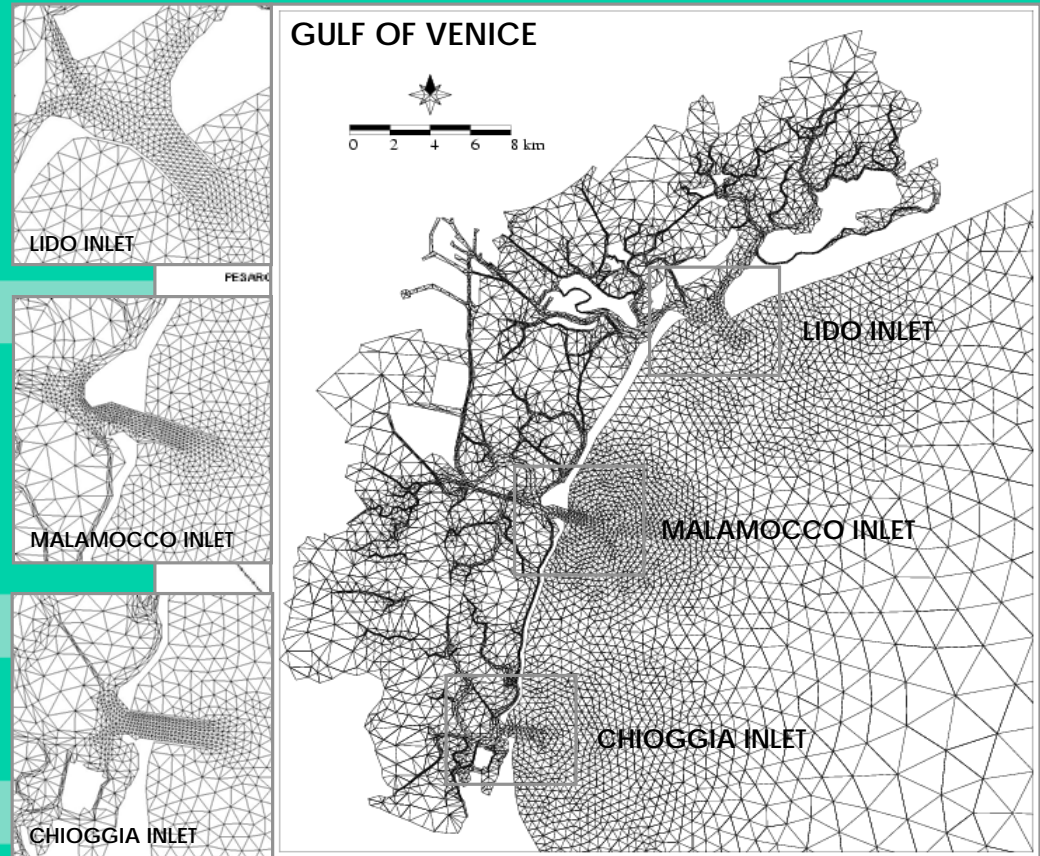
Friction term

$$F_x = \int_{-h}^{\zeta} \left[ \frac{\partial p_H}{\rho_0 \partial x} + \hat{f}_x \right] dz + \frac{1}{\rho_0} (\tau_x^B - \tau_x^W)$$

$$p_H = p_s + \int_z^{\zeta} g \rho^1(z) dz$$

Wind stress,  
non-linear  
advective terms ...

**MODEL DOMAIN** F.E. grid of the Adriatic Sea and Venice Lagoon (8072 nodes, 15269 elements, spatial resolution varying from 30 Km to 50 m)



# THE TRANSPORT TIME SCALES

## RESIDENCE TIME (Eulerian approach)

“ THE TIME REQUIRED FOR EACH ELEMENT OF THE DOMAIN TO REPLACE THE MASS OF A CONSERVATIVE TRACER, ORIGINALLY RELEASED, WITH NEW WATER ”

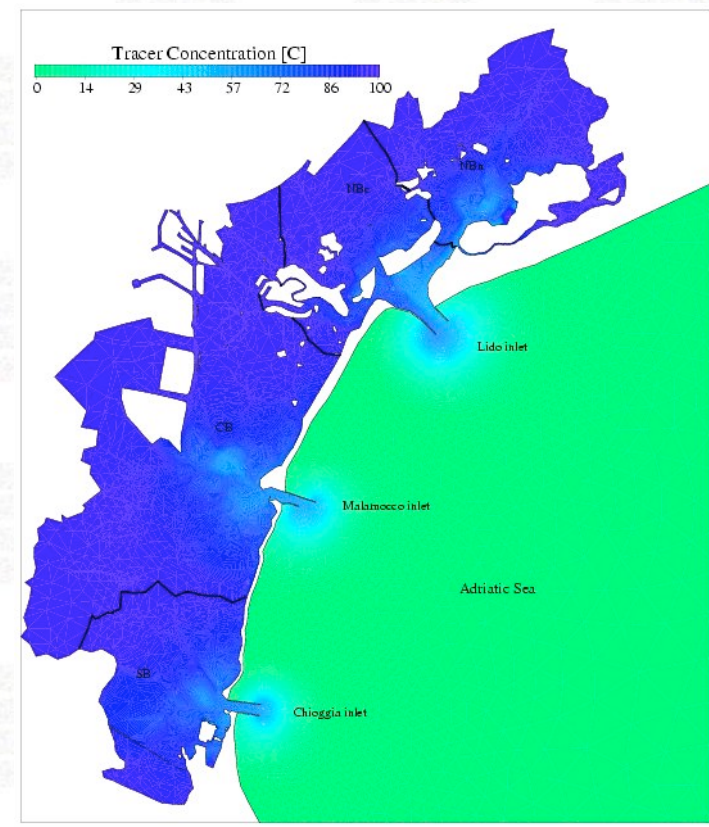
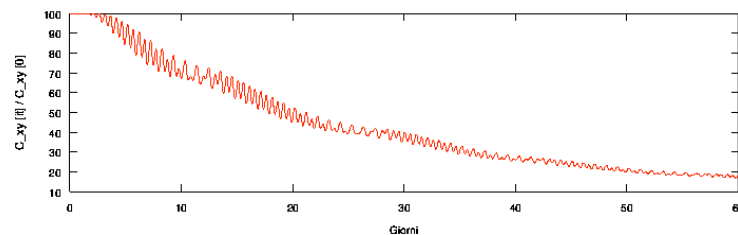
• TRACER [C] IN THE LAGOON = 100 %

$$S_0 = S(t = 0)$$

• TIDE AND WIND ACTION DRIVES IT OUT THE BASIN

$$\frac{\partial S}{\partial t} + \frac{\partial uS}{\partial x} + \frac{\partial vS}{\partial y} = K_H \left( \frac{\partial^2 S}{\partial x^2} + \frac{\partial^2 S}{\partial y^2} \right)$$

• TIME DECAY OF THE TRACER CONCENTRATION



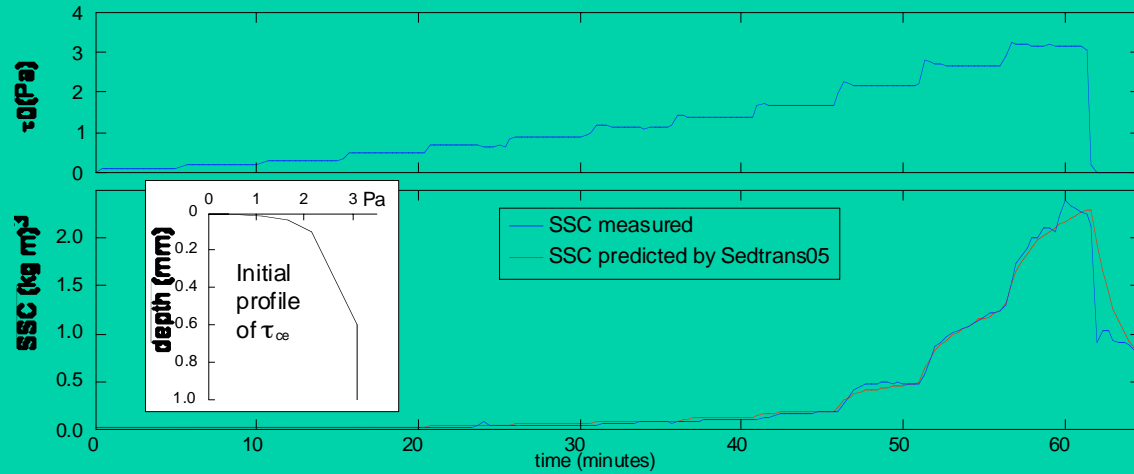
• DEFINITION OF THE REMNANT FUNCTION (Takeoka, 1984 a,b)

$$r(x, y, t) = S(x, y, t) / S_0$$

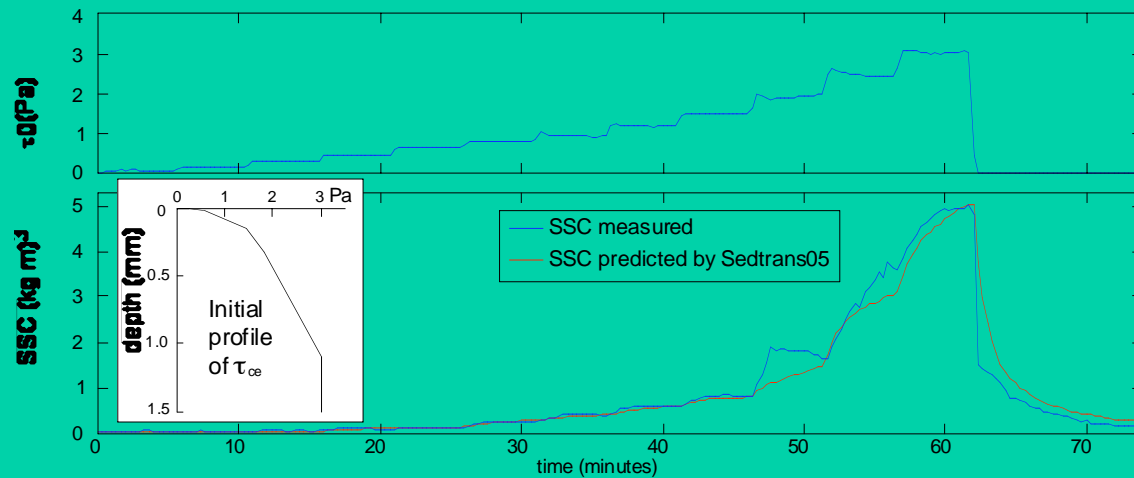
• DEFINITION OF THE WATER RESIDENCE TIME

$$\tau(x, y) = \int_0^{\infty} r(x, y, t) dt$$

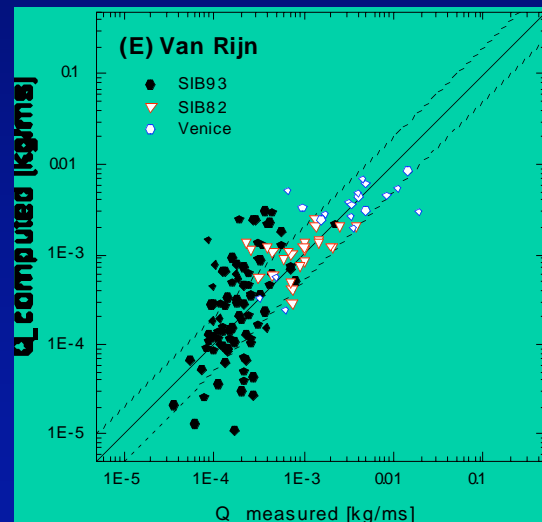
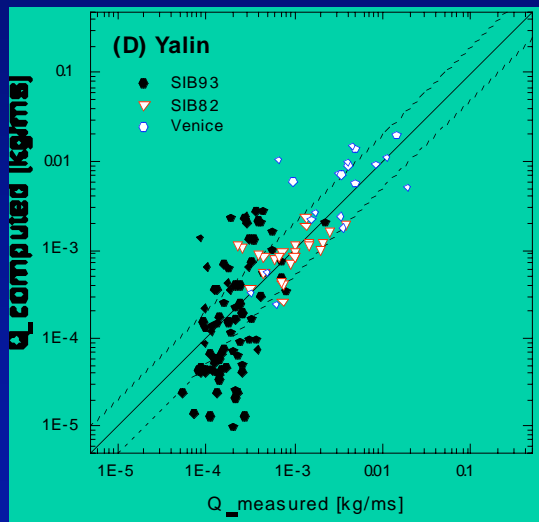
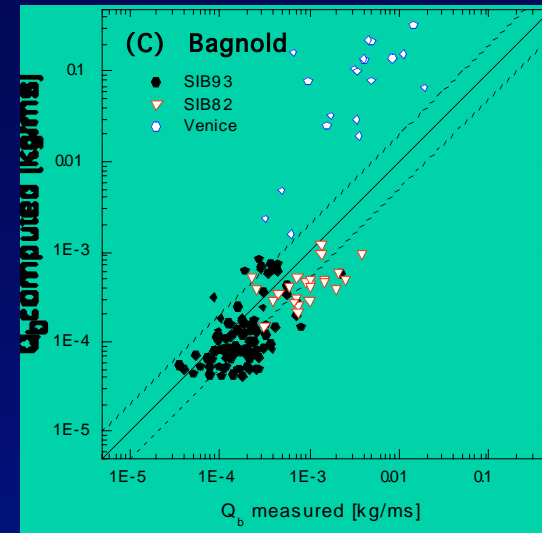
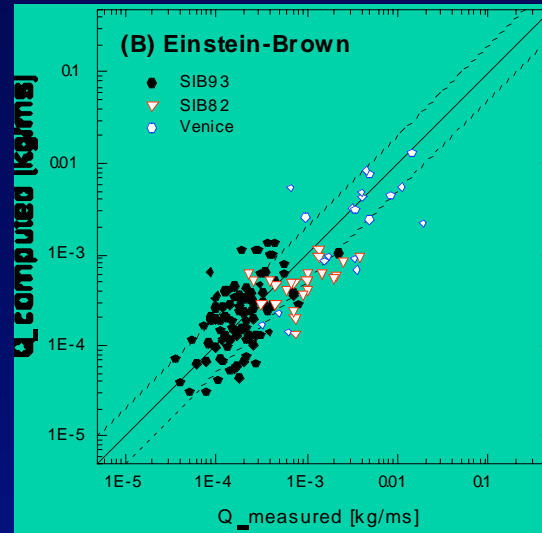
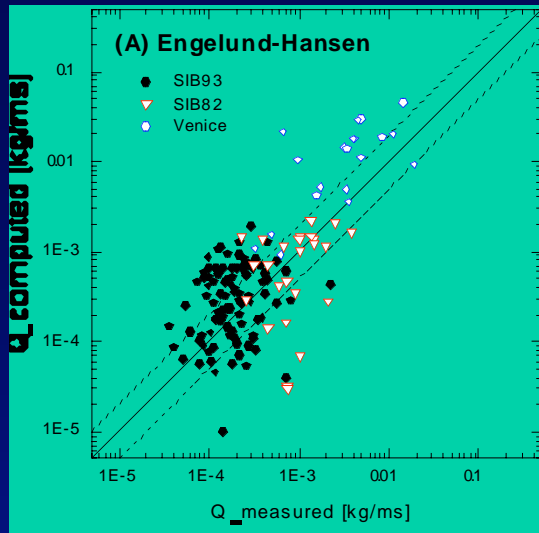
### A) Station V20



### B) Station V30



A comparison of the cohesive sediment algorithm with field data collected with the Sea Carousel in Venice lagoon (Stations 20 and 30, February 1999). The initial profile of critical erosion threshold  $\tau_{ce}$ , and the time-series of applied bed shear stress  $\tau_0$ , measured SSC, and SSC predicted by Sedtrans05 are shown.



A comparison between the measured rates of sediment transport and the rates computed according to the five non-cohesive transport equations in Sedtrans05. Solid dots are data from the 1993 deployment over medium sand (SIB93), triangles are data from the 1982 deployment over fine sand (SIB82), and open circles are data from Venice (2006). The solid line indicates perfect agreement; the dashed lines represent the factors 0.5 and 2.

## THE TRANSPORT TIME SCALES

### THE RETURN FLOW FACTOR (b)

FROM TIDAL PRISM METHOD:  
THE AVERAGE WATER RESIDENCE TIME IS DEFINED AS:

$$\tau_{av} = \frac{TV_{av}}{(1-b)P}$$

b IS THE RETURN FLOW FACTOR. IT EXPRESSES THE FATE OF THE WATER ONCE IT IS OUTSIDE THE EMBAYMENT

#### •DEFINITION OF THE RFF (b)

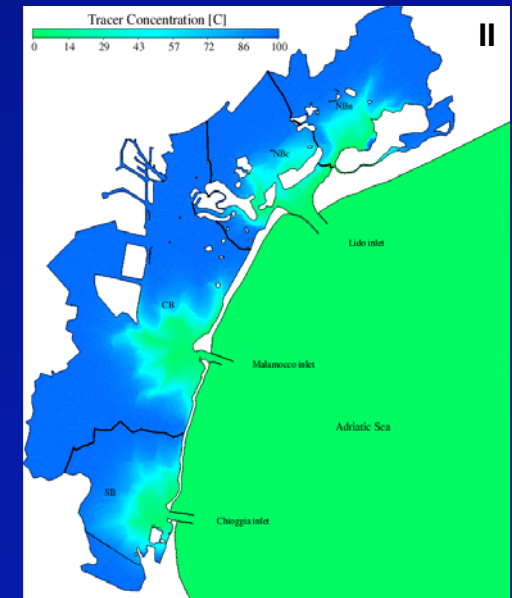
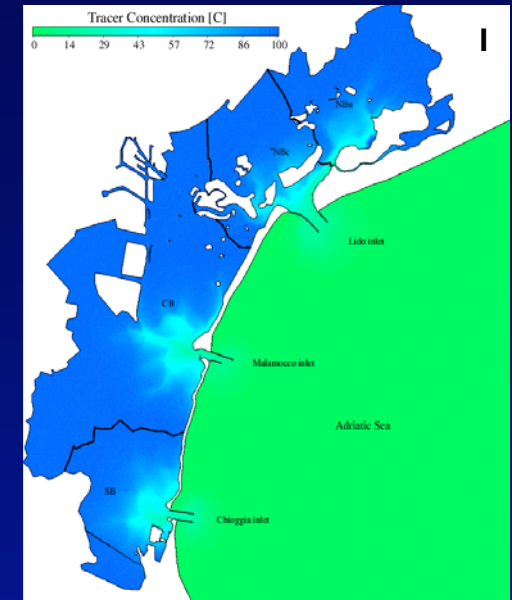
SIMULATION I, THE MASS OF THE TRACER EXITED THE LAGOON CAN RETURN TO THE EMBAYMENT.  $\tau_{Av}$  IS COMPUTED

SIMULATION II, THE MASS OF THE TRACER EXITED THE LAGOON IS SET TO ZERO, (b=0).  $\tau_0$  IS COMPUTED

$$\tau_0 = \frac{TV_{av}}{P} \longrightarrow \tau_{av} = \frac{\tau_0}{1-b}$$

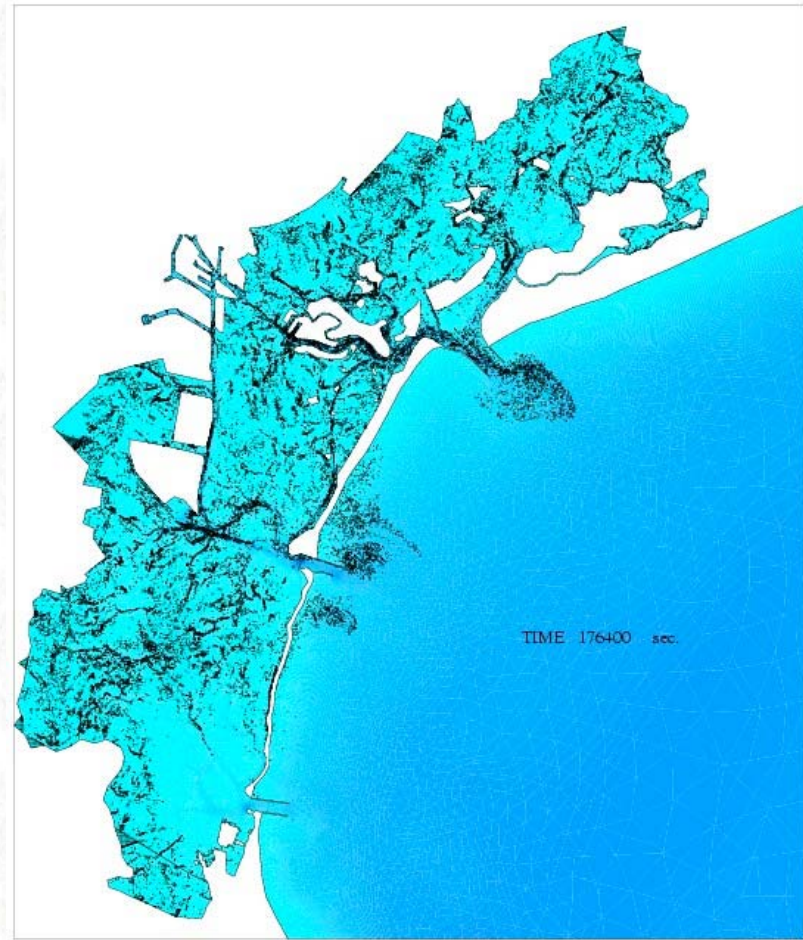
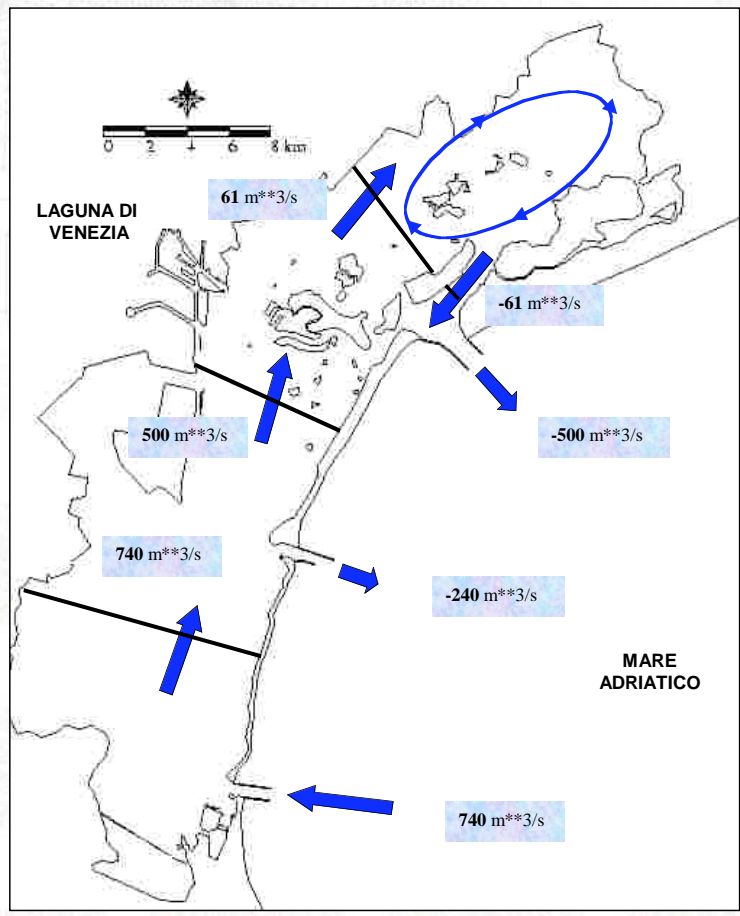
THE RFF IS DEFINED AS:

$$b(x, y) = \frac{\tau(x, y) - \tau_0(x, y)}{\tau(x, y)}$$



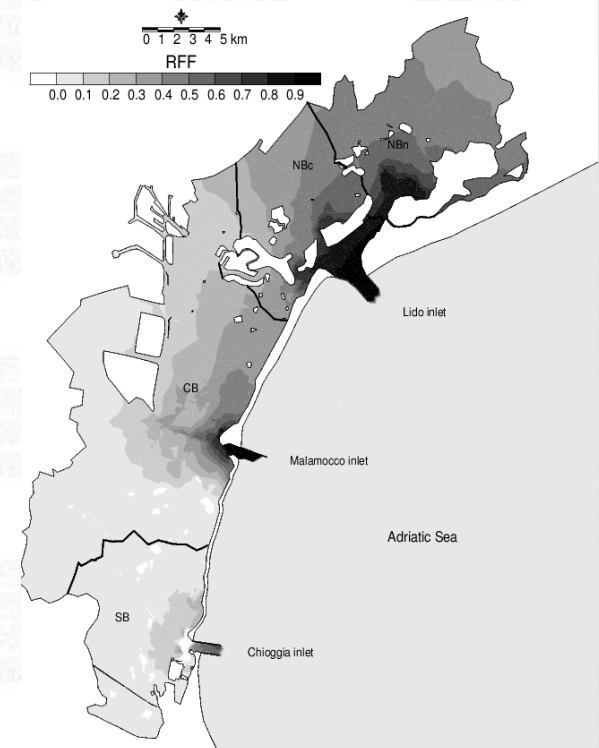
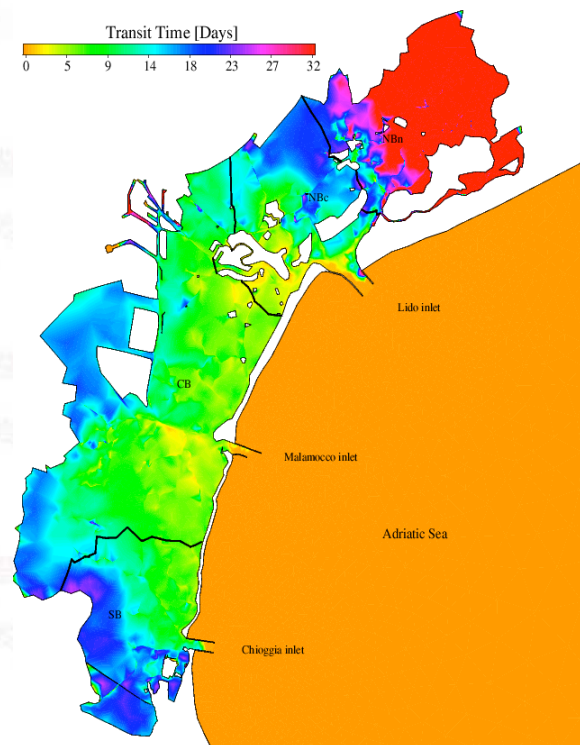
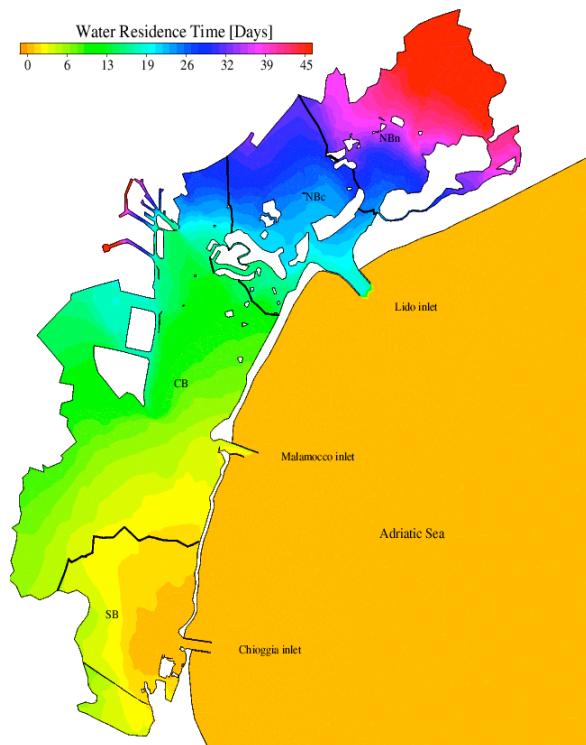


# SCENARIO: TIDE AND SIROCCO WIND (7 m/s) ↗

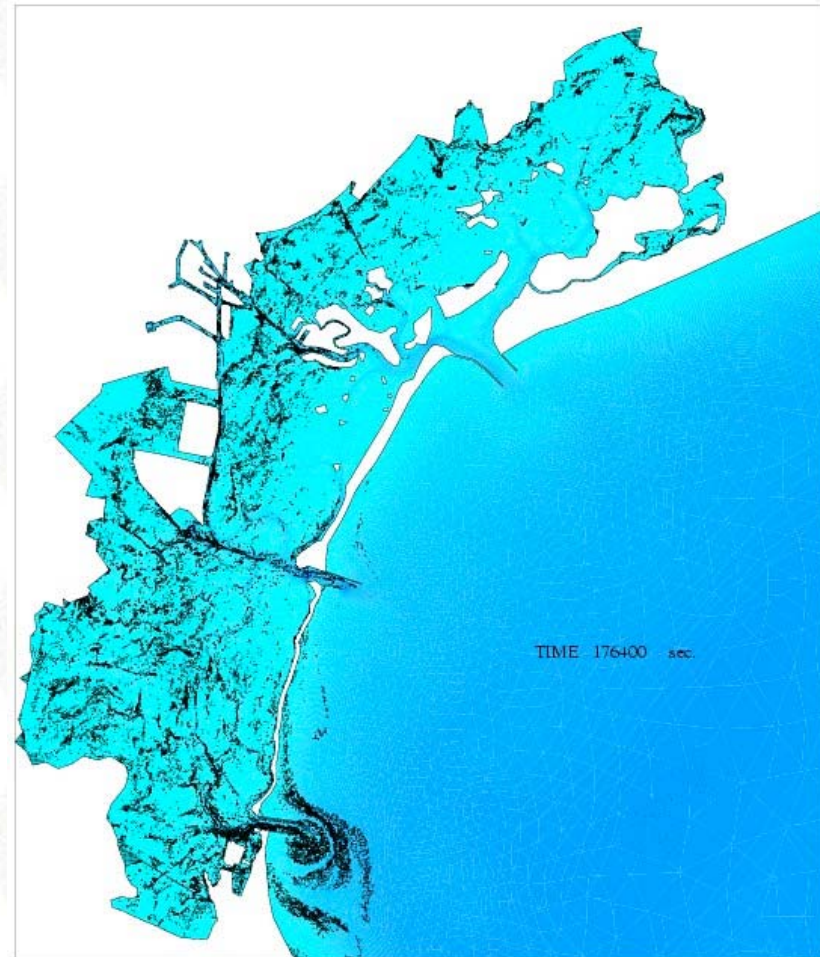
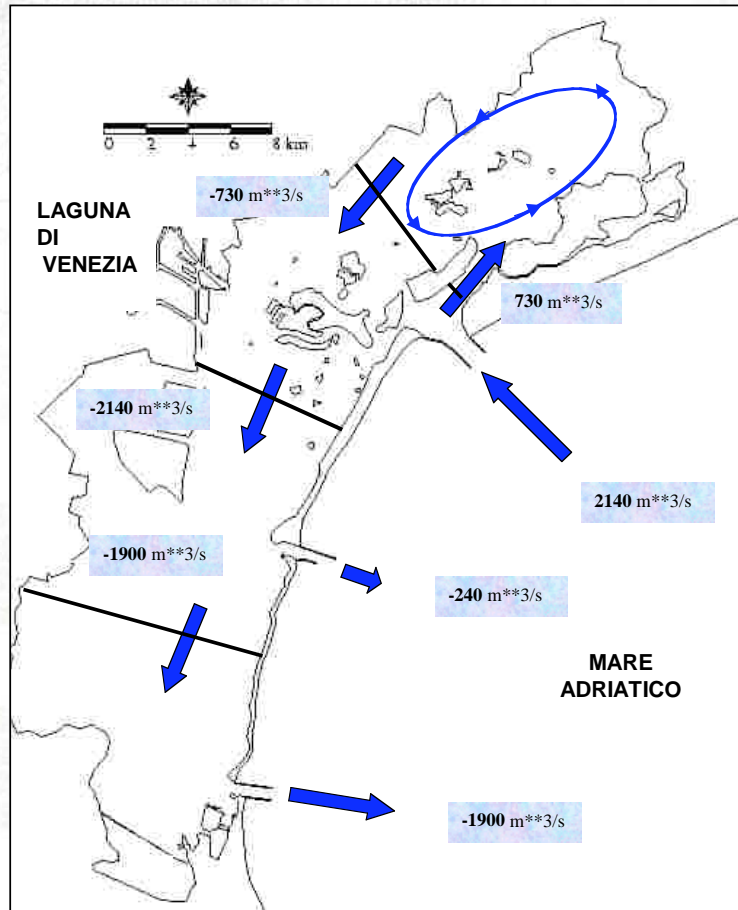


# SCENARIO: TIDE AND SIROCCO WIND (7 m/s)

TRANSPORT TIME SCALE	Total	NBn	NBc	CB	SB
WRT	$16 \pm 8$	$38 \pm 9$	$23 \pm 6$	$10 \pm 6$	$2 \pm 1$
		$32 \pm 10$		$8 \pm 6$	
WTT	$18 \pm 9$	$37 \pm 14$	$11 \pm 6$	$10 \pm 5$	$13 \pm 6$
		$26 \pm 17$		$11 \pm 5$	
RFF	<b>0.3</b>	<b>0</b>	<b>0</b>	<b>0</b>	<b>0</b>

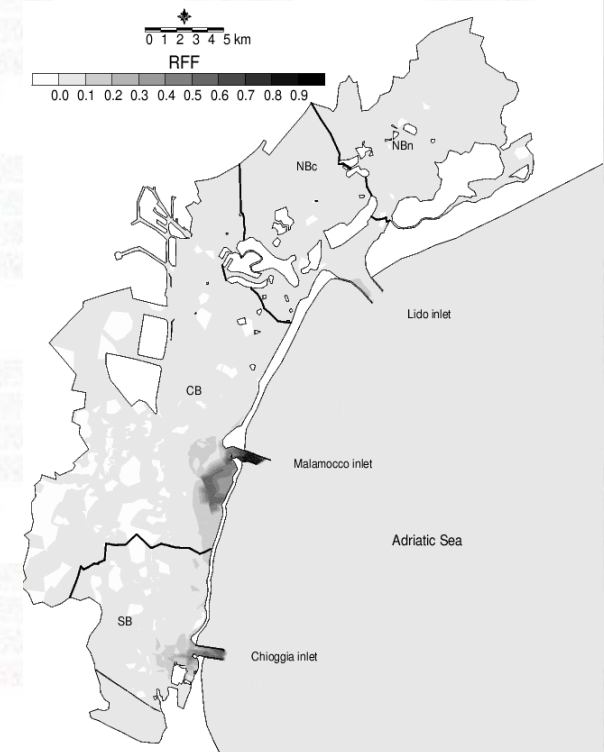
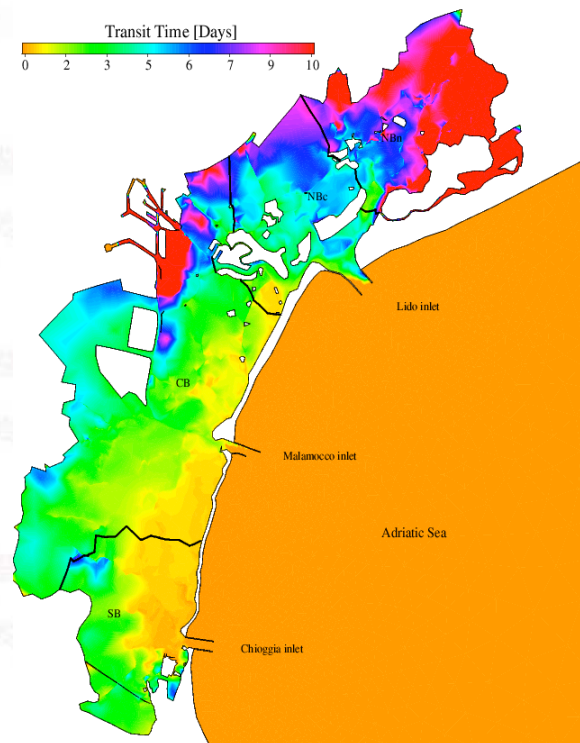
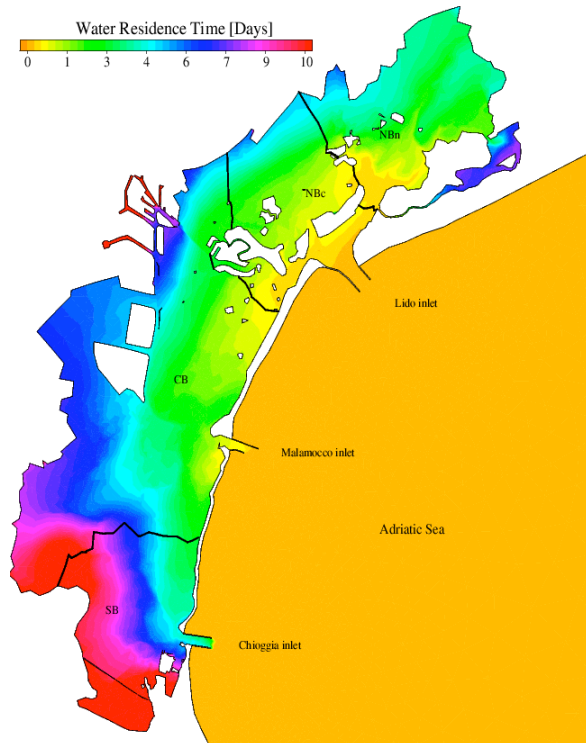


# SCENARIO: TIDE AND BORA WIND (10 m/s) ↙



# SCENARIO: TIDE AND BORA WIND (10 m/s) ✓

TRANSPORT TIME SCALE	Total	NBn	NBc	CB	SB
WRT	$4 \pm 4$	$3 \pm 1$	$2 \pm 1$	$5 \pm 3$	$7 \pm 3$
WTT	$4 \pm 2$	$9 \pm 4$	$4 \pm 1$	$3 \pm 2$	$2 \pm 1$
RFF	0	0	0	0	0

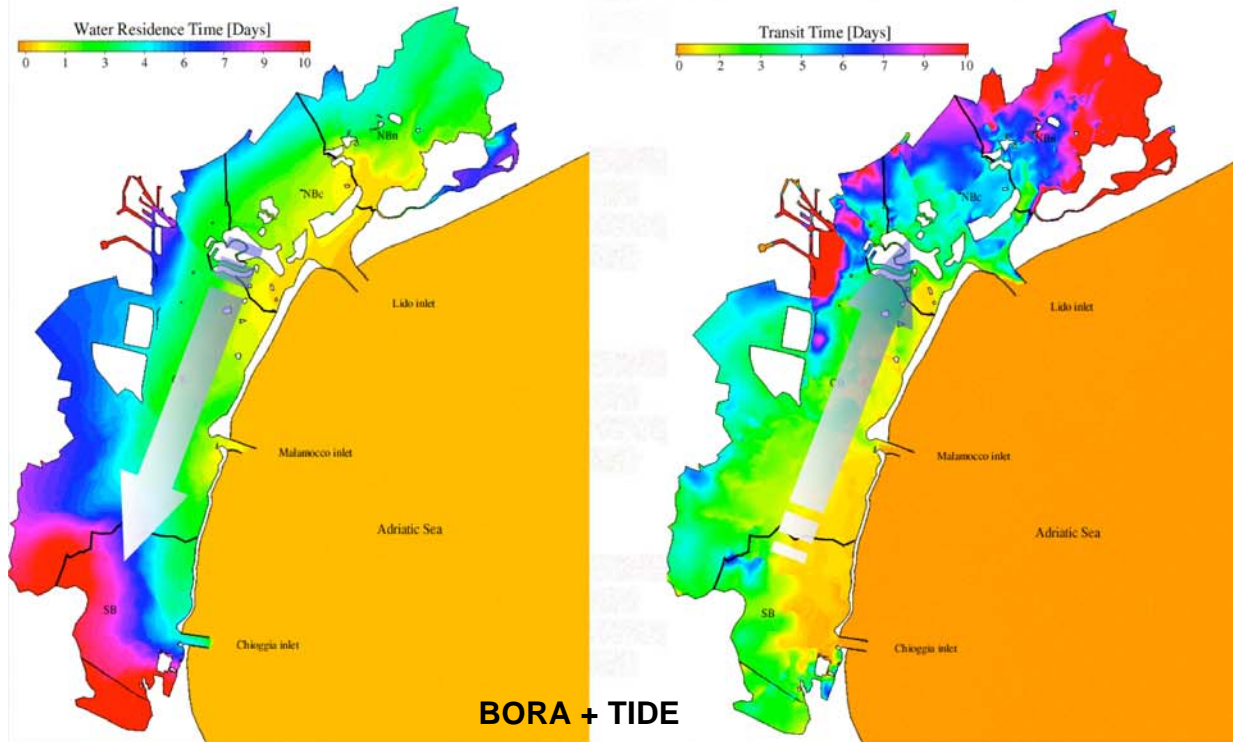


# RESIDENCE TIME VS TRANSIT TIME

## TRAPPING FACTOR

SIROCCO + TIDE	Total	NBn	NBc	CB	SB
WRT	16 ± 8	38 ± 9	23 ± 6	10 ± 6	2 ± 1
WTT	18 ± 9	37 ± 14	11 ± 6	10 ± 5	13 ± 6

BORA +TIDE	Total	NBn	NBc	CB	SB
WRT	4 ± 4	3 ± 1	2 ± 1	5 ± 3	7 ± 3
WTT	4 ± 2	9 ± 4	4 ± 1	3 ± 2	2 ± 1

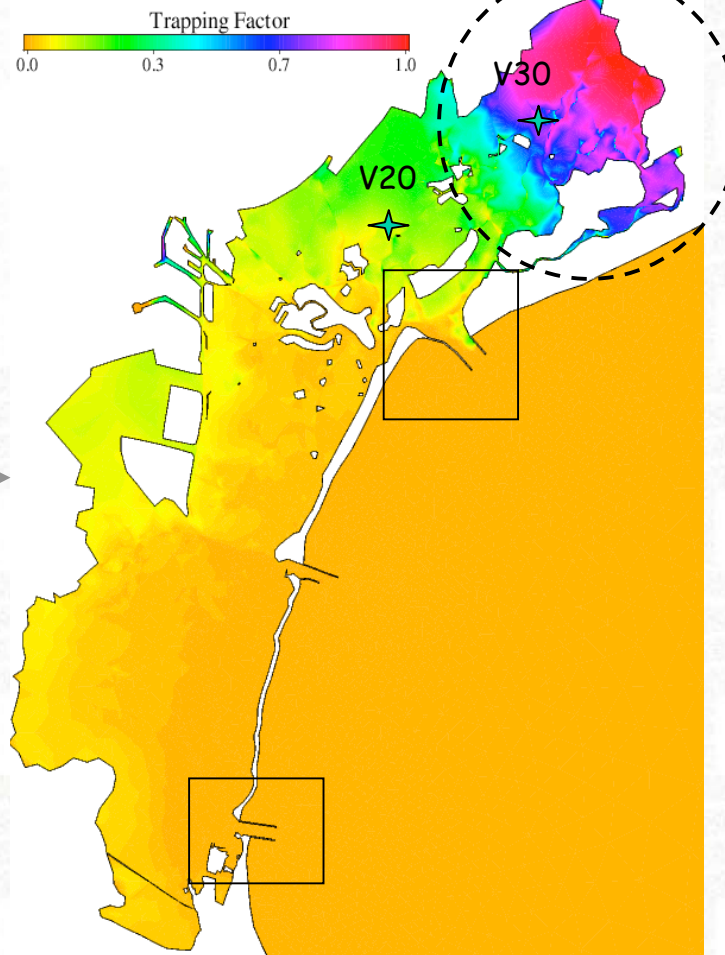


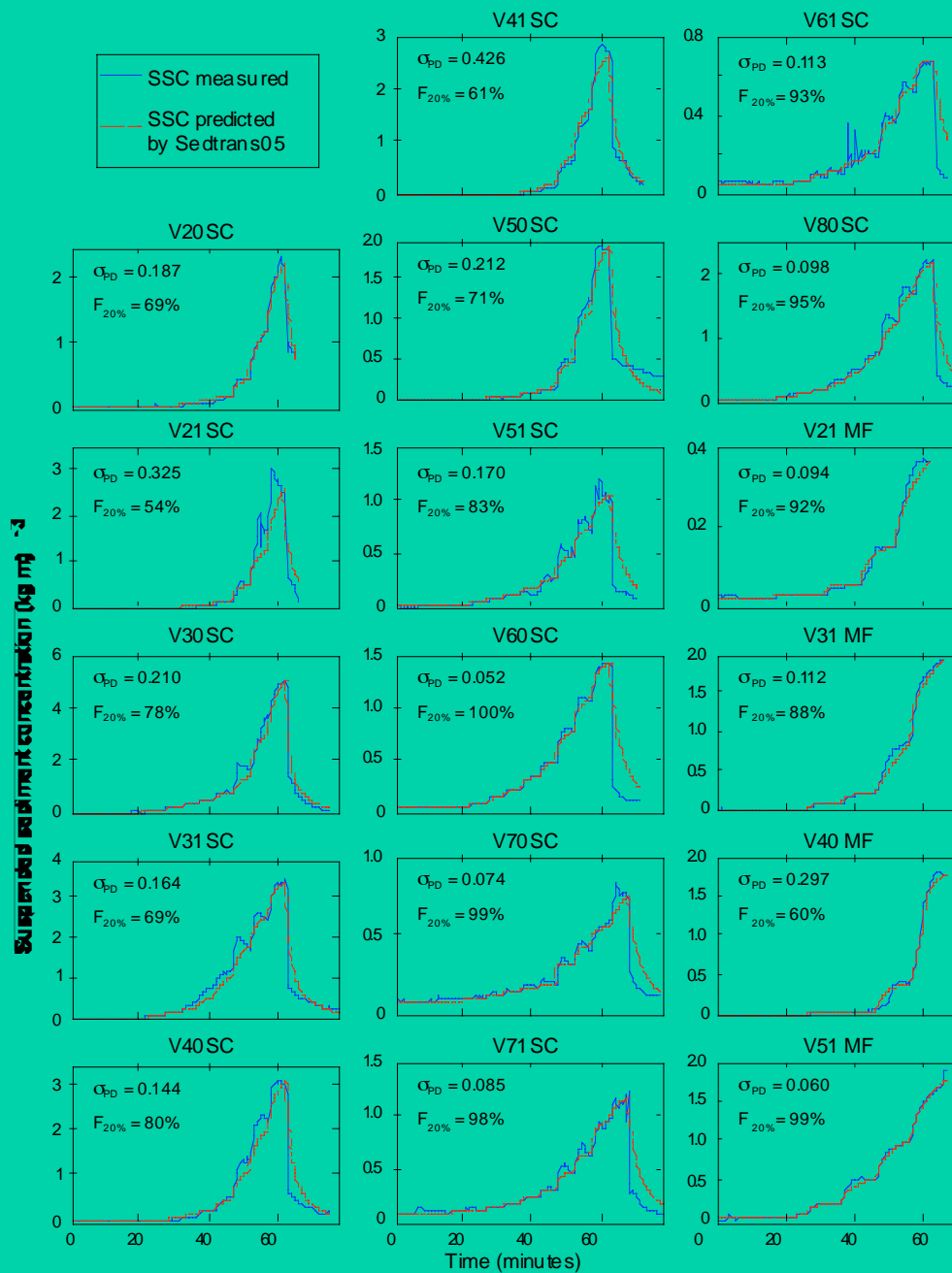
**THEY SEEM TO  
BE CORRELATED !**

# SCENARIO: TIDE AND SIROCCO WIND (7 m/s) ↗

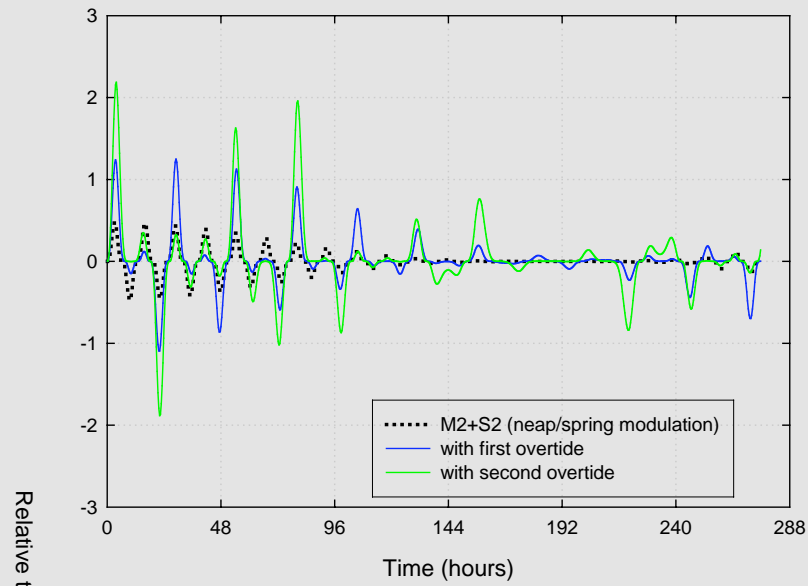
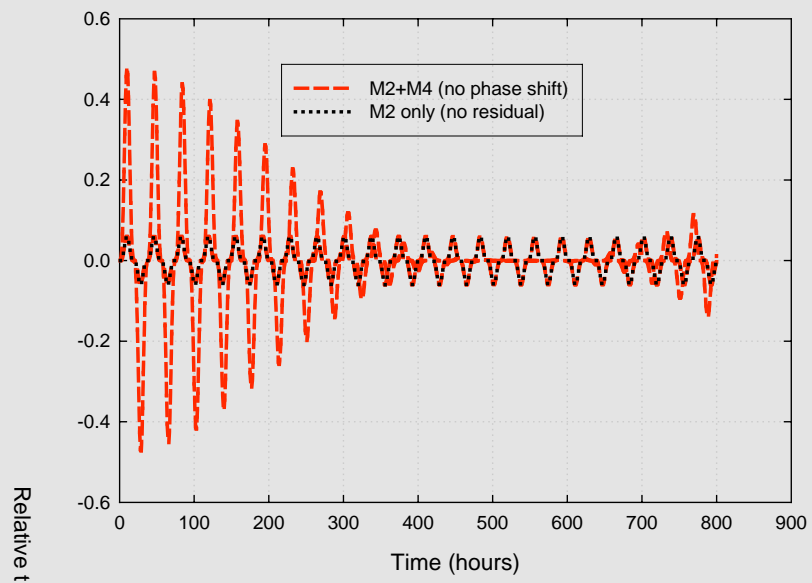
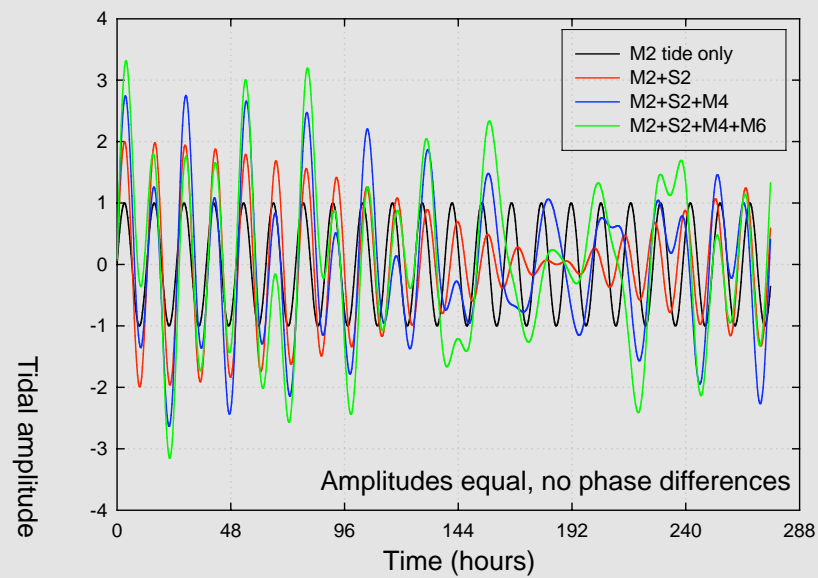
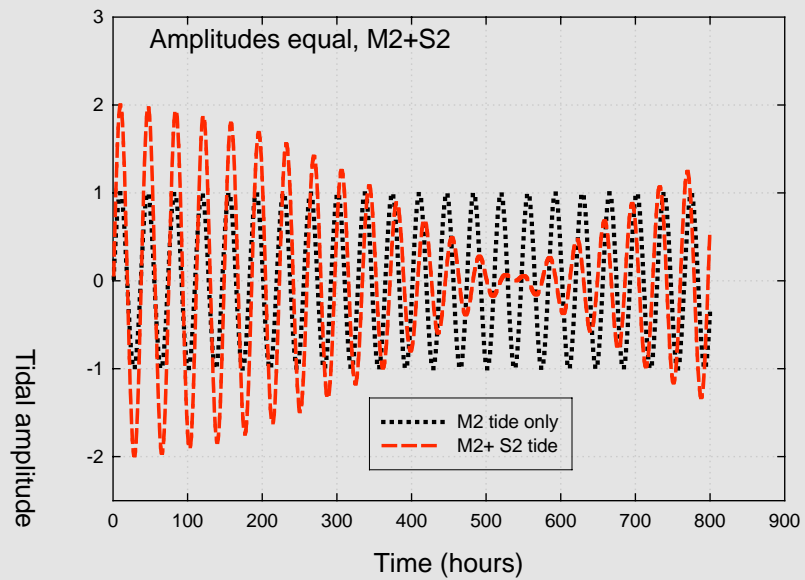
SIROCCO + TIDE	Total	NBn	NBc	CB	SB
WRT	16 ± 8	38 ± 9	23 ± 6	10 ± 6	2 ± 1
WTT	18 ± 9	37 ± 14	11 ± 6	10 ± 5	13 ± 6

CF = 0.09

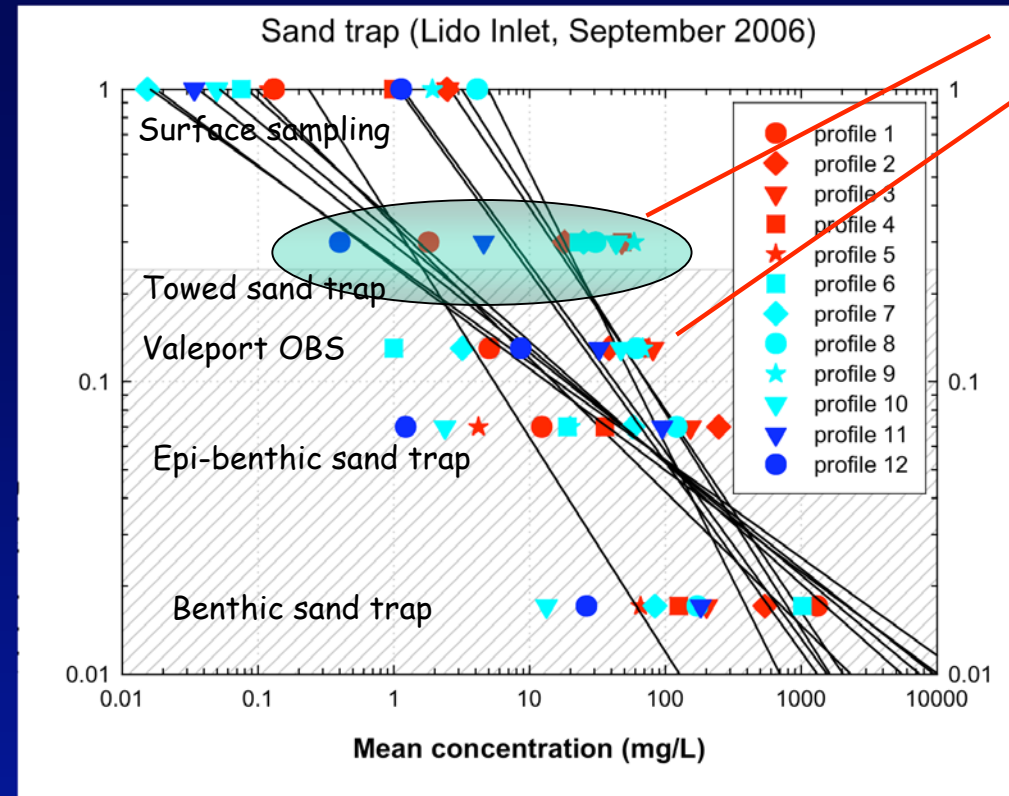




A comparison of the cohesive sediment algorithm with field data collected with the Sea Carousel (SC) and the field MiniFlume (MF) at different stations in Venice lagoon, February 1999. For each experiment, the time-series of SSC measured and predicted by Sedtrans05, the standard deviation of the proportional difference ( $\sigma_{PD}$ ), and the time percentage when the difference is less than 20% ( $F_{20\%}$ ) are shown.







Lido Sud (fixed ADCP site)  
Shaded region is the shadow zone of ADCP

PROFILE	R-squared	offset	1/m
1	0.97	-0.46	-2.17
2	0.96	0.29	-1.64
3	0.85	0.37	-1.35
4	0.76	0.04	-1.56
5	0.61	-0.04	-2.44
6	0.75	-0.53	-2.70
7	0.76	-0.61	-2.86
8	0.91	0.64	-1.08
9	0.43	0.02	-1.54
10	0.44		-3.03
11	0.89	-0.50	-2.56
12	0.51	-0.05	-1.37

$$\log_{10}(z) = m \log(C) + b$$

$$C = (z)^{\frac{1}{m}} 10^{\frac{-b}{m}}$$

Suspension number  
Our results  $1/m = -1.77$

Suspension throughout  
water column at peak  
flows

Stratification at Ht  
and LT

$$\frac{1}{m} = \left( \frac{W_s}{\beta \kappa U_*} \right) \approx -1.77$$

$$\left| \frac{W_s}{U_*} \right| = \beta m \kappa \approx 0.71$$

$$m = 0.56; k = 0.4; \beta = 1$$